

1 **Effect of Stratiform Heating on the Planetary-Scale Organization**  
2 **of Tropical Convection**

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## ABSTRACT

7  
8 It is widely recognized that stratiform heating contributes significantly to tropical rainfall  
9 and to the dynamics of tropical convective systems by inducing a front-to-rear tilt in the  
10 heating profile. Stratiform anvils forming in the wake of deep convection play a central role  
11 in the dynamics of tropical mesoscale convective systems; The wide spreading of stratiform-  
12 rain-evaporation downdrafts, originating from in the lower troposphere, strengthen the re-  
13 circulation of subsiding air in the neighborhood of the convection center and trigger cold  
14 pools and gravity currents in the boundary layer leading to further lifting, thus helping the  
15 mesoscale organization of convection. Here, aquaplanet simulations with a warm pool like  
16 surface forcing, based on a coarse-resolution GCM , of  $\sim 170$  km grid mesh, coupled with a  
17 stochastic multcloud parameterization, are used to demonstrate the importance of strati-  
18 form heating for the organization of convection on planetary and intraseasonal scales. When  
19 some key model parameters are set to produce higher stratiform heating fractions, the model  
20 produces low-frequency and planetary-scale MJO-like wave disturbances while lower to mod-  
21 erate stratiform heating fractions yield mainly synoptic-scale convectively coupled Kelvin-like  
22 waves. Furthermore, it is shown that when the effect of stratiform downdrafts is reduced  
23 in the model, the MJO-scale organization is weakened and a transition to synoptic-scale  
24 organization appears despite the use of larger stratiform heating parameters. Rooted from  
25 the stratiform instability, it is conjectured here that the strength and extent of stratiform  
26 downdrafts are key contributors to the scale selection of convective organizations perhaps  
27 with mechanisms that are in essence similar to those of mesoscale convective systems.

# 1. Introduction

Despite the continued progress in our understanding of precipitation and cloud processes in the tropics, their representation in coarse-resolution global climate models (GCMs) remains a challenge (Lin et al. 2006; Kim et al. 2009; Hung et al. 2013). The difficulty arises, because the underlying cumulus parameterization schemes used to represent unresolved convective process do not take into account the multi-scale character of organized tropical convection and the inherent interactions across time and spatial scales (Moncrieff and Klinker 1997; Majda 2007). At the heart of these complex interactions, tropical convection involves four main cloud types: (1) shallow cumulus clouds with tops below the temperature inversion just above the planetary boundary layer (PBL), that evolve in the subsidence regions of high convective inhibition, (2) cumulus congestus clouds with tops below the freezing level that are abundant in regions of low mid-tropospheric humidity, (3) deep convective towers that nearly reach the tropopause, which take over when the mid-troposphere is moist enough, and (4) stratiform clouds that typically develop in the upper troposphere, above the freezing level, in the wake of deep convection (Johnson et al. 1999; Lin et al. 2004; Mapes et al. 2006). We note that in contrast to stratiform clouds which expand horizontally, over a few hundred kilometres, the former three types are narrow (0.1-10 km in horizontal extent) and expand rather vertically. Their cloud base is found just above the top of the PBL, at the (first) lifting condensation level.

The occurrence of these cloud-types at a given point in time and space is largely controlled by the environmental conditions, as described above. However, due to large uncertainties and inaccuracies in the GCM state variables, a variety of cloud-type populations could in principle be present at the same time within the same GCM grid-box. Moreover, clouds have the ability to change considerably their environment either directly through exchange of latent heat associated with phase change of water and turbulent mixing (i.e. detrainment) or indirectly by modification of the radiation budget (Emanuel 1994). In this way, clouds are able to interact with each other and constitute a non-negligible source of climate variability

55 not directly captured by the GCM mesh size or time step. In terms of latent heating, the  
56 congestus, deep, and stratiform clouds are known to affect the environment in three different  
57 ways. Cumulus congestus warm the lower troposphere and cool the upper troposphere,  
58 by radiative cooling and detrainment at cloud top, and deep convective towers warm the  
59 whole troposphere quasi-uniformly, while stratiform clouds warm the upper troposphere and  
60 cool the lower troposphere, through the evaporation of stratiform rain. In addition to the  
61 warming and cooling effects, clouds have an impact on the distribution of moisture. Pre-  
62 existing cloud-types are thus able to create conditions that are favourable or unfavourable  
63 to new cloud types. For example it is believed that congestus clouds help moisten the mid-  
64 troposphere prior to deep convection while stratiform cloud decks develop on the remains of  
65 deep convective towers. In return, the evaporative cooling induced by stratiform rain drives  
66 downdrafts that cool and dry the PBL with a twofold consequence. The cooling and drying  
67 of the PBL locally decreases the instability for moist convection (i.e. convective available  
68 potential energy, CAPE) which causes convection to cease and at the same time triggers the  
69 propagation of cold pools and gravity currents or bores which cause the deepening of the PBL  
70 in the neighbourhood of the initial cloud (Mapes 1993; Houze Jr. 1997). The PBL deepening  
71 decreases convective inhibition and allows convection to develop in the neighbourhood of an  
72 existing or recently ceased convective tower. Moreover, stratiform heating induces a front-  
73 to-rear tilted heating profile which plays a crucial role in the MJO dynamics and organized  
74 convective systems in general (Kiladis et al. 2005; Lin et al. 2004; Lappen and Schumacher  
75 2014).

76 These complex processes just described are believed to be among the main mechanisms  
77 that allow convection to be “gregarious” (Mapes 1993) and lead to its organization into  
78 mesoscale cloud clusters and super-clusters (Nakazawa 1988). Nonetheless, large-scale cir-  
79 culation patterns associated with synoptic- and planetary-scale convective systems, such as  
80 convectively coupled equatorial waves (CCEWs) and the Madden-Julian oscillation (MJO)  
81 are believed to be favourable for convective organizations, by providing for instance large-

82 scale convergence of moisture at low-levels. The chicken-and-egg question associated with the  
83 two-way interactions between convection and the large-scale flow is a long standing problem.  
84 However, there appears to be some sort of consensus in the tropical meteorological commu-  
85 nity that at least for the MJO initiation both bottom-up and top-down energy cascades can  
86 be encountered in nature depending on whether we are in the presence of a primary or a  
87 successive MJO event (Matthews 2008; Zhang et al. 2013). Successive MJO’s seem to be  
88 triggered by the remains of preceding MJO events, in a form of circumnavigating dry Kelvin  
89 waves (Matthews et al. 1999; Ajayamohan et al. 2013) while primary MJO’s are believed to  
90 be initiated in situ perhaps due to the gregarious nature of tropical clouds.

91 The pre-dominance of stratiform clouds in organized tropical convective systems and  
92 their importance for the latter’s propagation and maintenance is widely recognized ( Houze  
93 Jr. 1997; Tokay et al. 1999; Schumacher and Houze Jr. 2003; Jakob and Schumacher 2008;  
94 Sharma et al. 2009; Zhang and Hagos 2009; Tao et al. 2010). It is for instance widely recog-  
95 nized that the upper tropospheric outflows and implied subsidence associated with stratiform  
96 anvils play a pivotal role in the dynamics, organization, and overall morphological structure  
97 of meso-scale systems that develop in the Atlantic and Eastern Pacific ITCZ and many  
98 other parts in the globe (Dudhia and Moncrieff 1987; Parker and Johnson 2004; Khouider  
99 and Moncrieff 2015). Also several observation and modelling studies have demonstrated  
100 that stratiform clouds directly associated with deep convection and the implied tilted heat-  
101 ing structure play a crucial role in the dynamics and propagation of the MJO and CCEWs as  
102 well as monsoon intraseasonal oscillations and low pressure systems (Lin et al. 2004; Lappen  
103 and Schumacher 2014; Choudhury and Krishnan 2011). Some important questions however  
104 remain. For example, how significantly and differently does stratiform heating and strati-  
105 form rain affect the MJO versus CCEWs? What distinguishes planetary-scale organization  
106 of tropical convection from its synoptic-scale counterpart? In this paper we use a coarse-  
107 resolution GCM with a stochastic parameterization of convection, based on the multcloud  
108 paradigm discussed above to contribute to these questions.

109 The multicloud model, in its deterministic version, was introduced in Khouider and  
110 Majda (2006), and further modified in Khouider and Majda (2008), as a refinement of  
111 the Majda and Shefter (2001) model for stratiform instability, which itself was inspired  
112 by Mapes (1993) and Mapes (2000). While from the linear theory point of the view, the  
113 stratiform instability yields a scale-selective-growth of moisture coupled gravity waves at  
114 synoptic scales nicely mimicking convectively coupled waves, nonlinear simulations require  
115 an additional mechanism, namely wind induced surface heat exchange (WISHE, Emanuel  
116 1987; Neelin et al. 1987) for the maintenance and propagation of these waves (Majda et al.  
117 2004). Also, in a warm pool setting, i.e. a horizontal distribution of the imposed sea surface  
118 temperature (SST) mimicking the Indian Ocean and Western Pacific warm pool, the wave  
119 activity occurs within the descending branch of the induced Walker cell where the surface  
120 wind is the strongest. Not only this is nonphysical but in addition, the simulation has in  
121 addition the peculiar feature of exhibiting eastward moving waves in the region of near-  
122 surface easterly winds (the eastern side) and westward waves in the region of near-surface  
123 westerlies, which is one of the main characteristics of WISHE waves.

124 WISHE is discarded as a viable mechanism for the MJO because it requires background  
125 easterlies to produce an MJO-like eastward moving disturbance but overall westerlies and/or  
126 very weak westerlies are observed to prevail over the Indian Ocean Western Pacific region in  
127 winter, when the MJO is most active. As demonstrated in Khouider and Majda (2006, 2008,  
128 and subsequent papers), WISHE-free waves with the right physical features are obtained  
129 when a model based on the three cloud types cumulus congestus, deep, and stratiform is  
130 used instead of only deep and stratiform. While the stratiform heating is able to destabilize  
131 the system at the right synoptic scale with the right eigen-structures of super-clusters, it is  
132 not able to sustain it. Cumulus congestus cloud decks that are observed to prevail in the  
133 front of organized convective systems of all scales are the missing link for a successful model  
134 for the two-way interactions between tropical clouds of various types and the associated large  
135 scale waves, including the MJO and CCEWs. Nonetheless, the stratiform instability remains

136 an essential ingredient, though not the only one. As demonstrated in Majda et al. (2004),  
137 the stratiform instability is tied to the parameter  $\mu$  which controls the relative contribution  
138 of stratiform heating in the downdraft closure formula. In the present study we further  
139 demonstrate that the (relative) amount of stratiform heating is the key parameter which  
140 controls the horizontal length-scale at which convection is organized in coarse-resolution  
141 GCM simulations using the stochastic multcloud model as a cumulus parameterization  
142 (Deng et al. 2015, hereafter DKM15).

143 The stochastic multcloud model (SMCM) was first introduced in Khouider et al. (2010)  
144 in order to take into account the unresolved variability due to interactions between various  
145 cloud types, in coarse-resolution GCMs, in the context of the multcloud model. It is used  
146 in Frenkel et al. (2012, 2013) to simulate convectively coupled gravity waves in a simplified  
147 primitive equations model. In DKM15, the SMCM was implemented in the High Order  
148 Methods Modelling Environment (HOMME) dynamical core as a cumulus parameterization  
149 for coarse-resolution GCM simulations, following Khouider et al. (2011) who previously used  
150 the deterministic MCM. Taken together, the HOMME-MCM and HOMME-SMCM models  
151 are very successful in simulating the MJO and CCEWs as well as monsoon-like intraseasonal  
152 oscillations (Khouider et al. 2011; Ajayamohan et al. 2013, 2014; DKM15). However, so far  
153 the HOMME-SMCM model is used only for the aquaplanet MJO simulations on a uniform  
154 SST background. Here we further introduce a warm pool like SST in the HOMME-SMCM  
155 model and study the sensitivity of the results to two key parameters which control the  
156 amount, i.e, the strength and temporal and spatial extent, of stratiform heating produced by  
157 the model and further investigate whether the stratiform instability mechanism is responsible  
158 for this sensitivity.

159 The paper is organized as follows. In Section 2, we discuss briefly the model set up and  
160 present the results of an MJO simulation in a typical parameter regime as our control simula-  
161 tion. Sensitivity tests to key stratiform parameters are presented in Section 3. In Section 4,  
162 we demonstrate that the effect on the planetary-scale organization due to stratiform heating

163 can be explained in large part by the mechanism of downdrafts induced by the evaporation of  
164 stratiform rain which helps re-moisten the mid-troposphere and cool and dry the boundary  
165 layer. The latter makes cold pools that expand and strengthen with the extent and strength  
166 of the stratiform heating, and which are believed to play a major role in re-initiating new  
167 convection in the neighbouring grid cells thus leading to propagating organized convective  
168 systems, cf. the stratiform instability (Majda and Shefter 2001; Mapes 2000). A summary  
169 and conclusion is given in Section 5.

## 170 **2. Model setup and control experiment**

171 In this section we briefly review the implementation of the global atmospheric model  
172 HOMME-SMCM and highlight the key parameters which control the strength and extent  
173 of the stratiform heating, the focus of the present paper. More details on the model's  
174 framework can be found in DKM15 and the references therein. A control experiment in  
175 a typical parameter regime simulating the MJO evolution and variability within the warm  
176 pool is also presented.

### 177 *a. Model setup*

178 The SMCM-HOMME model uses the High Order Methods Modelling Environment model  
179 of the National Center for Atmospheric Research (Taylor et al. 1997; Dennis et al. 2005; Nair  
180 et al. 2009) as a dry-dynamical core coupled to the stochastic multcloud model (SMCM)  
181 of Khouider et al. (2010) as a cumulus parameterization. Apart from boundary layer and  
182 upper tropospheric damping the model is free of any other physics, expect for the cumulus  
183 heating provided by the SMCM. HOMME is a highly scalable dynamical core based on  
184 spectral elements in the horizontal and finite differences in the vertical and uses a cubed  
185 sphere geometry. In our setting, each face of the cube carries 20 integration elements of  
186 four degrees of freedom. This is roughly equivalent to a horizontal grid size of 167 km. We



187 use 26 vertical levels and a time step of 30 seconds. The SMCM carries equations for the  
 188 vertically integrated moisture and boundary layer equivalent potential temperature which  
 189 are integrated in parallel with the dynamical core. The SMCM routine includes an imposed  
 190 uniform cooling with a strength of roughly 1 K day<sup>-1</sup> and a baroclinic vertical profile.

191 In the SMCM, the vertical profiles of convective heating and cooling associated with the  
 192 congestus, deep, and stratiform cloud types are prescribed while the heating rates ( $H_c$ ,  $H_d$   
 193 and  $H_s$ ) obey the closure equations in (1).

$$\begin{aligned}
 H_c &= \sigma_c \frac{\alpha_c \bar{\alpha}}{H_m} \sqrt{CAPE_l^+} \\
 H_d &= \sigma_d \left\{ \bar{Q} + \frac{1}{\bar{\sigma}_d \cdot \tau_{conv}} [a_1 \theta_{eb} + a_2 q - a_0 (\theta_1 + \gamma_2 \theta_2)] \right\}^+ \\
 H_s &= \sigma_s \alpha_s \left\{ \bar{Q} + \frac{1}{\bar{\sigma}_s \cdot \tau_{conv}} [a_1 \theta_{eb} + a_2 q - a_0 (\theta_1 + \gamma_2 \theta_2)] \right\}^+.
 \end{aligned} \tag{1}$$

194 Here  $q$  is the vertically averaged tropospheric moisture and  $\theta_{eb}$  is the boundary layer equiv-  
 195 alent potential temperature, while  $\theta_1$  and  $\theta_2$  are respectively the first and second baroclinic  
 196 components associated with the vertical mode expansion (Khouider et al. 2011). The rest  
 197 of the involved variables and parameters are listed in Tables 1 and 2 for the sake of stream-  
 198 lining. The heating profiles are based on the first and second baroclinic vertical structure  
 199 basis functions so that deep convection heats the entire troposphere (up to 200 hPa) while  
 200 congestus (stratiform) clouds warm (cool) the lower troposphere and cool (warm) the upper  
 201 troposphere. More details can be found in Khouider et al. (2011). The combined heating  
 202 profile provide the cumulus heating and cooling tendency for the temperature equation and  
 203 drives the HOMME dynamical core.

204 The boundary layer equivalent potential temperature  $\theta_{eb}$  and vertical average moisture  $q$   
 205 which appear in the closure equations in (1) satisfy,

$$\begin{aligned}
 \frac{\partial \theta_{eb}}{\partial t} + \mathbf{u}(x, y, p_1, t) \cdot \nabla \theta_{eb} &= \frac{1}{h} E_s - \frac{1}{h} D \\
 \frac{\partial q}{\partial t} + \nabla \cdot [q(\bar{\mathbf{u}} + \mathbf{u}_1 + \tilde{\alpha} \mathbf{u}_2)] + \tilde{Q}_1 \nabla \cdot \mathbf{u}_1 + \tilde{Q}_2 \nabla \cdot \mathbf{u}_2 &= -P + \frac{D}{H}.
 \end{aligned} \tag{2}$$

206 Here  $E_s$  is the evaporation from the sea surface, and  $D$  is the downdraft mass flux:

$$\frac{1}{h}E_s = \frac{1}{\tau_e}(\theta_{eb}^* - \theta_{eb}), \quad D = \frac{m_0}{Q_{R,1}^0}[Q_{R,1}^0 + \mu(H_s - H_c)]^+(\theta_{eb} - \theta_{em}), \quad (3)$$

207 where  $\theta_{eb}^*$  is the boundary layer saturation equivalent potential temperature and  $\theta_{em}$  is the  
 208 middle tropospheric equivalent potential temperature.  $P$  is the surface precipitation. In  
 209 Eq. (2),  $\mathbf{u}(x, y, p_1, t)$  is the horizontal velocity at the lowest model (pressure) level while  $\bar{\mathbf{u}}$ ,  
 210  $\mathbf{u}_1$ ,  $\mathbf{u}_2$  are, respectively, the barotropic and first and second baroclinic horizontal velocity  
 211 components. Here  $(x, y)$  are the longitude and latitude coordinates and  $\nabla$  is the associated  
 212 horizontal gradient vector. We note that the stratiform heating directly effects the downdraft  
 213 mass flux [Eq. (3)] through the parameter  $\mu$  which in turn acts simultaneously on the  
 214 tropospheric moisture  $q$  and the boundary layer  $\theta_e$ . The latter effect drives cold pools in the  
 215 boundary layer which are believed to help the initiation of new convection in the neighbouring  
 216 grid cells and lead to propagating organized convective systems via the stratiform instability  
 217 (Majda and Shefter 2001). The default parameters for the multcloud parameterization  
 218 equations in (1), (2), and (3) are given in Table 1. They are the same as in DKM15. Unless  
 219 otherwise specified, these parameter values are used throughout the present study. We note  
 220 that for consistency moisture variables are expressed in temperature units.

221 As formulated in (1), the heating rates are proportional to the congestus, deep and  
 222 stratiform cloud area fractions ( $\sigma_c$ ,  $\sigma_d$  and  $\sigma_s$ , respectively). The cloud area fractions are  
 223 simulated by a stochastic lattice model and they are the source of stochasticity, i.e. sub-  
 224 grid variability, in the SMCM. Each GCM horizontal grid box is overlaid by a rectangular  
 225  $n \times n$  lattice, and each lattice site is assumed to be either clear sky or occupied by a  
 226 congestus, deep or stratiform cloud. The cloud area fractions are defined as the area coverage  
 227 of the microscopic lattice by the sites occupied by each one of the three cloud types. A  
 228 judicious coarse graining then permits to recover the exact dynamics, in the case of non-  
 229 local interactions between lattice sites (Khouider et al. 2010), or approximate dynamics,  
 230 in the case of nearest neighbour interactions (Khouider 2014), for the meso-scopic cloud  
 231 area fraction, on the form of a three-species birth-death process at each GCM grid box.

232 The area-fraction birth-death process is evolved in time using Gillespie’s exact algorithm  
 233 (Gillespie 1975, 1977) in a straight forward fashion with very little computational overhead.  
 234 Due to the extra uncertain parameters associated with local interactions, only the SMCM  
 235 with non-local interactions of Khouider et al. (2010) is considered here. The implementation  
 236 of the SMCM with local interactions (Khouider 2014) is left for future developments.

237 In the SMCM, each individual cloud site makes random transitions from one state to  
 238 another according to intuitive probability rules depending on whether the environment is  
 239 favourable to one cloud type or another. This leads to a Markov process with conditional  
 240 transition rates. The latter are given in Table 2 for streamlining. A given rate  $R_{kl}$  goes up or  
 241 goes down according to whether the environment is favourable to the associated transition or  
 242 not. For instance, the transition rates from clear sky to deep convection and from congestus  
 243 to deep convection both increase with both CAPE and mid-tropospheric moistness. This  
 244 mainly inhibits deep convection when the troposphere is dry to allow a more physical–  
 245 progressive transition to deep convection as observed in nature.

246 The transition rates in Table 2 are given in terms of transition time scales denoted by  $\tau_{kl}$ .  
 247 They form a set of seven parameters whose values are uncertain. However some attempts to  
 248 infer them from data do exist (Peters et al. 2013; De La Chevrotiere et al. 2014). To take  
 249 into account the dependence of these parameters on the GCM grid resolution (in a crude  
 250 way), the extra parameter  $\tau_{grid}$  is introduced in FMK12. Following DKM15, here we use  
 251  $\tau_{grid} = 2$ . The number of lattice sites,  $n \times n$  is another important parameter of the SMCM.  
 252 Here we use the conservative value of  $n = 40$ . The sensitivity of the results to both  $\tau_{grid}$  and  
 253  $n$  is documented in DKM15.

254 To limit the effect of the cumulus heating to the tropics, we introduce a mask in the  
 255 meridional direction. It is set to one for latitudes between  $30^\circ$  S and  $30^\circ$  N and rapidly  
 256 and smoothly decreases to zero towards the poles (Khouider et al. 2011). Moreover, a non-  
 257 uniform sea surface temperature (SST) mimicking the Indian Ocean/Western pacific warm  
 258 pool is imposed through the prescribed surface evaporation rate,  $\frac{1}{\tau_e}(\theta_{eb}^* - \bar{\theta}_{eb})$ , which is raised

259 above its spatial mean by up to 5 K per  $\tau_e$  inside the warm pool region and lowered by the  
 260 same amount, outside, as illustrated in Figure 1 (see Ajayamohan et al. 2013). As shown  
 261 in (1), the stratiform heating rate is controlled by two key factors, namely, the stratiform  
 262 fraction  $\alpha_s$  and the stratiform cloud area fraction  $\sigma_s$ . While  $\alpha_s$  is a constant that can be  
 263 adjusted directly beforehand, the area fraction  $\sigma_s$  is a random variable which evolves during  
 264 the simulation. However, the relative strength and dynamics of the cloud area fractions are  
 265 strongly modulated by the transition rates in Table 2. For instance, persistent large areas  
 266 of stratiform cloud decks can be easily achieved by using large stratiform cloud decay time  
 267 scale,  $\tau_{30}$ , values. The same can be achieved through changes of other transition time scale  
 268 combinations but here only changes in  $\tau_{30}$  are considered, for the sake of simplicity.

269 *b. Control experiment*

270 As a first experiment, we consider the standard parameter values in Tables 1 and 2.  
 271 These are essentially the same values used in DKM15 to successfully simulate the MJO on  
 272 a uniform SST background except for the congestus cloud formation time scale,  $\tau_{01}$ , which  
 273 is increased from  $\tau_{01} = 1\tau_{grid}$  to  $\tau_{01} = 40\tau_{grid}$  (Table 2) and the deep cloud formation time  
 274 scale,  $\tau_{02}$ , which in turn is increased from  $\tau_{02} = 3\tau_{grid}$  to  $\tau_{02} = 4\tau_{grid}$ . This allows to  
 275 decrease the amount of congestus heating which otherwise leads to unrealistic results in the  
 276 present warm pool setting. This due essentially to the fact that the warm pool forcing yields  
 277 large CAPE values which increases the potential for congestus clouds; the transition time  
 278 scales introduced here counter balances this increase in CAPE. In particular, the stratiform  
 279 parameters are set to  $\alpha_s = 0.50$  and  $\tau_{30} = 5\tau_{grid}$ .

280 The Hovmöller diagrams of the meridionally averaged ( $10^\circ\text{S}$  to  $10^\circ\text{N}$ ) lower level and  
 281 upper level zonal winds are shown in Figure 2 followed by those of the convective heating  
 282 rates,  $H_d, H_c, H_s$  and vertical average moisture,  $q$ , in Figure 3. Successive well-organized  
 283 propagating convective systems are clearly seen in all of these plots, starting at the west  
 284 edge of the warm pool and slowly moving to the east at roughly  $5 \text{ m sec}^{-1}$ . Moreover, the

285 low-frequency and small-wavenumber peaks in the spectrum power plots in Figure 4 confirm  
286 the intraseasonal/planetary-scale variability which characterizes the simulation. These MJO-  
287 like events have in addition the typical quadrupole vortex and tilted vertical structures (not  
288 shown) which characterize the MJO, consistent with earlier multcloud results (Khouider  
289 et al. 2011; Ajayamohan et al. 2013; DKM15, etc).

290 Figure 5 depicts the time series of the cloud area fractions and heating rates averaged over  
291 a few grid points over the warm pool. As expected, the heating rates and the corresponding  
292 cloud area fractions are oscillating intensively and synchronously during the active phases of  
293 the MJO events. In particular, the area fraction time series exhibit an intermittent and yet  
294 causal variation as seen in observation, e.g., the radar data at Darwin, Australia in Peters  
295 et al. (2013).

### 296 **3. Stratiform transition from CCWs to MJO regimes**

297 Three more experiments (Table 3) are conducted to understand the response of planetary-  
298 scale organization to changes in the strength and extent of stratiform heating. As mentioned  
299 earlier, two key parameters that directly affect the stratiform heating strength and extent are  
300  $\alpha_s$  and  $\tau_{30}$  (1). The set of all numerical experiments conducted in this study are summarized  
301 in Table 3.

302 In EXP2, we decrease  $\alpha_s$  to 0.25 and keep  $\tau_{30} = 5\tau_{grid}$  to separate the effect of the two  
303 parameters. The associated Hovmöller and spectrum power diagrams are shown in Figures 6,  
304 7 and 8. From these figures we see that the variability has moved to synoptic scales and the  
305 MJO-like propagating streaks and associated low-frequency spectral power have both dimin-  
306 ished. While a few streaks of slowly moving planetary-scale wave-like signals are still visible  
307 in the Hovmöller diagram of the 200 hPa wind, the variability of deep and stratiform heating  
308 rates and especially moisture are dominated by synoptic-scale waves that move eastward at  
309 speeds approaching 10 m sec<sup>-1</sup>. While this speed is smaller than what is typically observed

310 for convectively coupled Kelvin waves, it can be readily seen that the spectrum power is  
 311 aligned linearly as it is following a dispersion-less dispersion curve of Kelvin waves with a  
 312 reduced equivalent height. However, when the data is filtered following the wavenumber-  
 313 frequency box shown in the spectrum power plot of deep convection in Figure 8 (a technique  
 314 initially used in Wheeler and Kiladis 1999), the corresponding horizontal and vertical struc-  
 315 tures, reported in Figure 9 do not seem to resemble those of typical convectively coupled  
 316 Kelvin waves. Unlike those reported in Khouider et al. (2011) for the case of a uniform  
 317 SST background, the waves in Figure 9 carry a non-trivial meridional velocity converging  
 318 at lower level towards the equator, within the region of active convection (corresponding  
 319 roughly to the region of zonal convergence). This is consistent with the structure of Kelvin  
 320 waves evolving in a meridional shear background (Ferguson et al. 2009; Han and Khouider  
 321 2010). Indeed this is unlike the MJO which instead exhibits Rossby gyres on both sides of  
 322 the convection center and zonal convergence along the equator; For the MJO the meridional  
 323 divergence at low level is positive, within the convection center. Nonetheless, the backward  
 324 vertical tilts are still prominent as seen on the bottom panels (e, f) of Figure 9.

325 Next (EXP3), we keep the small value  $\alpha_s = 0.25$  as in EXP2 but increase the stratiform  
 326 transition time scale to  $\tau_{30} = 10\tau_{grid}$ . Intuitively, this will have the effect of making stratiform  
 327 clouds last longer and thus expand in both time and space. In Figures 10 to 12, we show  
 328 the Hovmöller and spectrum power diagrams of the meridionally averaged zonal winds and  
 329 heating rates. Clearly, the planetary-scale organization of MJO-like waves are successfully  
 330 recovered as in the case of EXP1.

331 To further demonstrate the tendency of stronger stratiform heating to yield better MJO  
 332 simulation, we did another experiment with  $\alpha_s = 0.75$  and  $\tau_{30} = 5\tau_{grid}$  (results not shown).  
 333 It resulted in similar and slightly stronger MJO-like organization than EXP1 and EXP3.  
 334 However, if on the other hand we use the same large stratiform fraction  $\alpha_s = 0.50$  as in  
 335 EXP1 but combine it with a smaller transition time  $\tau_{30} = 2\tau_{grid}$  (EXP4), similarly to EXP2  
 336 ( $\alpha_s = 0.25, \tau_{30} = 5\tau_{grid}$ ), the planetary-scale organization of MJO-like waves is replaced

337 by convectively coupled Kelvin waves, which as in EXP2 dominate the warm pool region  
338 (results not shown).

339 Two statistical measures (one being the auto-correlation function of the precipitation  
340 and column averaged moisture and the other the frequency of precipitation events) of the  
341 four experiments (EXP 1-4) are reported in Figures 13 and 14. As in DKM15, for all the  
342 experiments, the auto-correlation of the precipitation is much shorter than the moisture,  
343 which is qualitatively consistent with observational studies (e.g., Holloway and Neelin 2009,  
344 2010). Also consistent with the results of DKM15, in the two experiments with clear MJO-  
345 like events (EXP 1 and 3), the moisture has much longer auto-correlation times. Moreover,  
346 the observed two-power-law structure of precipitation event distributions is captured in all  
347 of these four experiments consistent with the observations reported in Neelin et al. (2008)  
348 and Peters et al. (2010), consistent with the results of DKM15.

## 349 **4. The stratiform organization mechanism**

350 In this section we attempt to elucidate the physical mechanism through which the strat-  
351 iform heating affects the development of planetary-scale organized MJO-like waves. The  
352 stratiform heating affects the coupled HOMME-SMCM model in two distinct fashions. One  
353 is through the differential heating and cooling of the upper and lower troposphere, which  
354 results in a tilted heating profile acting directly on the free tropospheric dynamics and the  
355 other through the moist thermodynamic variables. As already pointed out, the evaporation  
356 of stratiform rain in the lower troposphere acts as a source of mid-tropospheric re-moistening  
357 and at the same time dries and cools the boundary layer via the induced downdrafts. The  
358 latter effects are taken into account in the SMCM model via the parameter  $\mu$  present in the  
359 downdraft equation [Eq. (3)]. The tilted heating is undoubtedly important for successful  
360 MJO and CCWs simulation in GCMs (e.g., Khouider et al. 2011; Lappen and Schumacher  
361 2014) but by the SMCM model design both congestus and stratiform heating contribute to

362 the front-to-rear tilting of the MJO heating profile. Given that a strong congestus heating  
363 does not lead to a better MJO simulation, by EXP8 of this study and many other tests not  
364 reported here, it is worthwhile investigating the effect of the contribution of the stratiform  
365 heating to the downdraft field.

366 As demonstrated in Majda et al. (2004), through the parameter  $\mu$ , the stratiform heating  
367 controls the scale-selective instability of super-clusters in terms of convectively coupled grav-  
368 ity waves, thus the phrase “stratiform instability”. As pointed out in Majda et al. (2004),  
369 the effect of the downdraft on the boundary layer  $\theta_e$  [Eq. (2)] mimics the dynamics of cold  
370 pools as they expand and spread in time and space following the stratiform heating. The  
371 stronger and more expanded the stratiform heating is, the more prominent the cold pool  
372 effect is.

373 Here we test this mechanism in the context of GCM simulations and see whether it can  
374 explain in part why the simulation of MJO-like planetary-scale organization versus synoptic-  
375 scale CCWs is tied to the amount of stratiform heating, as demonstrated above. To do so,  
376 we conducted a few more experiments where we keep  $\alpha_s = 0.5$  and  $\tau_{30} = 5\tau_{grid}$  as in EXP1  
377 but gradually decrease the value of the parameter  $\mu$ . In Figure 15, we plot the Hovmöller  
378 diagram of deep convective and congestus heating rates for the three values  $\mu = 0.1, 0.05$  and  
379  $0.01$ . As we can see, with  $\mu = 0.1$ , which is equivalent to reducing the effect of stratiform  
380 heating on downdraft by a factor of roughly 2, the change in  $\mu$  doesn’t seem to have a  
381 big impact on the MJO simulation. In fact the MJO events seem to be more persistent  
382 and more organized than in EXP1 (Figure 3) although the heating strength seems to be  
383 a bit weaker with  $\mu = 0.1$ . This is indeed unlike the effect of reducing  $\alpha_s$  by a factor  
384 of two as seen in EXP2 (Figure 7). This is in fact a clear evidence that the importance  
385 of stratiform heating, for planetary-scale organization of convection, is not limited to its  
386 contribution to the downdraft fluxes but has significant impact on the MJO and CCWs  
387 dynamics through its direct contribution to the tilting of the heating (Khouider et al. 2011;  
388 Lappen and Schumacher 2014). Nonetheless, as shown on the bottom panels (e, f) of Figure



389 15, when  $\mu$  is reduced significantly, to  $\mu = 0.01$ , the planetary-scale MJO-like organization  
 390 is lost but the simulation yields instead synoptic-scale eastward CCWs as in EXP2. At  
 391  $\mu = 0.05$ , the planetary-scale blobs of convection begin to fracture and split, though MJO-  
 392 like events clearly remain visible. The progressive transition from MJO-like to synoptic-scale  
 393 organization as  $\mu$  decreases is confirmed by spectral power plots (not shown) although the  
 394 changes are not as dramatic and as clear cut as in tuning  $\alpha_s$  and/or  $\tau_{03}$ . This suggests that  
 395 MJO dynamics are very complex and cannot be explained by a single mechanism or a single  
 396 variable such as column integrated moisture for example. Although, the latter is extremely  
 397 important.

398 Another way to counter the effect of stratiform heating, both in terms of the tilted heating  
 399 and its contribution to downdraft is increasing the amount of congestus heating while the  
 400 stratiform parameters are kept as in EXP1. The increase of lower level heating and upper  
 401 level cooling from increased congestus heating will compensate for the upper troposphere  
 402 heating and lower troposphere cooling from stratiform heating,  $H_s$ . At the same time, the  
 403 congestus heating rate appears in the downdraft equation [Eq. (3)], in front of  $H_s$ , with a  
 404 negative sign. The former will reduce the tilt in the overall heating profile while the latter  
 405 will have the effect of counterbalancing the effect of the contribution of stratiform heating to  
 406 downdraft. In physical terms, the reduction of stratiform induced downdraft by congestus  
 407 heating is the result of the associated compensating updrafts.

408 We thus repeat the simulation EXP1 but with a smaller congestus formation time scale,  
 409  $\tau_{01} = 1\tau_{grid}$  (EXP8) to allow substantial growth of congestus clouds. As we can see from  
 410 Figure 16, not surprisingly, this leads to CCWs type organization as in EXP2 and EXP4.  
 411 This indeed confirms the importance of the two mentioned effects of stratiform heating  
 412 but also the detrimental effect of over compensation by congestus heating. Nonetheless,  
 413 the effect of congestus heating cannot be neglected or left aside as it is the main driver of  
 414 moisture preconditioning, first by delaying deep convection and thus allowing the atmosphere  
 415 to moisten through the detrainment of shallow (and congestus) clouds then by effectively

416 driving low-level moisture convergence (Khouider and Majda 2006). The persistence of  
417 convectively coupled Rossby and Kelvin waves in this congestus dominated dry environment  
418 is consistent with the results of Khouider et al. (2011) who obtained such behaviour when  
419 the background moisture is weak since by the model design a dry environment promotes more  
420 congestus heating. The crucial role of congestus heating and moisture convergence have been  
421 thoroughly documented by two of the authors (e.g., Khouider and Majda 2006, 2008).

## 422 5. Summary and Conclusion

423 Numerical simulations using an atmospheric GCM, with an idealized water-only earth  
424 surface, with no land or topography (an aquaplanet), are presented and analyzed in terms  
425 of the ability of the model to simulate MJO-like wave disturbances. The model is based on  
426 the spectral elements HOMME dynamical core with coarse resolution using the stochastic  
427 multcloud model (SMCM) of Khouider et al. (2010) as a cumulus parameterization following  
428 DKM15. Unlike DKM15, however, here the surface forcing takes the more realistic shape  
429 of the Indian Ocean/Western Pacific warm pool. The current study focuses on the role of  
430 stratiform heating in the model’s capability to reproduce organized tropical convection on  
431 multiple scales.

432 Many previous (modelling and observation) studies have identified stratiform heating as  
433 a major component of organized tropical convection and the MJO in particular (Moncrieff  
434 1981; Dudhia and Moncrieff 1987; Houze Jr. 1997; Schumacher and Houze Jr. 2003; Lin et al.  
435 2004; Parker and Johnson 2004; Mapes et al. 2006; Jakob and Schumacher 2008; Khouider  
436 et al. 2011). It is believed to be important mainly for providing the “required” tilted heating  
437 which characterizes tropical convective systems of all scales (Kiladis et al. 2009; Lin et al.  
438 2004; Lappen and Schumacher 2014) and its ability to drive horizontal vorticity at mesoscales  
439 (Moncrieff 1981, 2010). In particular it has been identified as a source of instability for  
440 super-clusters (Mapes 2000; Majda and Shefter 2001). While many studies identified the

441 importance of the tilted heating structure in, for example, triggering gravity waves that  
442 precondition the environment downstream to new convection (Mapes 1993; Stechmann and  
443 Majda 2009), Majda and Shefter (2001) pinpointed that the so-called “stratiform instability”  
444 is mainly a result of the acceleration of downdrafts through the evaporation of stratiform  
445 rain, which in turn drives cold pools in the boundary layer.

446 Here the crucial role of stratiform heating for the simulation of MJO-like convective orga-  
447 nization in the coupled HOMME-SMCM is tested by changing a few key model parameters.  
448 In a first step, the amount of stratiform heating produced by the model was tested through  
449 two separate parameters, namely, the fraction of stratiform heating,  $\alpha_s$ , together with the  
450 time scale that controls the decay of stratiform cloud area fraction,  $\tau_{30}$ . It is found that these  
451 two parameters affect similarly the model simulations. Large values of either  $\alpha_s$  or  $\tau_{30}$  lead  
452 to planetary-scale intraseasonal MJO-like organized convection while smaller values yield  
453 synoptic-scale convectively coupled Kelvin waves. The fact that these two parameters lead  
454 to the same behaviour is not very surprising since  $\tau_{30}$  strongly modulates the area fraction of  
455 stratiform heating,  $\sigma_s$  and that both  $\alpha_s$  and  $\sigma_s$  appear as pre-factors in the stratiform heat-  
456 ing equation (1). However, the reason why MJO simulation is so sensitive to the stratiform  
457 heating remains to be elucidated.

458 In order to test the role of the stratiform instability as defined in Majda and Shefter  
459 (2001) through the contribution of stratiform heating to downdrafts by the evaporation of  
460 stratiform rain mechanism, we followed up with a series of simulations using decreasing  
461 values of the parameter  $\mu$  which controls the contribution of stratiform rain evaporation  
462 to downdrafts. It is found that for sufficiently small  $\mu$  values, the MJO-like organization  
463 disappears and is replaced by convectively coupled Kelvin waves as in the cases with small  
464  $\alpha_s$  or  $\tau_{30}$ . However, the amount by which  $\mu$  needs to be reduced in order to shut off the MJO  
465 is not proportional to the amount by which  $\alpha_s$  needs to be reduced in order to achieve similar  
466 results. While this clearly demonstrates the importance of stratiform induced downdrafts  
467 for MJO simulation, as it is the case for the stratiform instability, it also suggests that this

468 is not the only mechanism that controls the scale selection of convective organization and  
469 other factors such as tilted heating may play a role. The dynamics of the MJO and organized  
470 convection in general is very complex and may not be tied to one single physical mechanism  
471 (i.e. one single model parameter) such as the tilted heating (Lappen and Schumacher 2014)  
472 or the spreading of cold pools in the boundary layer (Savarin et al. 2012; Feng et al. 2015).

473 This extreme sensitivity of the model simulations to stratiform heating and especially  
474 evaporation of stratiform rain raise the question about the universality of such parameters.  
475 In nature, the strength and importance of such processes is often dictated by the large  
476 scale conditions. While the amount of stratiform is clearly depending on the strength and  
477 abundance of deep convection, the dependence is not a simple linear relationship. The  
478 proportion of deep convection that is being delayed as stratiform rain is not linear nor simple.  
479 It highly depends on cloud microphysics, turbulent fluctuations in temperature and aerosol  
480 concentrations and possibly many other factors. Already, the SMC framework takes this  
481 notion of nonlinear dependence into account through the stochastic area-fraction. However,  
482 this dependence is not strongly tied to all the physical processes that presumably control  
483 the amount of stratiform heating and especially the actual evaporation rate of stratiform  
484 rain in the lower troposphere. In state-of-the-art GCMs stratiform rain is not parameterized  
485 but directly represented through grid scale condensation. While this solves the issues of  
486 parameter tuning it lacks the observed causality associated with deep convection and the  
487 effect of sub-grid variability of the stratiform rain formation and evaporation. The authors  
488 are currently working on more realistic ways of parameterizing stratiform heating fractions  
489 using the stochastic multicloud model framework applied to comprehensive bulk mass flux  
490 column-physics cumulus parameterizations (Tiedtke 1993; Zhang and McFarlane 1995).

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## 654 List of Tables

655	1	List of the default multcloud parameters for SMCM-HOMME. $\tilde{Q}_j$ in parentheses corresponding to a normalization with the $L_2$ norm of the basis function	
656		$\phi_j$ that enter in the projections of the horizontal velocity field.	29
657			
658	2	Transition rates and time scales in the stochastic parametrization.	30
659	3	List of the experiments with different stratiform heating strength.	31

TABLE 1. List of the default multcloud parameters for SMCM-HOMME.  $\tilde{Q}_j$  in parentheses corresponding to a normalization with the  $L_2$  norm of the basis function  $\phi_j$  that enter in the projections of the horizontal velocity field.

Parameter	Value	Description
$\tilde{Q}_1$	38.47 K	First baroclinic projection of the background moisture gradient in Eq.(2)
$\tilde{Q}_2$	38.35 K	Second baroclinic projection of the background moisture gradient in Eq.(2)
$Q_{R,1}^0$	1K/day	First baroclinic radiative cooling rate
$\bar{\theta}_{eb} - \bar{\theta}_{em}$	11.00K	Discrepancy between $\theta_{eb}$ and $\theta_{em}$ at RCE in Eq.(3)
$\bar{\theta}_{eb}^* - \bar{\theta}_{eb}$	10.00K	Discrepancy between saturation and actual $\theta_{eb}$ at RCE in Eq.(3)
$a_1/a_2$	0.1 / 0.9	Relative contribution of $\theta_{eb}/q$ to deep convection in (1)
$a_0$	0.5	Dry convective buoyancy frequency in deep and congestus heating in (1)
$\gamma_2/\gamma_2'$	0.25 / 0.6	Relative contribution of $\theta_2$ to deep/congestus heating in (1) and to $CAPE/CAPE_i$ in Table 2
$\mu$	0.2	Relative contribution of stratiform and congestus to downdrafts in Eq.(3)
$\alpha_c/\alpha_s$	0.25 / 0.5	Congestus/stratiform adjustment coefficient in (1)
$\tau_c/\tau_s$	1 hr / 3 hrs	Congestus/stratiform adjustment time scale in (1)
$\tau_{conv}$	2h	Convective time scale in (1)
$h$	500 m	Prescribed boundary layer height
$H$	16 km	Average height of the tropical troposphere
$m_0 = \frac{\bar{P} \cdot Q_{R,1}^0}{[Q_{R,1}^0 + \mu(\bar{H}_s - \bar{H}_c)] \cdot 1/(\bar{\theta}_{eb} - \bar{\theta}_{em}) \cdot H}$	0.00734 m sec <sup>-1</sup> (in EXP1)	Scale of downdraft mass flux, value set by RCE solution
$\tau_e = \frac{(\bar{\theta}_{eb}^* - \bar{\theta}_{eb}) \cdot h}{(\bar{P} \cdot H)}$	14.8 hrs (in EXP1)	Evaporation time scale, value set by RCE solution
$\tilde{\alpha}$	0.1	Coefficient of second baroclinic velocity component in moisture equation
$R$	320 J/kg K <sup>-1</sup>	CAPE constant in Table 2
$\gamma$	1.7	Contribution of $\theta_1$ to CAPE anomalies in Table 2
$T_0$	30 K	Scaling factor of dryness in Table 2
$CAPE_0$	400 J/kg	Scaling factor of CAPE in Table 2
$n \times n$	1600	Number of lattice sites within each CGM grid box

TABLE 2. Transition rates and time scales in the stochastic parametrization.

Transition	Transition Rate	Time scale (h)
Formation of congestus	$R_{01} = \frac{1}{\tau_{01}}\Gamma(C_l)\Gamma(D)$	$\tau_{01} = 40\tau_{grid}$
Decay of congestus	$R_{10} = \frac{1}{\tau_{10}}\Gamma(D)$	$\tau_{10} = 1\tau_{grid}$
Conversion of congestus to deep	$R_{12} = \frac{1}{\tau_{12}}\Gamma(C)[1 - \Gamma(D)]$	$\tau_{12} = 1\tau_{grid}$
Formation of deep	$R_{02} = \frac{1}{\tau_{02}}\Gamma(C)[1 - \Gamma(D)]$	$\tau_{02} = 4\tau_{grid}$
Conversion of deep to stratiform	$R_{23} = \frac{1}{\tau_{23}}$	$\tau_{23} = 3\tau_{grid}$
Decay of deep	$R_{20} = \frac{1}{\tau_{20}}[1 - \Gamma(C)]$	$\tau_{20} = 3\tau_{grid}$
Decay of stratiform	$R_{30} = \frac{1}{\tau_{30}}$	$\tau_{30} = 2 \text{ or } 5 \text{ or } 10\tau_{grid}$

$$\Gamma(x) = \begin{cases} 1 - \exp(-x), & \text{if } x > 0; \\ 0, & \text{otherwise.} \end{cases}$$

$$D = (\theta_{eb} - \theta_{em})/T_0$$

$$CAPE_l = \overline{CAPE} + R[\theta_{eb} - \gamma(\theta_1 + \gamma'_2\theta_2)], \quad C_l = CAPE_l/CAPE_0$$

$$CAPE = \overline{CAPE} + R[\theta_{eb} - \gamma(\theta_1 + \gamma_2\theta_2)], \quad C = CAPE/CAPE_0$$

TABLE 3. List of the experiments with different stratiform heating strength.

Experiment	Stratiform heating coefficient ( $\alpha_s$ )	Stratiform decay time scale ( $\tau_{30}$ )	Other changes
EXP1	0.50	$5\tau_{grid}$	
EXP2	0.25	$5\tau_{grid}$	
EXP3	0.25	$10\tau_{grid}$	
EXP4	0.50	$2\tau_{grid}$	
EXP5	0.50	$5\tau_{grid}$	$\mu = 0.1$
EXP6	0.50	$5\tau_{grid}$	$\mu = 0.05$
EXP7	0.50	$5\tau_{grid}$	$\mu = 0.01$
EXP8	0.50	$5\tau_{grid}$	$\tau_{01} = 1\tau_{grid}, \tau_{02} = 3\tau_{grid}$



## 660 List of Figures

661	1	Warm pool structure.	34
662	2	Hovmöller diagram of meridionally averaged ( $10^{\circ}\text{S}$ - $10^{\circ}\text{N}$ ) zonal wind at (a)	
663		850hPa and (b) 200 hPa in the standard parameter regime with $\alpha_s = 0.50$	
664		and $\tau_{30} = 5\tau_{grid}$ (EXP1). The black dashed line marks an MJO-like event	
665		moving eastward at roughly $5 \text{ m s}^{-1}$ .	35
666	3	Same as Figure 2 but for (a) deep convective, (b) congestus, and (c) stratiform	
667		heating rates and (d) vertically averaged moisture anomaly.	36
668	4	Spectral power of the meridionally averaged (a) 800 hPa and (b) 200 hPa	
669		zonal wind, (c, d, e) convective heating rates and (f) moisture anomalies	
670		corresponding in Figure 2 and 3.	37
671	5	Time series of the cloud area fractions (blue) and heating rates (red) averaged	
672		between $10^{\circ}\text{S}$ and $10^{\circ}\text{N}$ at $150^{\circ}$ longitude for EXP1.	38
673	6	Same as Figure 2 but with $\alpha_s = 0.25$ and $\tau_{30} = 5\tau_{grid}$ (EXP2). The black	
674		dashed line marks an eastward wavespeed about $10.3 \text{ m s}^{-1}$ .	39
675	7	Same as Figure 6 but for (a) deep, (b) congestus, and (c) stratiform heating	
676		rates and (d) moisture.	40
677	8	Same as Figure 4 but for EXP2.	41
678	9	Horizontal (a, b, c, d) and vertical (e, f) structures of convectively coupled	
679		waves from EXP2. The composite is obtained by first filtering in Fourier space	
680		using the window highlighted in Figure 8 and averaging the filtered data in	
681		time between day 1860 and day 1870 in the frame moving at $10.3 \text{ m s}^{-1}$ .	42
682	10	Same as Figure 2 but with $\alpha_s = 0.25$ and $\tau_{30} = 10\tau_{grid}$ (EXP3).	43
683	11	Same as Figure 3 but with $\alpha_s = 0.25$ and $\tau_{30} = 10\tau_{grid}$ (EXP3).	44
684	12	Spectral power diagrams for EXP3: $\alpha_s = 0.25$ and $\tau_{30} = 10\tau_{grid}$ .	45
685	13	Time auto-correlation functions of moisture (blue) and precipitation (green)	
686		for (a) EXP1, (b) EXP2, (c) EXP3 and (d) EXP4.	46

687	14	Same as Figure 13 but for distribution of precipitation events.	47
688	15	Hovmöller diagrams of deep convective (left) and congestus (right) heating	
689		rates for EXP5 (a,b), 6 (c,d) and 7 (e,f): $\alpha_s = 0.50$ , $\tau_{30} = 5\tau_{grid}$ and $\mu =$	
690		$0.1, 0.05, 0.01$ for respectively.	48
691	16	Hovmöller diagram of (a, b, c) heating rates and (d) moisture for the case	
692		with DKM15 parameters: $\alpha_s = 0.50$ , $\tau_{30} = 5\tau_{grid}$ , $\tau_{01} = 1\tau_{grid}$ and $\tau_{02} = 3\tau_{grid}$	
693		(EXP8).	49

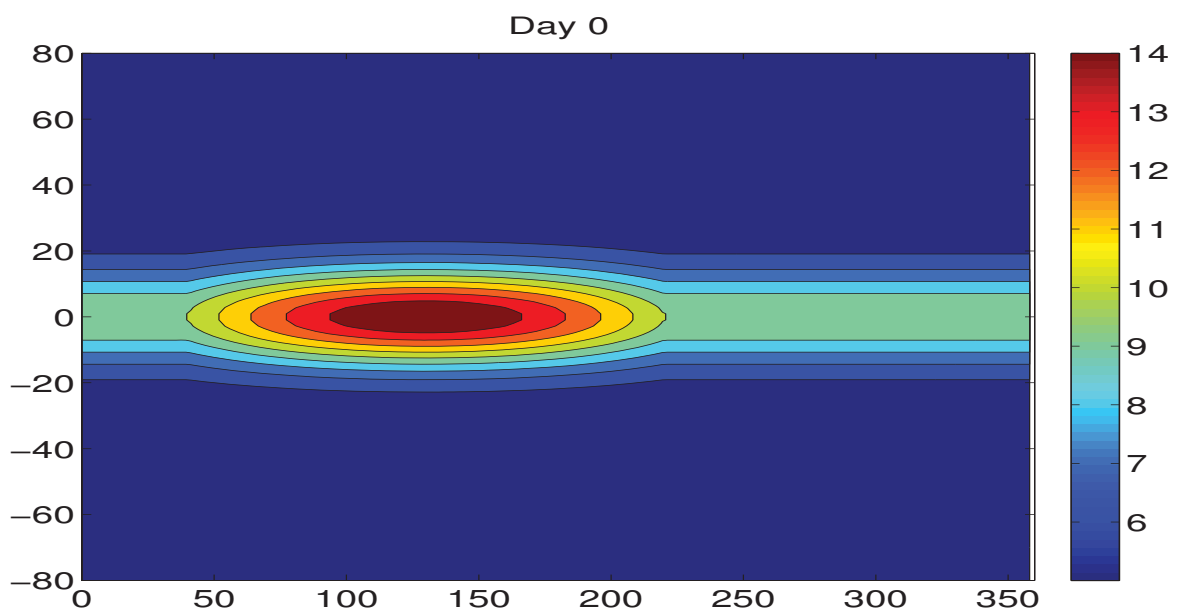


FIG. 1. Warm pool structure.

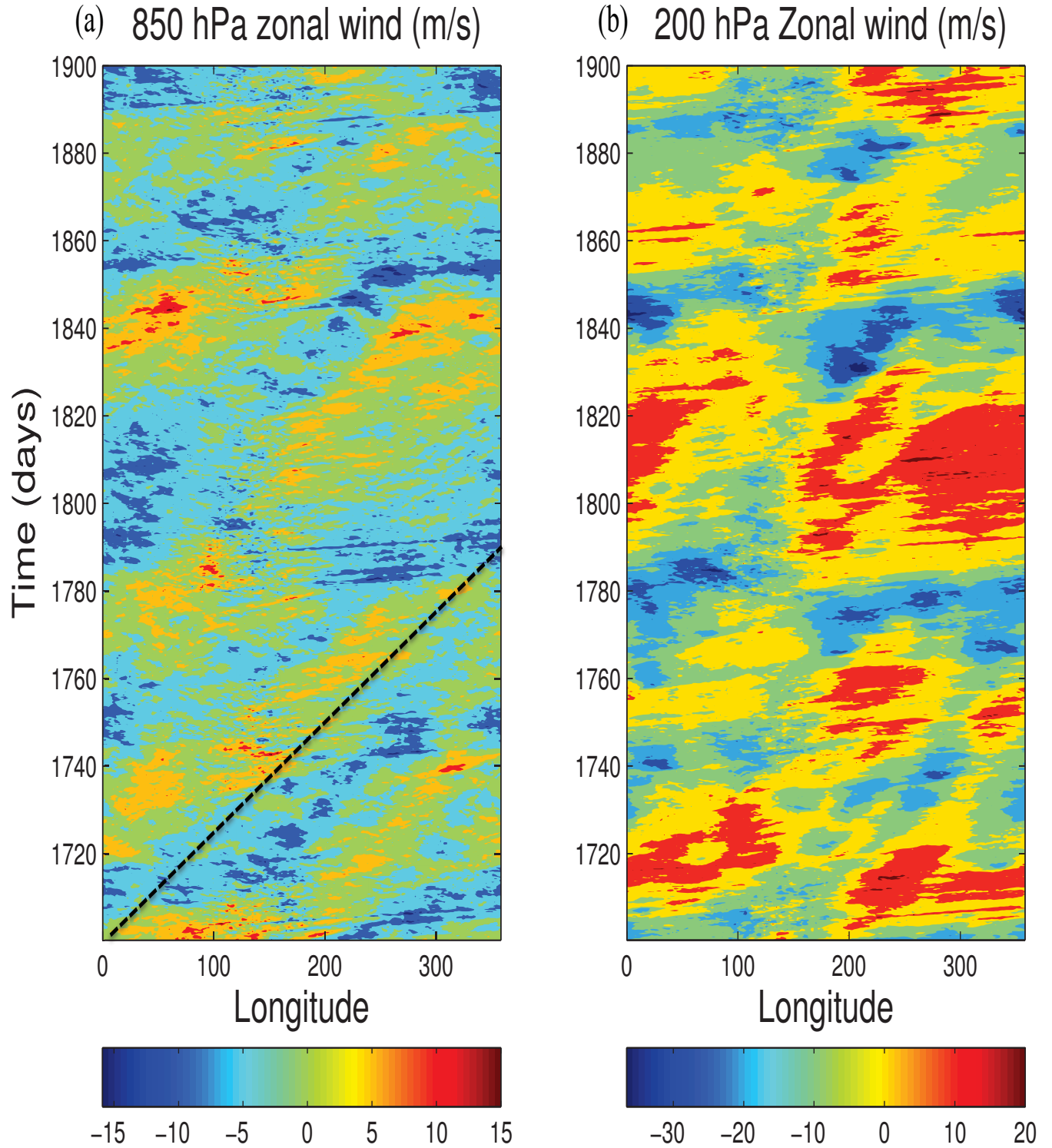


FIG. 2. Hovmöller diagram of meridionally averaged ( $10^{\circ}\text{S}$ - $10^{\circ}\text{N}$ ) zonal wind at (a) 850hPa and (b) 200 hPa in the standard parameter regime with  $\alpha_s = 0.50$  and  $\tau_{30} = 5\tau_{grid}$  (EXP1). The black dashed line marks an MJO-like event moving eastward at roughly  $5 \text{ m s}^{-1}$ .

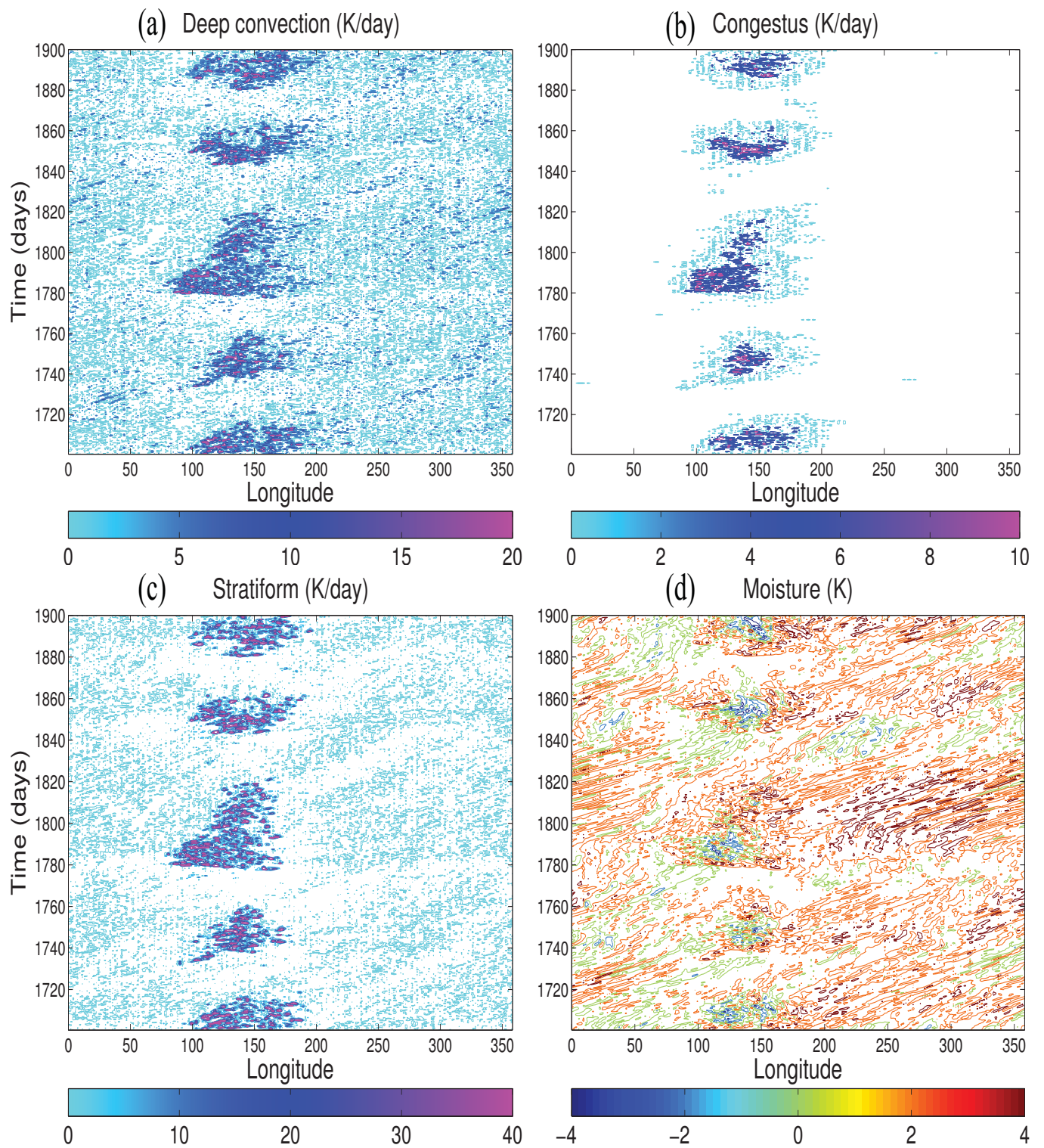


FIG. 3. Same as Figure 2 but for (a) deep convective, (b) congestus, and (c) stratiform heating rates and (d) vertically averaged moisture anomaly.

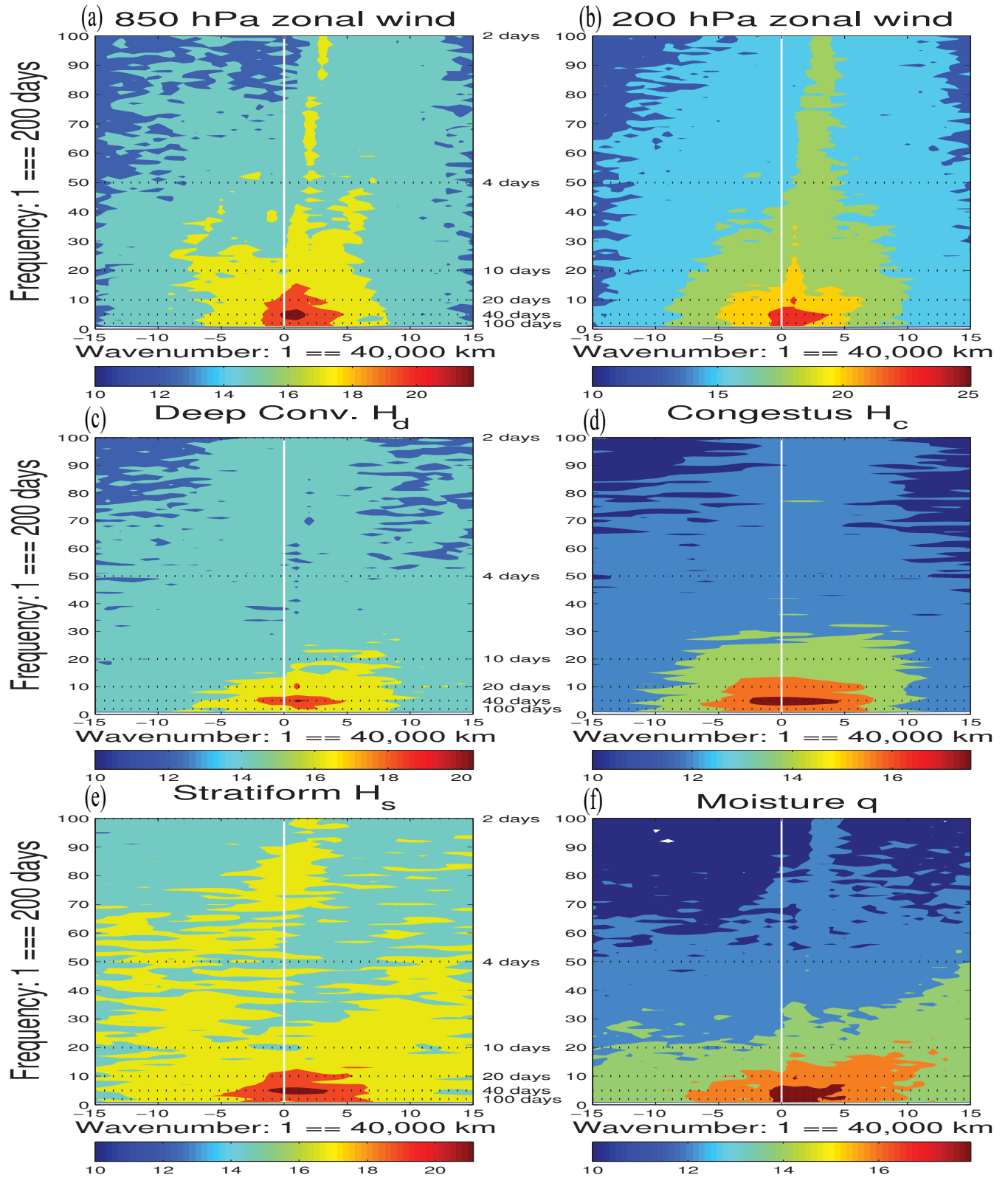


FIG. 4. Spectral power of the meridionally averaged (a) 800 hPa and (b) 200 hPa zonal wind, (c, d, e) convective heating rates and (f) moisture anomalies corresponding in Figure 2 and 3.

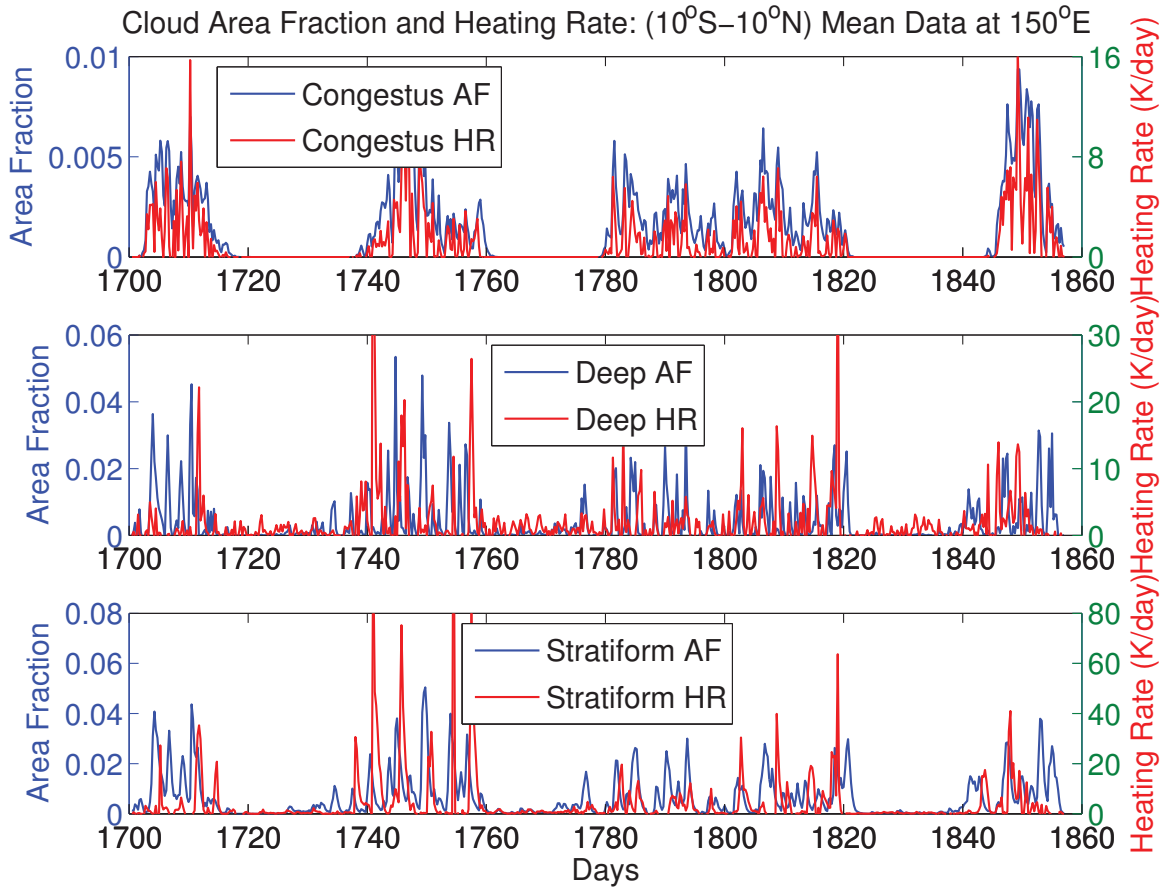


FIG. 5. Time series of the cloud area fractions (blue) and heating rates (red) averaged between  $10^{\circ}\text{S}$  and  $10^{\circ}\text{N}$  at  $150^{\circ}$  longitude for EXP1.

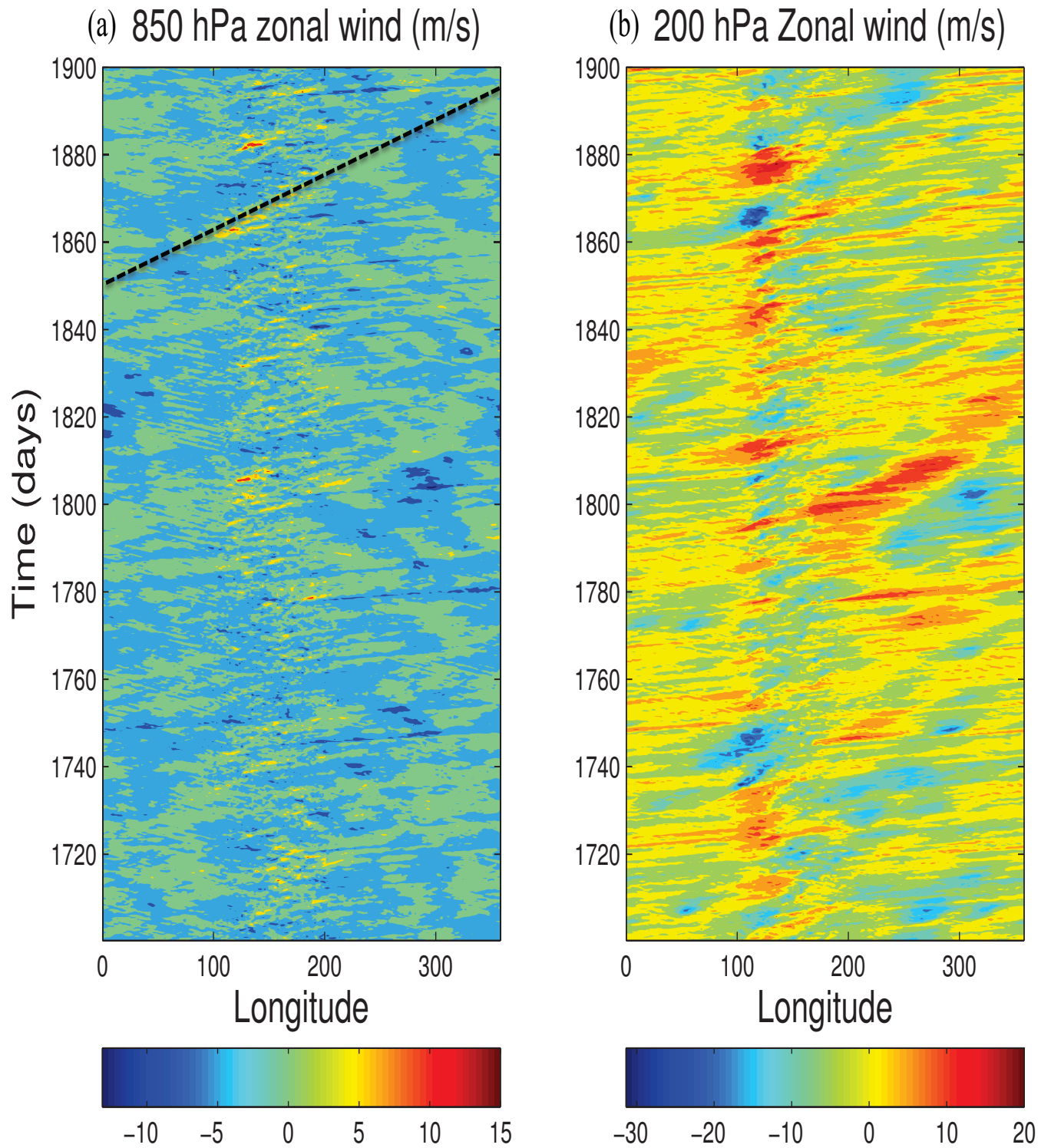


FIG. 6. Same as Figure 2 but with  $\alpha_s = 0.25$  and  $\tau_{30} = 5\tau_{grid}$  (EXP2). The black dashed line marks an eastward wavespeed about  $10.3 \text{ m s}^{-1}$ .



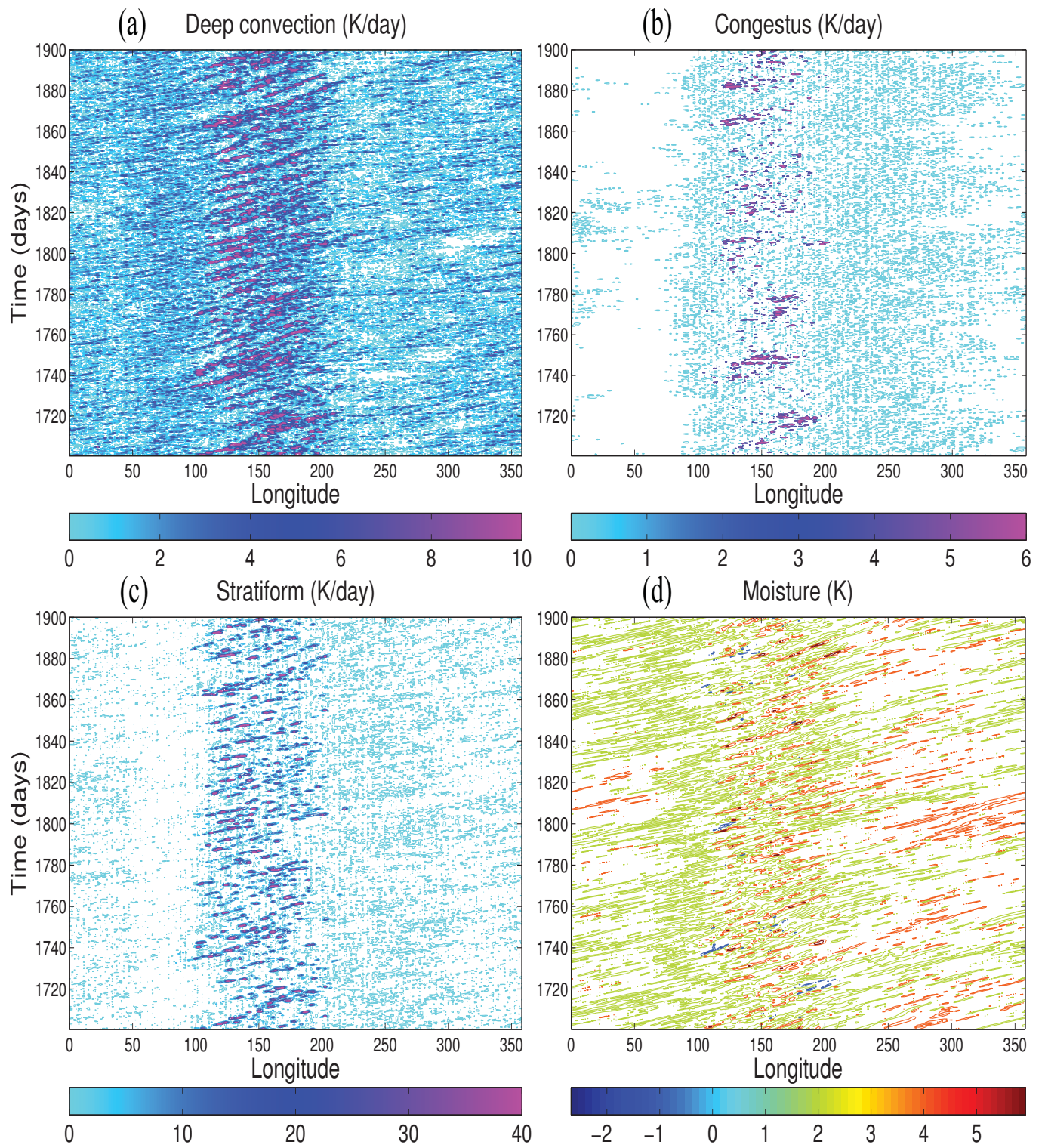


FIG. 7. Same as Figure 6 but for (a) deep, (b) congestus, and (c) stratiform heating rates and (d) moisture.

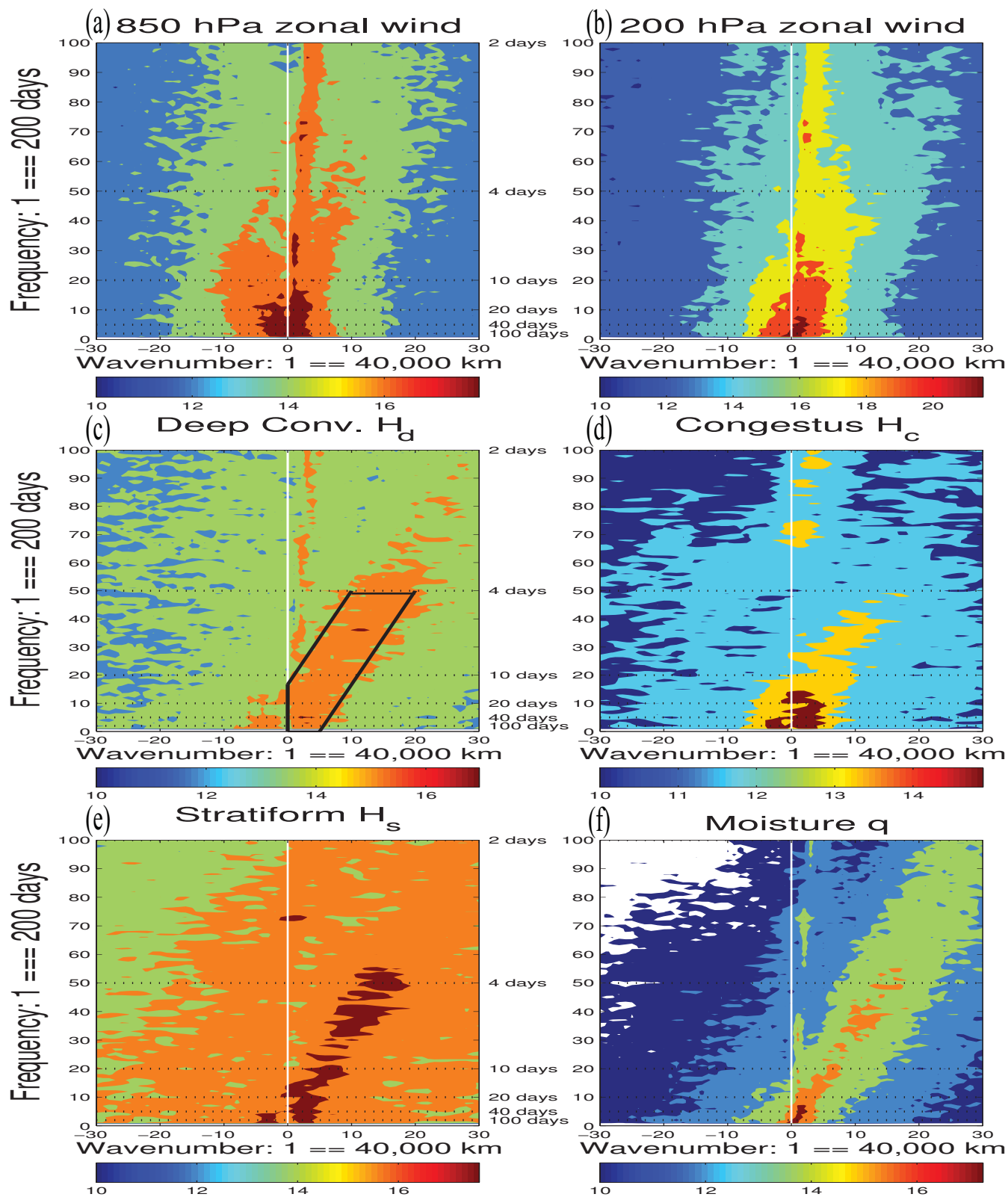


FIG. 8. Same as Figure 4 but for EXP2.

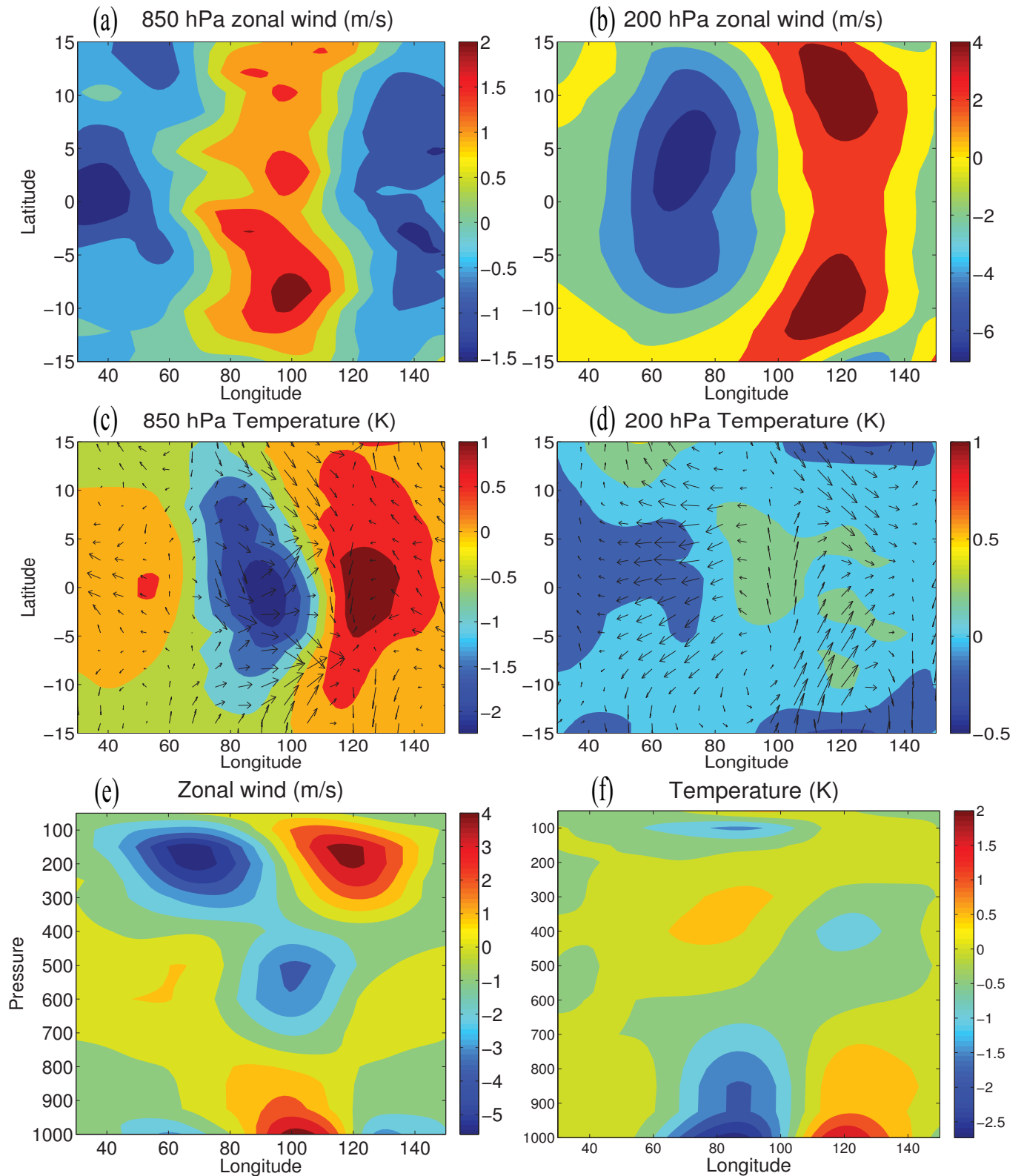


FIG. 9. Horizontal (a, b, c, d) and vertical (e, f) structures of convectively coupled waves from EXP2. The composite is obtained by first filtering in Fourier space using the window highlighted in Figure 8 and averaging the filtered data in time between day 1860 and day 1870 in the frame moving at  $10.3 \text{ m s}^{-1}$ .

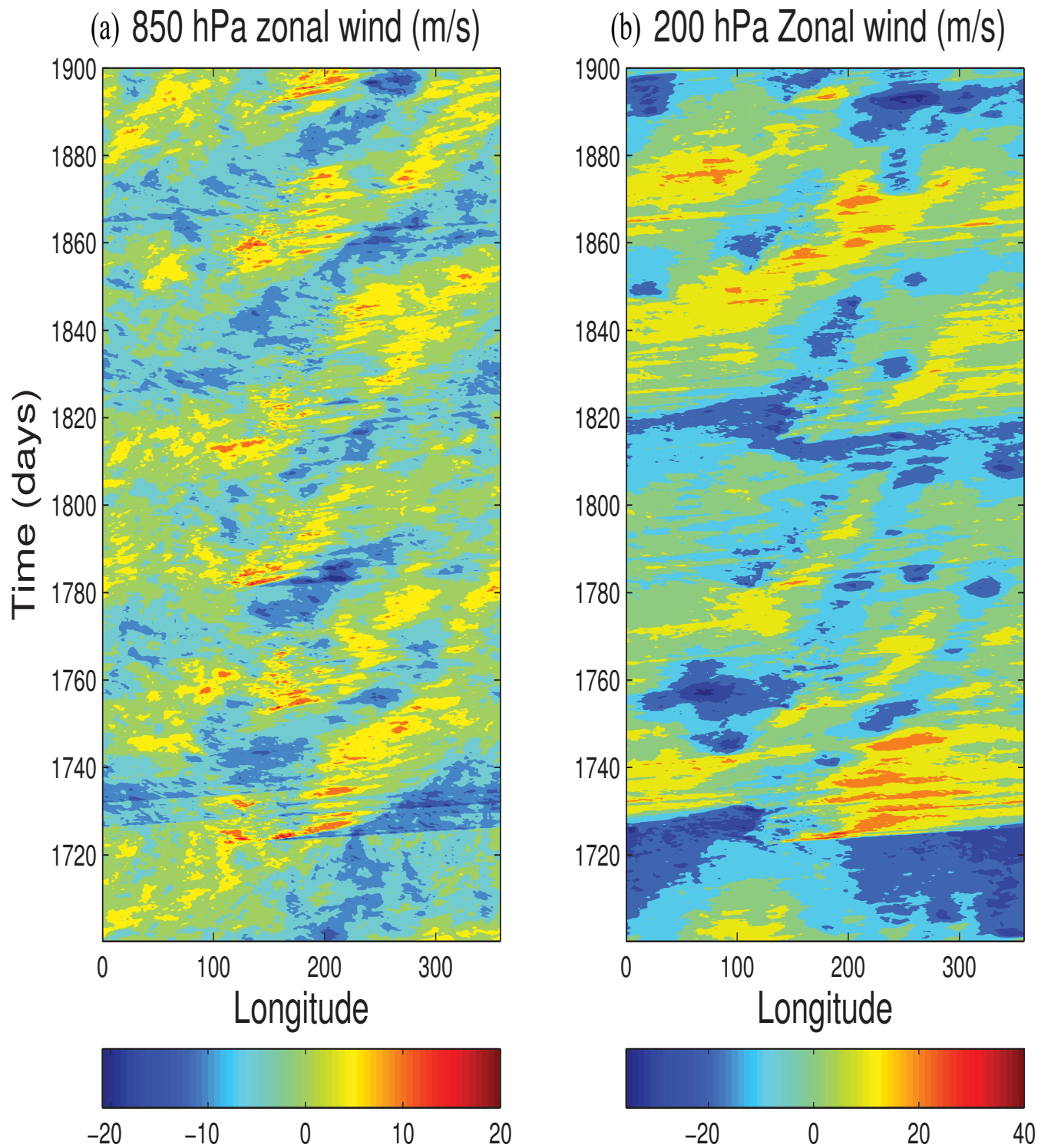


FIG. 10. Same as Figure 2 but with  $\alpha_s = 0.25$  and  $\tau_{30} = 10\tau_{grid}$  (EXP3).

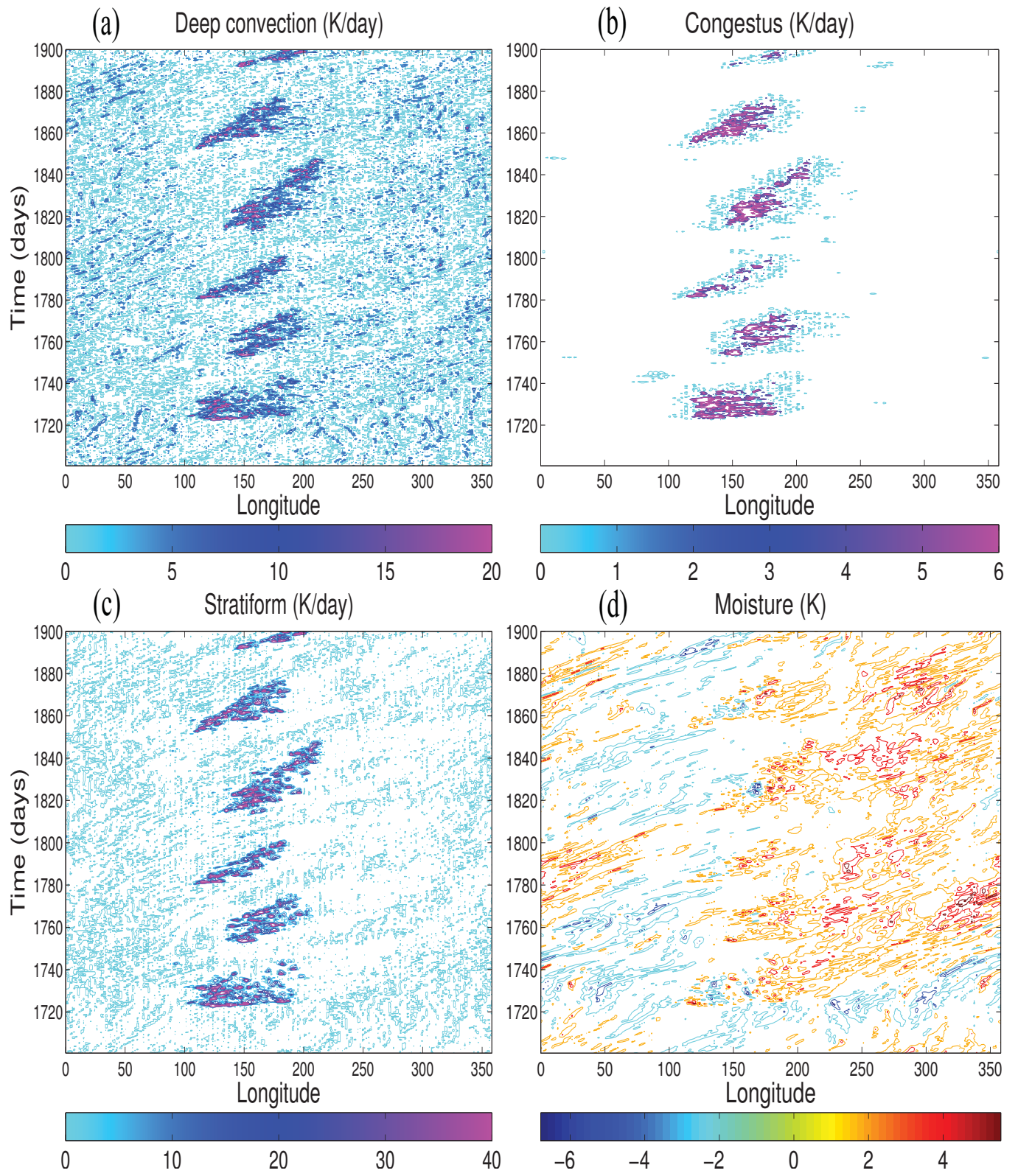


FIG. 11. Same as Figure 3 but with  $\alpha_s = 0.25$  and  $\tau_{30} = 10\tau_{grid}$  (EXP3).

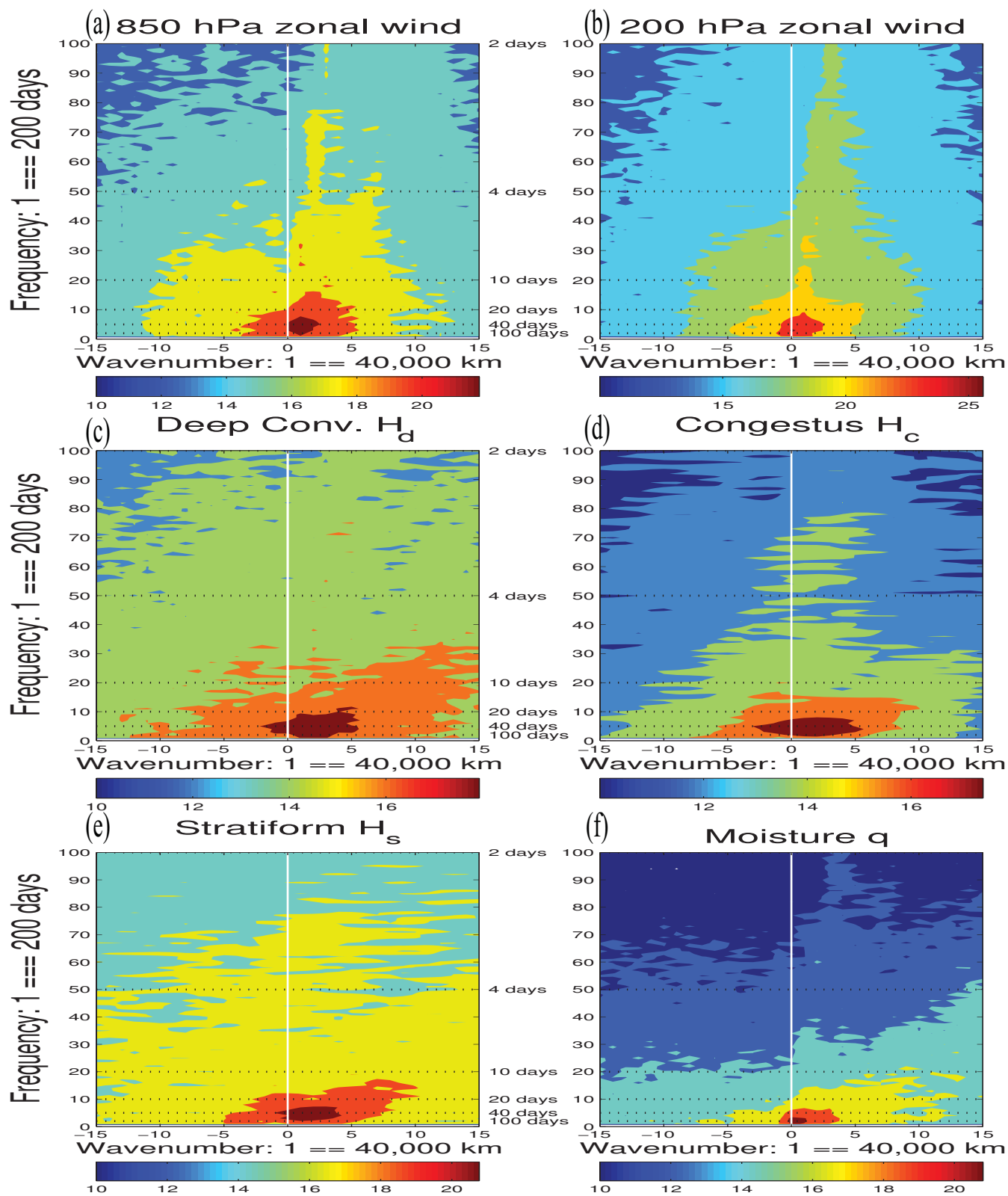


FIG. 12. Spectral power diagrams for EXP3:  $\alpha_s = 0.25$  and  $\tau_{30} = 10\tau_{grid}$ .

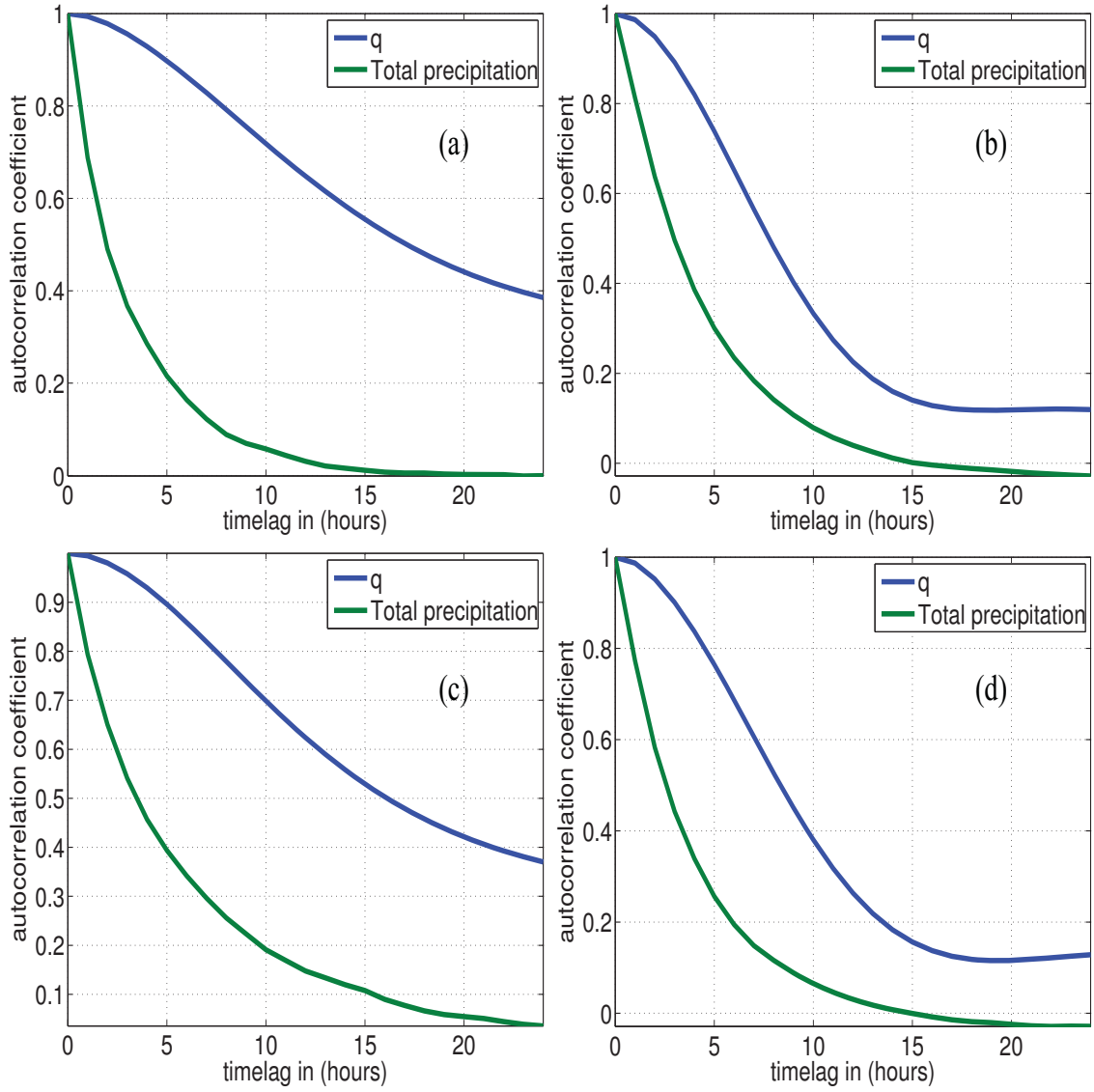


FIG. 13. Time auto-correlation functions of moisture (blue) and precipitation (green) for (a) EXP1, (b) EXP2, (c) EXP3 and (d) EXP4.

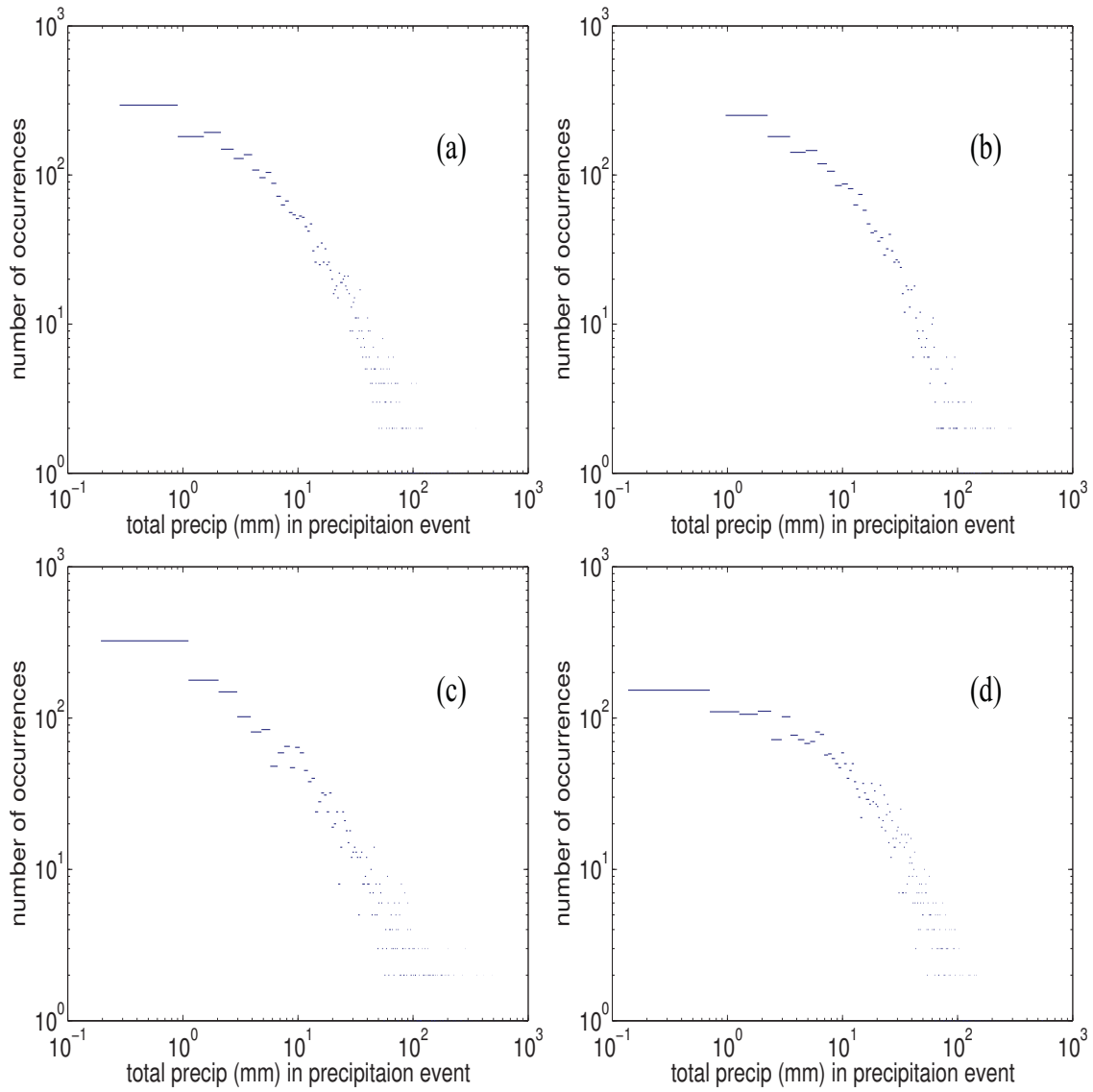


FIG. 14. Same as Figure 13 but for distribution of precipitation events.



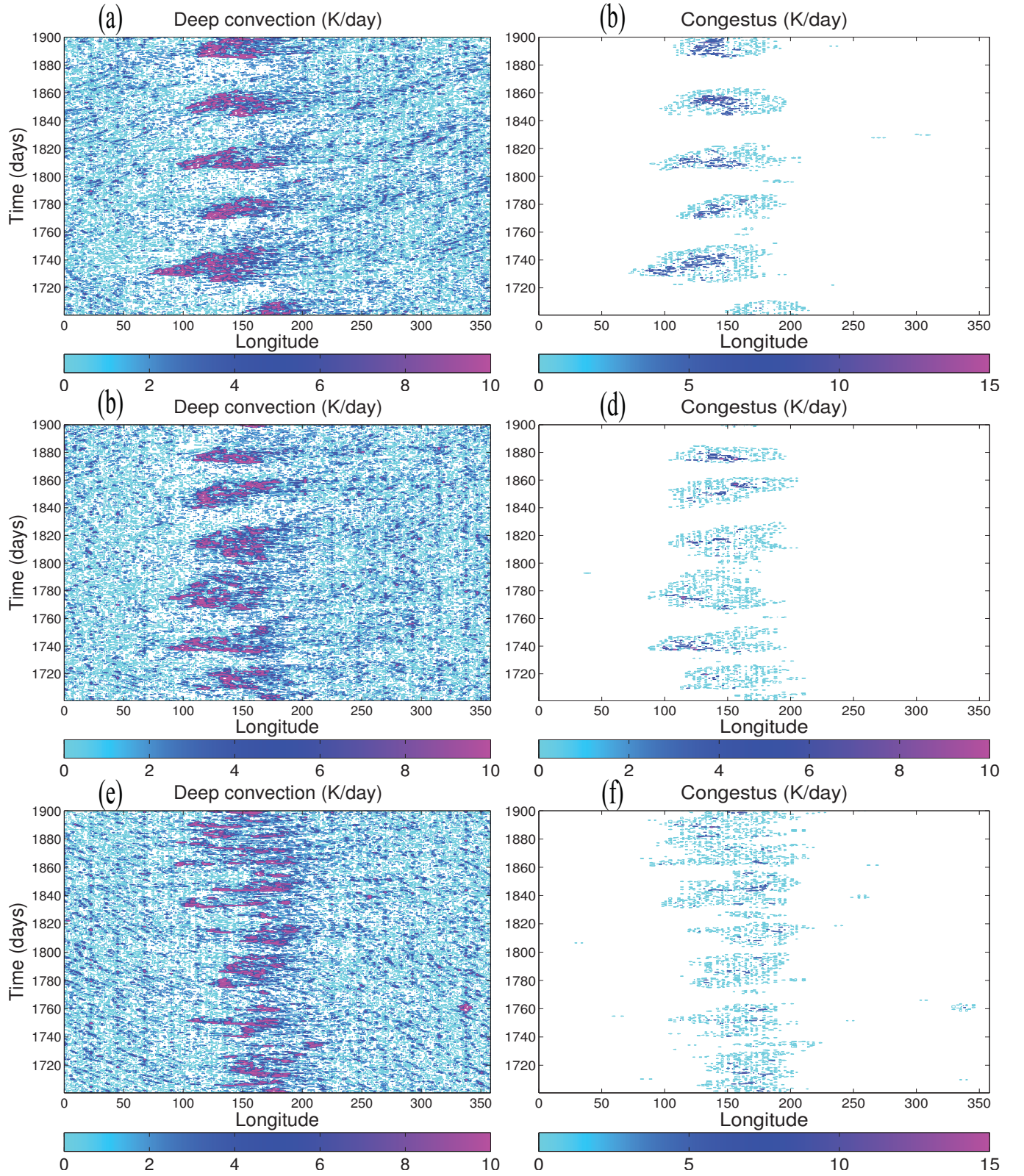


FIG. 15. Hovmöller diagrams of deep convective (left) and congestus (right) heating rates for EXP5 (a,b), 6 (c,d) and 7 (e,f):  $\alpha_s = 0.50$ ,  $\tau_{30} = 5\tau_{grid}$  and  $\mu = 0.1, 0.05, 0.01$  for respectively.

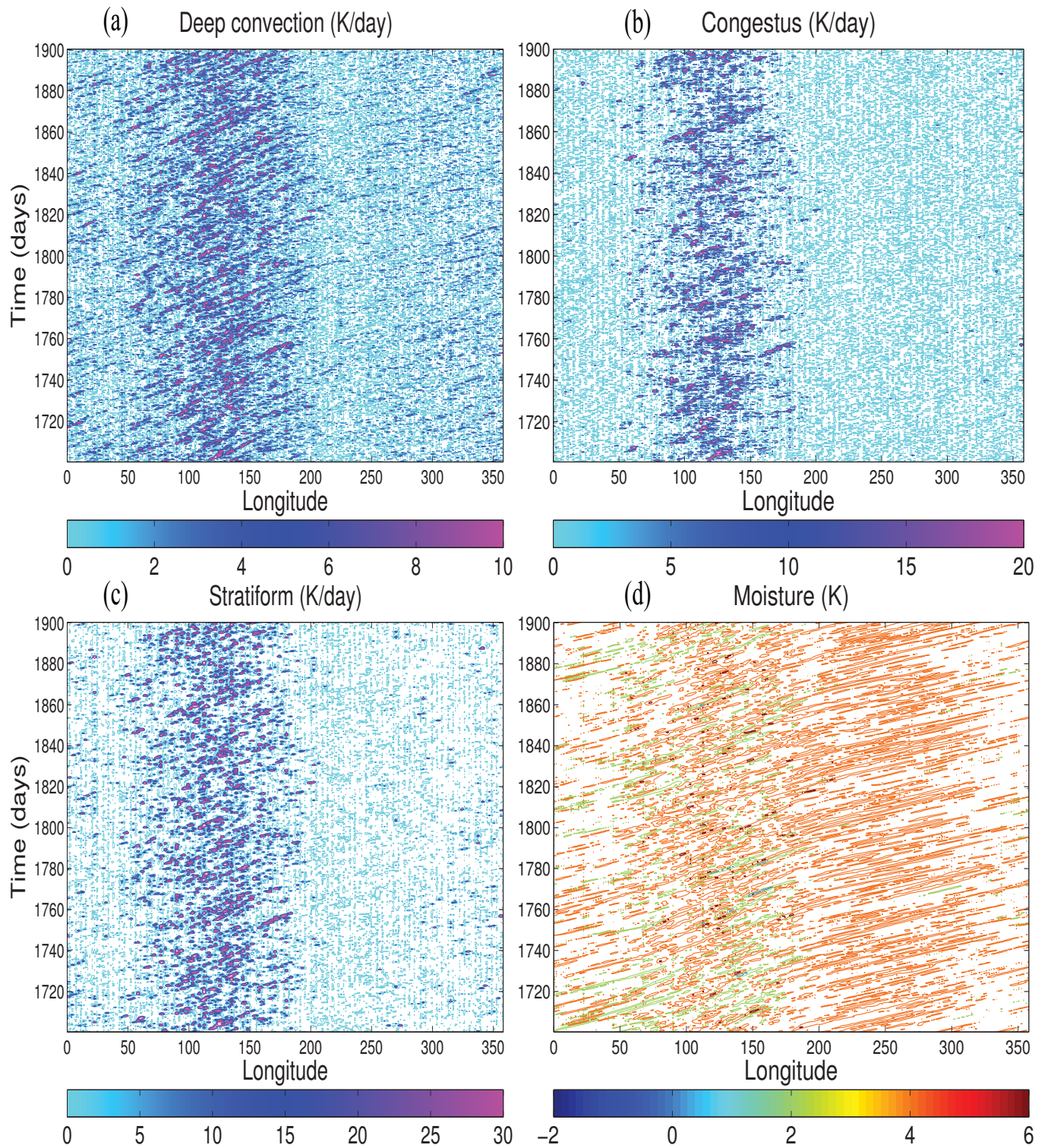


FIG. 16. Hovmöller diagram of (a, b, c) heating rates and (d) moisture for the case with DKM15 parameters:  $\alpha_s = 0.50$ ,  $\tau_{30} = 5\tau_{grid}$ ,  $\tau_{01} = 1\tau_{grid}$  and  $\tau_{02} = 3\tau_{grid}$  (EXP8).