

1 **Upscale Impact of Mesoscale Convective Systems and its Parameterization**  
2 **in an Idealized GCM for a MJO Analog above the Equator**

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## ABSTRACT

16 The Madden-Julian oscillation (MJO) typically contains several superclus-  
17 ters and numerous embedded mesoscale convective systems (MCSs). It is hy-  
18 pothesized here that the poorly simulated MJOs in current coarse resolution  
19 global climate models (GCMs) is related to the inadequate treatment of unre-  
20 solved MCSs. So its parameterization should provide the missing collective  
21 effects of MCSs. However, a satisfactory understanding of the upscale impact  
22 of MCSs on the MJO is still lacking. A simple two-dimensional multicloud  
23 model is used as an idealized GCM with clear deficiencies. Eddy transfer of  
24 momentum and temperature by the MCSs, predicted by the mesoscale equato-  
25 rial synoptic dynamics (MESD) model, is added to this idealized GCM. The  
26 upscale impact of westward-moving MCSs promotes eastward propagation  
27 of the MJO analog, consistent with the theoretical prediction of the MESD  
28 model. Furthermore, the upscale impact of upshear-moving MCSs signifi-  
29 cantly intensifies the westerly wind burst, due to two-way feedback between  
30 easterly vertical shear and eddy momentum transfer with low-level eastward  
31 momentum forcing. Finally, a basic parameterization of upscale impact of  
32 upshear-moving MCSs modulated by deep heating excess and vertical shear  
33 strength is provided as a new parameterization. This significantly improves  
34 key features of the MJO analog in the idealized GCM with clear deficiencies.  
35 A three-way interaction mechanism between the MJO analog, parameterized  
36 upscale impact of MCSs and background vertical shear is identified.

## 37 **1. Introduction**

38 The MJO is the dominant component of tropical intraseasonal variability (Zhang 2005) and dra-  
39 matically impacts local weather through extreme rainfall and mid-latitude atmospheric conditions  
40 by tropical-extratropical teleconnection (Zhang 2013; Stan et al. 2017; Henderson et al. 2017).  
41 Tropical convection associated with the MJO is hierarchically organized across multiple spatial  
42 and temporal scales. The MJO typically contains multiple eastward- and westward-moving su-  
43 perclusters of cloudiness (Nakazawa 1988; Chen et al. 1996) with numerous embedded MCSs  
44 (Houze 2004) and cumulus clouds on smaller scales. As the major rainfall producer in the tropics,  
45 MCSs contribute up to 50% of the rainfall in most tropical regions (Tao and Moncrieff 2009).  
46 Although the effects of large-scale atmospheric conditions on the modulation of MCSs have been  
47 well documented in observations (Lin and Johnson 1996; Chen et al. 1996; LeMone et al. 1998),  
48 a satisfactory understanding of the collective effects of MCSs on the momentum and heat budgets  
49 of the MJO is still lacking.

50 It is hypothesized that the poorly simulated MJOs in current coarse resolution GCMs are related  
51 to the inadequate treatment of MCSs and their upscale impact. The essential difference between  
52 MCSs and smaller individual convective towers lies in the fact that the former typically have  
53 front-to-rear tilted organized structures, while the latter are unorganized (Moncrieff and Klinker  
54 1997). Typical behavior of the poorly simulated MJOs in the GCMs includes impersistent eastward  
55 propagation, unrealistic planetary/intraseasonal variability in precipitation and winds, and upright  
56 vertical structure with a negligible westerly wind burst (WWB) (Jiang et al. 2015). In contrast,  
57 global cloud-resolving simulations that resolve MCSs successfully capture some key features of  
58 the MJOs (Grabowski 2003; Miura et al. 2007), and motivated the development of the superparam-  
59 eterization method based on two-dimensional cloud resolving models (CRMs) (Grabowski 2001,

60 2004; Randall et al. 2003; Majda 2007a) and a sparse space-time technique (Xing et al. 2009).  
61 Nevertheless, the computational cost to explicitly resolve MCSs is too expensive to be practical  
62 in long GCM simulations. An alternative way to address this issue is to develop new parameter-  
63 izations for coarse-resolution GCMs that capture the upscale impact of unresolved MCSs on the  
64 MJO.

65 Several studies have assessed the upscale impact of MCSs based on observational measurement,  
66 reanalysis dataset and cloud-resolving simulations, most of which focus on convective momen-  
67 tum transfer (CMT) (Moncrieff 1981; LeMone 1983; Moncrieff 1992; LeMone and Moncrieff  
68 1994). Convective-scale CMT by unorganized convection normally has frictional effects that re-  
69 duce large-scale vertical shear (Zhang and McFarlane 1995). In contrast, mesoscale CMT by  
70 organized convection over hundred kilometers in horizontal scale can have countergradient mo-  
71 mentum transport that enhances the large-scale vertical shear (Moncrieff 1981, 1992). Tung and  
72 Yanai (2002a) concluded that CMT is, on the average, downgradient over the western Pacific  
73 warm pool but upgradient during the westerly wind phase of the MJO (Tung and Yanai 2002b).  
74 Oh et al. (2015) found that the subgrid-scale and mesoscale CMT associated with the MJO has  
75 a distinctive three-layer vertical structure. Grabowski and Moncrieff (2001) demonstrated that  
76 CMT from westward-moving MCSs embedded in the eastward-moving convective envelope pro-  
77 motes the large-scale organization of convection. Inspired by multi-scale organization and the  
78 observed statistical self-similarity of tropical convection, Majda (2007b) systematically derived  
79 multi-scale asymptotic models that describe scale-interactions among clusters, superclusters and  
80 intraseasonal oscillations and highlight the crucial role of eddy transfer of momentum and tem-  
81 perature. Brenowitz et al. (2018) concluded that mesoscale CMT dominates the total vertical flux  
82 feedback on planetary-scale kinetic energy budget, providing new mechanisms for the planetary-  
83 scale organization of convection.

84 From a theoretical perspective, several modeling studies have sought to better understand the  
85 upscale impact of MCSs on the large-scale organization of tropical convection. Majda and Stech-  
86 mann (2009) utilized a simple dynamic model with features of CMT from convectively coupled  
87 gravity waves and their interactions with large-scale mean flow. Khouider et al. (2012) demon-  
88 strated that in the active region of the MJO with WWB, CMT from both convectively coupled  
89 Kelvin waves (CCKWs) and MCSs plays a significant role in accelerating the low-level westerly  
90 winds. The three-dimensional mesoscale equatorial synoptic dynamic (MESD) model, originally  
91 derived by Majda (2007b), was used as a multi-scale framework to assess the upscale impact of  
92 MCSs on eastward-moving CCKWs (Yang and Majda 2018b) and westward-moving 2-day waves  
93 (Yang and Majda 2018a). Explicit expressions for eddy transfer of momentum and temperature  
94 obtained from the MESD model are an essential basis for the parameterization of upscale impact of  
95 MCSs provided here. Moncrieff et al. (2017) introduced the multi-scale coherent structure param-  
96 eterization (MCSP) that achieved significant improvement in tropical precipitation patterns and  
97 precipitation variability in a GCM. In general, idealized models that simulate some key features  
98 of the MJO can serve as a useful testbed. Here we refer to these MJO-like events arising from the  
99 idealized models as the MJO analog.

100 The goals of this paper include the following three aspects: first, use a simple multicloud model  
101 for the MJO analog and intraseasonal variability above the equator to mimic the typical behav-  
102 ior of GCMs with clear deficiencies. Secondly, assess the upscale impact of MCSs on key fea-  
103 tures of the MJO analog, including persistent propagation of a two-scale structure, realistic plane-  
104 tary/intraseasonal variability in precipitation and winds, and a significant WWB. Thirdly, introduce  
105 a basic parameterization of upscale impact of MCSs and test its effects in the idealized GCM to  
106 address deficiencies.

107 In general, the multicloud models represent three dominant cloud types (congestus, deep, strat-  
108 iform) by using the first- and second-baroclinic vertical modes and build the life-cycle of these  
109 cloud types into the convective heating closure through a switch function for mid-latitude dryness  
110 (Khouider and Majda 2006c, 2007, 2006a). The deterministic version of the multicloud mod-  
111 els successfully captures characteristic features of CCEWs (Khouider and Majda 2008b, 2006b,  
112 2008a) and the diurnal cycle (Frenkel et al. 2011a,b, 2013). The stochastic version captures the  
113 MJO (Khouider et al. 2010; Deng et al. 2015; Goswami et al. 2017) when coupled to the GCM.  
114 In this paper, we use a deterministic two-dimensional multicloud model for the MJO analog and  
115 intraseasonal variability above the equator (Majda et al. 2007; Harlim and Majda 2013). By re-  
116 ducing the magnitude of both congestus and stratiform heating, this model mimics the typical  
117 behavior of GCMs with clear deficiencies, where both convection types are underestimated (Seo  
118 and Wang 2010; Del Genio et al. 2012; Lappen and Schumacher 2012; Del Genio et al. 2015). In  
119 order to introduce the upscale impact of MCSs, we use explicit expressions for the eddy transfer of  
120 momentum and temperature theoretically predicted by the MESD model (Yang and Majda 2018b).

121 The upscale impact of MCSs on the MJO analog is assessed through comparison experiments  
122 with/without adding extra eddy transfer of momentum and temperature. The modulation effects  
123 of deep heating excess on eddy transfer of momentum and temperature are considered in order to  
124 mimic the scenario that MCSs are prominent in the active convection region of the MJO (Khouider  
125 et al. 2012). The results show that the upscale impact of westward-moving MCSs promotes the  
126 eastward propagation of the MJO analog, consistent with the theoretical prediction by the MESD  
127 model (Yang and Majda 2018b). The modulation effects of vertical shear are considered to mimic  
128 the observation that MCSs typically move towards the convection center (Lin and Johnson 1996;  
129 Chen et al. 1996; Moncrieff and Klinker 1997; Yanai et al. 2000; Houze Jr et al. 2000). The re-  
130 sults show that the upscale impact of upshear-moving MCSs leads to a significant WWB in the

131 middle and west of the MJO analog, due to the positive feedback between large-scale easterly ver-  
132 tical shear and embedded eddy momentum transfer with low-level eastward momentum forcing.  
133 Finally, we provide a basic parameterization of upscale impact of upshear-moving MCSs, where  
134 modulation effects of deep heating effects and vertical shear strength are linearly combined. Sig-  
135 nificant improvement is achieved by adding this parameterization to the idealized GCM that has  
136 clear deficiencies. A further simulation illustrates a three-way interaction mechanism between the  
137 MJO analog, parameterization of upscale impact of MCSs and background mean flow over a long  
138 time scale. Specifically, the resulting oscillatory background mean flow resembles the QBO-like  
139 oscillation identified in cloud resolving simulations (Held et al. 1993; Nishimoto et al. 2016) and  
140 simplified GCMs (Horinouchi and Yoden 1998).

141 The results of this paper are presented as follows. Section 2 summarizes the governing equations  
142 and properties of the two-dimensional multicloud model, including the realistic MJO analog above  
143 the equator and the idealized GCM that has clear deficiencies. Section 3 discusses the effects of  
144 eddy transfer of momentum and temperature from MCSs on the MJO analog. Section 4 provides  
145 a basic parameterization of upscale impact of upshear-moving MCSs under the modulating effects  
146 of deep heating excess and vertical shear strength, and tests its effects in the idealized GCM that  
147 has clear deficiencies. The paper concludes with discussion in Section 5.

## 148 **2. An Idealized GCM for a MJO Analog and Intraseasonal Variability above the Equator**

149 In this section, we briefly review the equations governing the multicloud model and the con-  
150 vective heating closure. The simple two-dimensional multicloud model used here (Majda et al.  
151 2007; Harlim and Majda 2013) captures the MJO analog and intraseasonal variability above the  
152 equator. The goals of this section are to reproduce: i) a realistic MJO analog above the equator as

153 a proxy for the observations, and ii) a simulation with reduced congestus and stratiform heating as  
 154 an idealized GCM having clear deficiencies.

155 *a. Governing equations and multicloud model parameterization*

156 The multicloud models describe the life-cycle of three main cloud types (congestus, deep and  
 157 stratiform) (Johnson et al. 1999) and incorporate it in the convective heating closure by using  
 158 a switch function for mid-tropospheric dryness. Specifically, shallow congestus convection is  
 159 first initialized with low-level heating (upper-level cooling), moistening the lower troposphere and  
 160 preconditioning the deep convection. Then deep convection warms the whole troposphere due to  
 161 extreme rainfall, followed by stratiform convection with upper-level latent heating and low-level  
 162 cooling by rain evaporation (Khouider and Majda 2008b).

163 The governing equations and multicloud convective parameterization in dimensionless units are  
 164 listed in Table 1 and Table 2, and all relevant parameters in Table 3. All physical variables are  
 165 nondimensionalized by the following synoptic scaling: first-baroclinic dry Kelvin wave speed  $c =$   
 166  $N\frac{H_T}{\pi} = 50ms^{-1}$  for horizontal velocity, equatorial Rossby deformation radius  $L = \sqrt{\beta c} = 1500km$   
 167 for length,  $T = \frac{L}{c} = 8hrs$  for time,  $\bar{\alpha} = \frac{H_T\Theta_0}{\pi g}N^2 = 15K$  for temperature, and  $\frac{\alpha}{T} = 45Kday^{-1}$  for  
 168 heating. For convenience, the moisture anomaly has the unit of temperature in  $K$ . Correspondingly,  
 169 as the moisture sink, the precipitation has the unit of heating in  $Kday^{-1}$ .

170 Consistent with the first-baroclinic deep heating and the second-baroclinic consgestus/stratiform  
 171 heating, both momentum and temperature variables in the free troposphere are truncated to the  
 172 first- and second-baroclinic modes using the following Galerkin projection,

$$f = f_1 \left[ \sqrt{2} \cos(z) \right] + f_2 \left[ \sqrt{2} \cos(2z) \right], \quad f \in \{u, p, F^u\} \quad (1)$$

$$g = g_1 \left[ \sqrt{2} \sin(z) \right] + g_2 \left[ 2\sqrt{2} \sin(2z) \right], \quad g \in \{\theta, S^\theta, F^\theta\} \quad (2)$$

173 where the vertical coordinate  $z$  is scaled by 5 km so that  $z = 0, \pi$  in dimensionless units corre-  
 174 spond to the surface (0 km) and top of the troposphere ( $5\pi \approx 15.7$  km), respectively. Here  $u$  is  
 175 zonal velocity,  $p$  is the pressure perturbation,  $F^u$  is eddy momentum transfer,  $\theta$  is potential tem-  
 176 perature anomaly,  $S^\theta$  is heating, and  $F^\theta$  is eddy heat transfer. As shown by Table 1, the first-  
 177 and second-baroclinic momentum is forced by linear momentum damping mimicking boundary-  
 178 layer turbulent drag  $-\frac{C_d u_0}{h_b} u_j$ , Rayleigh friction  $-\frac{1}{\tau_R} u_j$ , and eddy momentum transfer  $F_j^u$ . The  
 179 first-baroclinic potential temperature is driven by the deep heating  $P$ , and the second-baroclinic  
 180 potential temperature by congestus and stratiform heating  $-H_s + H_c$ . Both are further forced by  
 181 radiative cooling  $-Q_{R,j}^0 - \frac{1}{\tau_D} \theta_j$  and eddy heat transfer  $F^\theta$ . These dynamical fields are coupled to  
 182 a column-integrated moisture perturbation (Khouider and Majda 2006b), where both linear and  
 183 nonlinear moisture advection terms are retained and precipitation  $-\frac{2\sqrt{2}}{\pi} P$  and downdrafts  $\frac{D}{H_T}$  are  
 184 added as moisture sink and source, respectively. Specifically, the precipitation in dimensionless  
 185 units,  $-\frac{2\sqrt{2}}{\pi} P$ , is assumed to be equal to the total column-integrated heating, contributed by the  
 186 first-baroclinic mode. The boundary-layer equivalent potential temperature equation shows that  
 187 surface-level evaporation  $\frac{E}{h_b}$  warms and moistens the boundary layer while the downdrafts  $\frac{D}{h_b}$  have  
 188 the opposite effects. Both congestus heating  $H_c$  and stratiform heating  $H_s$  are governed by linear  
 189 relaxation equations. Congestus heating is triggered in the leading cold and dry mid-troposphere,  
 190 and stratiform heating lags the deep heating region. A switch function for mid-troposphere dry-  
 191 ness  $\Lambda$  is defined in Table 2. The multcloud heating closure is completed by introducing deep  
 192 heating  $P$ , downdrafts  $D$  and evaporation  $E$ .

193 All physical variables are imposed on the domain of the tropical belt,  $0 \leq x < 40,000$  km, with  
 194 periodic boundary conditions in the zonal direction. The governing equations shown in Table 1  
 195 and Table 2 are solved numerically by spatially discretizing the solutions at equal-spaced grids and  
 196 then temporally integrated using the 4th-order Runge-Kutta scheme. The horizontal resolution is

197 100 km and each time step is 4.5 min, close to typical coarse-resolution GCMs. The moisture  
198 equation with nonlinear advection terms is solved by pseudo-spectral methods. To stabilize the  
199 numerical scheme and eliminate grid-scale numerical instability, a fourth-order hyper-diffusion  
200 term is added to all prognostic equations,  $-v f_{xxxx}$ , where the dimensionless value of  $v$ , chosen as  
201  $2 \times 10^{-5}$ , is based on trial-and-error.

202 The radiative-convective equilibrium (RCE) state is a convenient way to describe linear convec-  
203 tive instability of the multcloud model. Specifically, we consider a state where zonal velocity,  
204  $u = 0$ , and potential temperature and moisture perturbation vanish in both the troposphere and the  
205 boundary layer,  $\theta_j = 0, \theta_{eb} = 0$  and  $q = 0$ . The actual value of the other variables at the RCE state  
206 is included in Table 4. Both eddy momentum transfer  $F^u$  and eddy heat transfer  $F^\theta$  are set to zero  
207 in the simulations presented in this section. To trigger unstable moist modes, a random field of  
208 moisture in a very weak magnitude ( $10^{-5}$  in dimensionless units) is added to the initial conditions.  
209 All solutions presented in this paper refer to the equilibrium state obtained after long simulations  
210 (4000 days in Section 2 and 3, 7000 days in Section 4).

### 211 *b. Realistic MJO analog and intraseasonal variability above the equator*

212 We first implement the 2D multcloud model with all default parameter values as in Majda  
213 et al. (2007). The default parameters for the congestus and stratiform adjustment coefficients  
214 are  $\alpha_c = 0.5$  and  $\alpha_s = 0.25$ , respectively, and the background moisture stratification  $\bar{Q}$  is 1.0.  
215 Although the typical value of  $\bar{Q}$  in other studies based on observation has smaller value (0.9), the  
216 larger value of  $\bar{Q}$  is chosen to increase convective instability and intensify precipitation. We run  
217 the simulation for 4000 days, out of which the last 1000-day output are used in the equilibrium  
218 state for interpretation purposes. Since the model output in the default parameter regime share  
219 features that resemble observations, we regard them to be a realistic MJO analog of intraseasonal

220 variability above the equator, and thus as a proxy for observations. It is worth clarifying that by  
221 “realistic”, we refer to the good solutions with optimal parameters in this idealized framework, in  
222 contrast to the deficient solutions as shown in Sec.2c.

223 Fig.1a is the Hovmöller diagram for precipitation during the last 200 days, characterized by a  
224 two-scale structure consisting of eastward-moving planetary-scale envelopes and numerous em-  
225 bedded westward-moving synoptic-scale disturbances. The wavenumber 2 envelopes of period 40  
226 days propagate eastward at  $6.17 \text{ ms}^{-1}$ . Embedded in these planetary-scale envelopes are several  
227 synoptic-scale disturbances that propagate westward at slower speeds, resembling the observed  
228 westward-moving superclusters in the active phases of MJO over the West Pacific, (e.g., 2-day  
229 waves (Chen et al. 1996)). However, this too-regular pulsing of precipitation during the eastward  
230 propagation of planetary-scale envelopes is less realistic than the more intermittent behavior of  
231 observed superclusters in the MJO. Fig.1b and Fig.1c show the log-scale wavenumber-frequency  
232 spectra of precipitation and zonal velocity. The eastward-moving precipitation component has a  
233 dominant peak in wavenumber 2 and period of 30 days. The spectra of zonal velocity are similar  
234 but confined to a smaller wavenumber and longer period, consistent with the observation that the  
235 dynamical circulation usually has larger spatial scales than the heating that drives it. For both  
236 precipitation and zonal velocity, the eastward-moving mode is the sum of at least three distinct  
237 harmonics with the same phase speed, thus differing from the single peak for the MJO seen in  
238 observation (Kiladis et al. 2009). The spectra of the westward-moving mode feature three regular  
239 and linear bands, according to the linearity of the dynamic core in Table 1. These multiple bands  
240 have the same slope as the three peaks of eastward-moving modes, indicating a modulation of  
241 westward-moving synoptic-scale disturbances by eastward-moving envelopes. Fig.1d-e show the  
242 zonal and vertical profiles of the composite planetary-scale envelopes in the moving frame of ref-  
243 erence. As shown by panel (d), the precipitation peak is led by both column-integrated moisture

244 and boundary-layer equivalent potential temperature, and followed by stratiform heating. This  
245 is consistent with the conceptual understanding that a moist free troposphere and boundary layer  
246 tends to precondition deep convection while stratiform convection in the form of anvil clouds  
247 forms subsequent to deep convection. Panel (e) shows the vertical cross-sections of zonal velocity  
248 and potential temperature anomalies in the free troposphere. Both fields are characterized by a  
249 front-to-rear tilt with increasing height, akin to the observed MJO. The surface-level westerlies  
250 resemble the WWB of the observed MJO. It is worth mentioning that the model is invariant under  
251 changing the sign of  $x$  and  $u$  so that the solution does not have direction preference. The eastward  
252 propagation of the MJO analog in Fig. 1a is solely determined by the initial random perturbation.

253 Key features of the realistic MJO analog include the following three aspects: First, two-  
254 scale structure with eastward-moving planetary-scale envelope and embedded westward-moving  
255 synoptic-scale disturbances. Secondly, spectra of precipitation and zonal velocity with dominant  
256 peaks at wavenumber 1-3 and period of 30-90 days in eastward-moving components and wide  
257 bands of spectra signals for westward-moving components at wavenumber 5-15 and period less  
258 than 30 days. Thirdly, front-to-rear tilts in zonal velocity and potential temperature with the WWB  
259 located in the middle and west of the planetary-scale envelope. In connection with the known bi-  
260 ases in complex weather and climate models, contemporary GCMs have difficulty in simulating  
261 the persistent eastward propagation of the MJO (Zhang 2005), let alone the embedded westward-  
262 moving synoptic-scale disturbances. Moreover, the GCMs also show significant discrepancies  
263 in the wavenumber-frequency spectra for planetary/intraseasonal variability and the WWB (Jiang  
264 et al. 2015). In the remaining experiments, we will focus on these three key features of the MJO  
265 analog.

266 *c. Idealized GCM with clear deficiencies*

267 Sensitivity experiments (not shown) show that the model solutions are quite sensitive to several  
268 key parameters, such as stratiform heating adjustment coefficient  $\alpha_s$ , congestus heating adjustment  
269 coefficient  $\alpha_c$  and background moisture stratification  $\tilde{Q}$ . There is no guarantee that these key  
270 parameters will have optimal values in physically motivated applications, resulting in significant  
271 bias and poor behavior. In order to mimic the behavior of GCMs with clear deficiencies, we  
272 reduce the heat adjustment coefficients for congestus  $\alpha_c$  and stratiform convection  $\alpha_s$  to half as  
273 shown by Table 3. Meanwhile, the background moisture stratification  $\tilde{Q}$  is increased from 1.00 to  
274 1.03 to give relatively stronger convective instability. Physically, this increment in the value of  $\tilde{Q}$   
275 corresponds to 3% more background moisture in the lower troposphere.

276 Fig.2a shows Hovmöller diagrams for precipitation after the system attains the equilibrium. The  
277 planetary-scale envelopes are wavenumber 4, somewhat shorter than the observed MJO wave-  
278 length in the wavenumber 1-3 range, and propagate eastward at a speed of  $2.4 \text{ ms}^{-1}$ , much slower  
279 than the typical observed MJO ( $5 \text{ ms}^{-1}$ ). The maximum magnitude of precipitation is equivalent  
280 to about  $8 \text{ Kday}^{-1}$  heating, much weaker than in Fig.1. Fig.2b and Fig.2c show the log-scale  
281 wavenumber-frequency spectra of precipitation and zonal velocity. Notably, these spectra peaks  
282 are quasi-symmetric about the wavenumber zero axis, and both are featured by the planetary-scale  
283 (about wavenumber 4) and intraseasonal (near 40 days) variability. Such eastward/westward sym-  
284 metry stems from the mixture of both eastward- and westward-moving analogs. In fact, present-  
285 day GCMs suffer a similar bias in that the spectra of westward-moving planetary-scale precipita-  
286 tion is as significant as its eastward-moving counterpart.

### 287 **3. Upscale Impact of Mesoscale Convective Systems on the MJO Analog above the Equator**

288 In this section, we assess the upscale impact of MCSs on the MJO analog through comparison  
289 experiments with/without eddy transfer of momentum and temperature from mesoscale fluctua-  
290 tions. Specifically, we use the idealized GCM with clear deficiencies in Fig.2 as the control simu-  
291 lation. In order to introduce the upscale impact of MCSs, we use the explicit expressions for eddy  
292 transfer of momentum and temperature obtained from theoretical predictions of the MESD model  
293 (Yang and Majda 2018b). We consider the upscale impact of MCSs that propagate either slowly (5  
294  $ms^{-1}$ ) or rapidly ( $20ms^{-1}$ ), either upshear or downshear, modulated by either deep heating excess  
295 or vertical shear strength. The observed typical propagation speed of MCSs lies within the range  
296 5-20 m/s (Houze 1975, 1977, 2004). The two speeds (5 and 20 m/s) are chosen to highlight dif-  
297 ferences between slow and rapid propagating scenarios. Due to the invariance of this model under  
298 changing the signs of  $x$ ,  $u$  and  $F''$ , we only need consider the case with westward-moving MCSs  
299 because the opposite case can be inferred through counter analogy.

300 We investigate how the upscale impact of MCSs improves the simulations of the MJO analog  
301 in the idealized GCM with clear deficiency by conducting several experiments with different eddy  
302 transfer of momentum and temperature. In brief, we first consider cases with eddy transfer of  
303 momentum and temperature modulated by the deep heating excess in Sec.3b. Two specific cases  
304 with upscale impact of MCSs propagating westward at either a slow or fast speed are investigated.  
305 We then consider cases with eddy transfer of momentum and temperature modulated by the ver-  
306 tical shear strength in Sec.3c, including three cases with upscale impact of MCSs propagating  
307 westward/upshear/downshear at a slow speed are investigated. Details of the model setup in each  
308 experiment are shown in Table 5.

309 *a. Eddy transfer of momentum and temperature predicted by the MESD model*

310 In general, the multi-scale models based on the multi-scale asymptotic methods (Majda and  
 311 Klein 2003; Majda 2007b) have been applied to study multi-scale interactions of tropical convec-  
 312 tion such as the upscale impact of synoptic-scale fluctuations on the MJO (Majda and Biello 2004;  
 313 Biello and Majda 2005, 2006), the intraseasonal impact of the diurnal cycle on the MJO (Yang  
 314 and Majda 2014; Majda and Yang 2016) and ITCZ breakdown (Yang et al. 2017). In particu-  
 315 lar, the Majda (2007b) MESD model has been used to assess upscale impact of embedded MCSs  
 316 on eastward-moving CCKWs (Yang and Majda 2017, 2018b) and westward-moving 2-day waves  
 317 (Yang and Majda 2018b). In those studies, mesoscale heating is prescribed by phase-lagged first-  
 318 and second-baroclinic modes to mimic the observed front-to-rear tilt structure (Houze 2004),

$$s'_\theta = c_0 [\sin(kx' - \omega\tau) \sin(z) + \alpha \sin(kx' - \omega\tau + \phi_0) \sin(2z)] \quad (3)$$

319 where  $x'$  points to the propagation direction of mesoscale heating.  $c_0$  is magnitude coefficient.  $k$   
 320 and  $\omega$  are wavenumber and frequency respectively. Here  $\alpha$  measures the relative strength of the  
 321 second-baroclinic mode, and  $\phi_0$  the phase lag. The MESD model provides explicit expressions for  
 322 eddy transfer of momentum and temperature,

$$F^u = \kappa^u \left[ -\frac{3}{2} \cos(z) + \frac{3}{2} \cos(3z) \right] \cos(\gamma), \quad \kappa^u = \frac{c_0^2 \sin(\phi_0) \alpha k^3}{2(\omega^2 - k^2)(4\omega^2 - k^2)} \quad (4)$$

$$F^\theta = \kappa^\theta \left[ \frac{3}{2} \sin(z) - \frac{9}{2} \sin(3z) \right], \quad \kappa^\theta = \frac{c_0^2 \sin(\phi_0) \alpha k^3 c}{2(\omega^2 - k^2)(4\omega^2 - k^2)} \quad (5)$$

323 where  $\gamma$  is the tilt angle between propagation direction of mesoscale heating and zonal direction  
 324 in the horizontal plane. In the following experiments, for simplification,  $F^u$  and  $F^\theta$  are further  
 325 truncated by retaining only the dominant first-baroclinic mode.

326 Fig.3 shows vertical profiles of mesoscale fluctuations and the eddy transfer of momentum and  
 327 temperature. In particular, the red curves in panels (c,d) show the corresponding eddy transfer of

328 momentum and temperature for eastward-propagating mesoscale systems. When the mesoscale  
329 systems propagate westward, the sign of eddy momentum transfer is reversed, while that of eddy  
330 heat transfer stays the same. In fact, the CRM study by Badlan et al. (2017) showed that the  
331 vertical profile of eddy momentum transfer is dominated by the first-baroclinic mode. In the simple  
332 multicloud model that resolves the first two baroclinic modes, we further truncate the vertical  
333 profiles of eddy transfer of momentum and temperature by retaining only the first-baroclinic mode.  
334 Consequently, the eddy momentum transfer has eastward (westward) momentum forcing in the  
335 lower (upper) troposphere, with maximum strength at the surface (top) of the domain. The eddy  
336 heat transfer cools throughout the troposphere, with maximum strength in the middle troposphere.

337 It is straightforward to show that the ratio between  $F^\theta$  and  $F^u$  in dimensionless units is deter-  
338 mined by propagation speed of the mesoscale heating,

$$\frac{\kappa^\theta}{\kappa^u} = c \quad (6)$$

339 where  $c$  is the dimensionless value (dimensional value divided by  $50 \text{ ms}^{-1}$ ) of propagation speed  
340 of the mesoscale heating. In the following simulations, we do not need to specify exact values of  
341 parameters in the expressions of  $\kappa^u, \kappa^\theta$ , but just specify the value of  $\kappa^u$ . The value of  $\kappa^\theta$  is then  
342 inferred by Eq.6, when the propagation speed of the mesoscale heating  $c$  is specified.

343 *b. Eddy transfer of momentum and temperature modulated by deep heating excess*

344 Here we consider the scenario when the eddy transfer of momentum and temperature in the first  
345 baroclinic mode is modulated by the maximum allowable deep heating excess  $P_0$  as follows,

$$F^u = \kappa^u \frac{P_0^+}{\bar{Q}} \left[ -\frac{3}{2} \cos(z) \right] \quad (7)$$

$$F^\theta = \kappa^\theta \frac{P_0^+}{\bar{Q}} \left[ \frac{3}{2} \sin(z) \right] \quad (8)$$

346 where  $P_0 = \frac{1}{\tau_{conv}} (a_1 \theta_{eb} + a_2 q - a_0 (\theta_1 + \gamma_2 \theta_2))$  is the anomaly component of the maximum allow-  
 347 able deep heating (see Table 2).  $\bar{Q}$  is the corresponding RCE value. The value of the expression  
 348  $P_0^+$  stays the same as  $P_0$  if  $P_0$  is positive and zero if it is negative. The closure for  $P_0$  is a combina-  
 349 tion of the Betts-Miller relaxation-type parameterization and convective available potential energy  
 350 (CAPE) parameterization. Physically, the maximum allowable deep heating excess  $P_0$  resembles  
 351 the effect of CAPE in modulating MCSs and the resulting CMT (Moncrieff 2004). Majda and  
 352 Stechmann (2008) developed a stochastic parameterization for CMT, whose strength is modulated  
 353 by the square of the maximum allowable deep heating.

354 Three cases are compared with/without  $F^u$  and  $F^\theta$  modulated by the effects of  $P_0$ . The first case  
 355 is the control simulation in Fig.2. The second and third cases consider the eddy transfer of momen-  
 356 tum and temperature from MCSs that propagate at a slow ( $5 \text{ ms}^{-1}$ ) and fast speed ( $20 \text{ ms}^{-1}$ ). The  
 357 magnitude coefficient for eddy momentum transfer  $\kappa^u$  is fixed at 0.0032. The difference between  
 358 the second and third cases lies in the stronger magnitude of  $F^\theta$  in the case of fast propagation.

359 Fig.4 shows the Hovmöller diagrams for precipitation. The control simulation in Fig.4a features  
 360 both eastward- and westward-moving planetary-scale disturbances with no clear two-scale struc-  
 361 ture. Compared with the control simulation, the cases with eddy terms in panels b and c show an  
 362 apparent two-scale structure, where planetary-scale envelopes propagate eastward and embedded  
 363 synoptic-scale disturbances propagate westward. In panel b, the maximum magnitude of precip-  
 364 itation is equivalent to  $28 \text{ K/day}$ . Such intense precipitation and the promoted eastward-moving  
 365 planetary-scale envelope by westward-moving MCSs is consistent with Yang and Majda (2018b).  
 366 In panel c, the maximum magnitude of precipitation is reduced to  $12 \text{ K/day}$  and convection is  
 367 suppressed due to the extra cooling from eddy heat transfer, again consistent with Yang and Majda  
 368 (2018b). This extra cooling reduces low-level moisture convergence, resulting in a weaker growth  
 369 rate of the unstable modes.

370 Fig.5 shows the log-scale wavenumber-frequency spectra of precipitation and zonal velocity.  
371 Compared with the control simulation in panel a, both cases show a clear east/west contrast in the  
372 spectra, similar to the realistic MJO analog shown in Fig.1. For the slowly propagating MCSs,  
373 the spectra of precipitation in panel c are characterized by three discrete spectra peaks for the  
374 eastward-moving components and three bands of spectra of westward-moving components. In  
375 particular, the peak for eastward-moving planetary-scale envelope has wavenumber 3 and period  
376 about 50 days. The spectra of zonal velocity in panel d resembles that in panel c, indicating close  
377 correlation between convection and the large-scale circulation. As for the faster propagating MCSs  
378 in panels e-f, the associated spectra of precipitation are dominated by a planetary-scale peak for  
379 the eastward-moving component and a band of spectra for the westward-moving component.

380 Fig.6 shows the vertical cross-sections of the composite planetary-scale envelopes in the mov-  
381 ing reference frame. The vertical structure of zonal velocity and potential temperature anomalies  
382 features a significant front-to-rear tilt, consistent with the built-in transition of life-cycle from con-  
383 gestus to deep to stratiform convection. In panel a, the maximum magnitude of zonal velocity  
384 of about  $2 \text{ ms}^{-1}$  is at the top of the domain. In the lower troposphere, the wind convergence is  
385 mostly in phase with the maximum precipitation with westerlies to the west and easterlies to the  
386 east. The WWB is negligible. The maximum magnitude of both positive and negative potential  
387 temperature are both attained in the upper troposphere. In contrast, both the maximum magni-  
388 tude of zonal velocity, potential temperature anomalies and precipitation anomalies in panel b are  
389 much weaker than those in panel a, indicating suppressed convection due to eddy heat transfer.  
390 The control simulation features a mixture of both eastward- and westward-propagating large-scale  
391 disturbances. The corresponding composite planetary-scale envelope that is calculated only along  
392 the eastward-moving reference frame is less meaningful and thus not shown.

393 *c. Eddy transfer of momentum and temperature modulated by vertical shear*

394 Here we consider the scenario when eddy transfer of momentum and temperature is modulated  
 395 by the strength of vertical shear  $\Delta U$  as follows,

$$F^u = \kappa^u \frac{\Delta U}{U_{ref}} \left[ -\frac{3}{2} \cos(z) \right] \quad (9)$$

$$F^\theta = \kappa^\theta \frac{\Delta U}{U_{ref}} \left[ \frac{3}{2} \sin(z) \right] \quad (10)$$

396 where  $U_{ref} = 50ms^{-1}$  and the strength of vertical shear is defined as follows,

$$U_{max}^u = \max_{\pi/2 \leq z \leq \pi} \{u\}; U_{min}^u = \min_{\pi/2 \leq z \leq \pi} \{u\} \quad (11)$$

$$U_{max}^l = \max_{0 \leq z \leq \pi/2} \{u\}; U_{min}^l = \min_{0 \leq z \leq \pi/2} \{u\} \quad (12)$$

$$\Delta U \equiv \max \left\{ \left| U_{max}^u - U_{min}^l \right|, \left| U_{min}^u - U_{max}^l \right| \right\} \quad (13)$$

397 Fig.7a explains the definition of vertical shear strength  $U_{max}^l$ , which basically calculates the maxi-  
 398 mum possible easterly and westerly shear between the upper and lower troposphere and selects the  
 399 larger one. Fig.7b describes the scenarios when the MCSs propagate upshear (along the opposite  
 400 direction of vertical shear) and downshear (along the same direction of vertical shear).

401 Four cases are compared with/without  $F^u$  and  $F^\theta$  modulated by the effects of  $\Delta U$ . Besides the  
 402 first cases from the control simulation in Fig.2, the remaining three cases consider the eddy transfer  
 403 of momentum and temperature from MCSs that propagate westward, upshear and downshear at a  
 404 slow speed ( $5 ms^{-1}$ ). Correspondingly, the magnitude coefficient of eddy momentum transfer  $\kappa^u$   
 405 is 0.0024, 0.0030, 0.0030, respectively. The choice of a smaller value of  $\kappa^u$  in the second case is  
 406 to obtain a more realistic precipitation intensity.

407 Fig.8 shows the Hovmöller diagrams for precipitation. Compared with the control simulation in  
 408 Fig.8a, the maximum magnitude of precipitation in both Fig.8b and Fig.8c is intensified, while that  
 409 in Fig.8d is weakened. Specifically, the maximum magnitude of precipitation in Fig.8b reaches

410 25 K/day, consistent with the Yang and Majda (2018b) result that westward-moving MCSs favor  
411 the eastward propagation of convection. The pattern of spatio-temporal variability of precipita-  
412 tion in Fig.8b features the two-scale structure with eastward-moving planetary-scale envelopes at  
413 wavenumber 3 and embedded shorter wavelength westward-moving synoptic-scale disturbances.  
414 Compared with the realistic MJO analog in Fig.1, the solutions exhibit more intermittency in  
415 precipitation intensity and spatio-temporal pattern. In Fig.8c, the maximum precipitation also in-  
416 tensifies to 19 K/day, which is associated with the strengthened low-level moisture convergence  
417 due to the positive feedback between vertical shear and eddy momentum transfer. The precipita-  
418 tion anomalies are dominated by both eastward- and westward-moving planetary-scale envelopes  
419 and exhibit no clear east/west contrast. Based on a similar argument, the precipitation in Fig.8d  
420 is reduced due to the negative feedback between vertical shear and eddy momentum transfer from  
421 downshear-moving MCSs. Due to the lack of persistent propagating planetary-scale envelopes,  
422 this downshear-moving case is omitted in Fig.9 and Fig.10.

423 Fig.9 shows the log-scale wavenumber-frequency spectra of precipitation and zonal velocity  
424 for these three cases. Compared with the symmetric spectra in the control simulation, Fig.9c  
425 and Fig.9d are characterized by significant zonal asymmetry. Specifically, the eastward-moving  
426 components are dominated by a continuous band of spectra along the non-dispersive line across  
427 the equator, which extends from wavenumber 3 to 10 and period from 15 days to 50 days. In  
428 this case, such continuous spectra reflect the intermittent nature of both precipitation and zonal  
429 velocity. For the case in Fig.9e and Fig.9f, the spectra of both precipitation and zonal velocity  
430 exhibits significant symmetry under changing sign of  $x$ , indicating the prevalence of both the  
431 eastward-moving MJO analog and westward-moving reversed MJO analog.

432 Fig.10 shows vertical cross-sections of zonal velocity and potential temperature anomalies. No-  
433 tably, the WWB does not reach the surface in Fig.10a, whereas it has a much stronger magnitude in

434 Fig.10b. In the case with eddy terms from westward-moving MCSs, the eddy momentum transfer  
435 induces low-level westward (upper-level eastward) momentum forcing, reducing the westerlies  
436 to the west but increasing easterlies to the east. In contrast, in the case where MCSs propa-  
437 gate upshear, the positive feedback between vertical shear and eddy momentum transfer tends  
438 to strengthen both westerlies (easterlies) to the west (east) at the surface (see Eq.9). Due to the  
439 relatively stronger modulation by vertical shear strength to the west, the resulting surface-level  
440 westerly winds dominate. In these two cases, both zonal velocity and potential temperature fields  
441 exhibit a front-to-rear tilt, due to the built-in transition from congestus to deep to stratiform con-  
442 vection.

#### 443 **4. Parameterization of the Upscale Impact of MCSs in the Idealized GCM**

444 According to Section 3, the upscale impact of westward-moving MCSs under the modulation of  
445 deep heating excess produces a persistent propagating MJO analog with a two-scale structure and  
446 realistic variability of precipitation and winds. In contrast, the upscale impact of upshear-moving  
447 MCSs under the modulation of vertical shear strength produces a significant WWB. In this section,  
448 we provide a basic parameterization of the upscale impact of upshear-moving MCSs modulated  
449 by both deep heating excess and vertical shear strength. We test the improvement of key features  
450 of the MJO analog in the idealized GCM having clear deficiencies. In particular, we focus on the  
451 cases with upscale impact of MCSs propagating upshear at a slow speed, modulated by the effects  
452 of both deep heating excess and vertical shear strength.

453 *a. A basic parameterization of upscale impact of MCSs combining upshear momentum and deep*  
 454 *heating excess in the GCM*

455 In reality, the maximum allowable deep heating  $P_0$  (conceptually similar to CAPE) should  
 456 mainly influence the magnitude of mesoscale heating, while the vertical shear strength influences  
 457 the vertical tilting angles of MCSs (i.e., relative location among shallow congestus, deep and strat-  
 458 iform convection). According to previous results based on the MESD model (Yang and Majda  
 459 2018b), both conditions control the magnitude and sign of the eddy transfer of momentum and  
 460 temperature. Here we combine these two conditions by summing them linearly with a tuning  
 461 coefficient  $\alpha$ , and assume that the MCSs all propagate upshear.

462 A basic parameterization for upscale impact of MCSs (eddy transfer of momentum and temper-  
 463 ature  $F^u, F^\theta$ ) is,

$$F^u = \kappa^u \left( \alpha \frac{P_0}{\bar{Q}} + (1 - \alpha) \frac{|\Delta U|}{U_{ref}} \right) \text{sign}(\Delta U) \left[ -\frac{3}{2} \cos(z) \right] \quad (14)$$

$$F^\theta = \kappa^\theta \left( \alpha \frac{P_0}{\bar{Q}} + (1 - \alpha) \frac{|\Delta U|}{U_{ref}} \right) \left[ \frac{3}{2} \sin(z) \right] \quad (15)$$

464 where  $P_0 = \left| \frac{1}{\tau_{conv}} (a_1 \theta_{eb} + a_2 q - a_0 (\theta_1 + \gamma_2 \theta_2)) \right|^+$  is the positive excess of the maximum allowable  
 465 deep heating and  $\bar{Q}$  is its RCE value, and  $\Delta U$  represents the vertical shear strength,  $U_{ref} = 10ms^{-1}$ .  
 466 Recall that the magnitude coefficients  $\kappa^u > 0$ ,  $\kappa^\theta < 0$  satisfy the relation  $\left| \frac{\kappa^\theta}{\kappa^u} \right| = c$ , where  $c$  is the  
 467 absolute propagation speed of the MCSs. The coefficient  $\alpha$  controls the relative importance of  
 468  $P_0$  and vertical shear strength in modulating the strength of the eddy transfer of momentum and  
 469 temperature.

470 *b. Three-way interaction between MJO analog, parameterized upscale impact of MCSs, and back-*  
471 *ground vertical shear on longer time scales*

472 Here we test effects of the parameterization by adding it into the idealized GCM having clear  
473 deficiencies. Four cases with various value of  $\alpha$  in Eqs.14-15 are considered. The magnitude coef-  
474 ficient  $\kappa''$  is fixed at 0.0008 and speed of MCSs  $c$  is 0.1 (corresponds to  $5 \text{ ms}^{-1}$ ). In order to explore  
475 the solutions over longer time scales, we extend the integration period to 7000 days and use the  
476 last 3000-day model output for analysis. For better visualization, we perform a low-pass filtering  
477 by transforming solutions into wavenumber-frequency spectra in Fourier space and only keeping  
478 small wavenumber and frequency (large wavelength and period). Only precipitation anomalies at  
479 the length scale longer than 10,000 km and time scale longer than 30 days are retained.

480 Fig.11 shows the Hovmöller diagrams for precipitation with various value of  $\alpha$ . A large value of  
481  $\alpha$  corresponds to stronger modulation by deep heating excess  $P_0$ , while a smaller value of  $\alpha$  corre-  
482 sponds to stronger modulation by vertical shear strength. One particular interesting feature is the  
483 direction switching of the MJO analog for  $\alpha = 0.8$  (panel c) and  $\alpha = 1.0$  (panel d). In panel c, the  
484 MJO analog persistently propagates eastward between day 4000 and day 4500, switches to west-  
485 ward propagation between day 4500 and day 4800, then switches back to eastward propagation  
486 between day 5000 and day 5300, and so forth. The period between two eastward (or westward)  
487 propagation phases is about 800 days, much longer than the intraseasonal time scale. Such a QBO-  
488 like behavior in the presence of CMT are quite similar to Majda and Stechmann (2009) which also  
489 shows periodic direction switching of unstable CCEWs and background mean flow. It is worth  
490 clarifying that by “QBO-like”, we mean the behavior of direction switching is similar to the man-  
491 ifestation of the QBO but not the underlying processes. Compared with panel c, the solution in  
492 panel d differs in the duration of persistent propagation of the MJO analog/reversed MJO analog in

493 each phase, exhibiting more chaotic features. For example, the persistently eastward-propagating  
494 MJO analog lasts 1200 days between day 5500 and day 6700, while that between day 4500 and  
495 day 5000 only last 500 days. Unlike panels c and d, the solutions in panels a and b show little  
496 QBO-like behavior. Such a clear difference among the cases with large/small value of  $\alpha$  indicates  
497 the crucial modulation effects of deep heating excess on the eddy terms from upshear-moving  
498 MCSs. As shown by Fig.11e, the realistic MJO analog features persistent eastward propagation  
499 over a long time period. In contrast, the solution in Fig.11f from the deficient GCM shows a  
500 transient behavior with alternate eastward/westward propagation during day 4000 and day 5000,  
501 standing-wave pattern near day 5500 and persistent westward propagation after day 6000.

502 For  $\alpha = 0.8$  in Fig.12a shows a periodic direction-switch between eastward-propagating MJO  
503 analog and westward-propagating reversed MJO analog. Panel b shows the domain-mean zonal  
504 winds in the first-baroclinic mode, which also exhibits a periodic direction-switch between east-  
505 erlies and westerlies. Such a QBO-like behavior in domain-mean flow also occurs in the CRM  
506 studies by Held et al. (1993). Specifically, during the phase with eastward-moving (westward-  
507 moving) MJO analog, the domain-mean zonal winds gradually increase from low-level easter-  
508 lies (westerlies) to low-level westerlies (easterlies), reaching its maximum magnitude as the MJO  
509 analog switches direction. The persistently eastward (westward) propagation phase is highly cor-  
510 related with the increasing (decreasing) background zonal winds. According to the governing  
511 equations for  $u_1$  in Table 1, domain-mean zonal winds vanish in the cases without eddy momen-  
512 tum transfer. Thus, the accumulating contribution by eddy momentum transfer modulated by  
513 deep heating excess associated with the MJO analog induces these nonzero domain-mean back-  
514 ground flow. Fig.12c shows the time series of domain-mean thermodynamical fields, including  
515 first-baroclinic potential temperature, boundary-layer equivalent potential temperature, and mois-  
516 ture. The domain-mean first-baroclinic potential temperature decreases at each phase when MJO

517 analog persistently propagates westward/eastward. Such cooling effects can be explained by eddy  
518 heat transfer from MCSs that accumulate in space and time as the MJO analog persistently propa-  
519 gates across the domain.

520 Fig.13a shows the zonal/vertical cross-sections of zonal velocity and zonal profiles of deep heat-  
521 ing excess and vertical shear strength in the composite eastward-moving planetary-scale envelopes.  
522 A significant WWB is produced, resembling the realistic MJO analog in Fig.1. A crucial feature  
523 is the displacement of the peak of deep heating excess to the west of the dashed line, which is  
524 consistent with the observation that convective center of the MJO typically sits over the WWB in  
525 easterly vertical shear. Such westward displacement of the deep heating excess preferably mod-  
526 ulates eddy momentum transfer in the trailing edge, resulting in a stronger low-level eastward  
527 momentum forcing in the trailing edge than in the leading edge. The relatively weak maximum  
528 zonal velocity compared to the realistic MJO analog in Fig.1 is due to the intermittent property of  
529 the solutions shown in the Hovmöller diagram in Fig.13b. Specifically, westerlies and easterlies  
530 are not aligned during the eastward propagation of planetary-scale envelopes and cancel each other  
531 after averaging in the eastward-moving reference frame.

532 We identify the following three-way interaction between MJO analog, parameterized upscale  
533 impact of MCSs, and background vertical shear:

534 1. Eastward-moving MJO analog modulates eddy momentum transfer mainly through deep  
535 heating excess.

536 2. Due to the westward displacement of the deep heating excess, the resulting eddy momentum  
537 transfer with low-level eastward momentum forcing accumulates in space and time and switches  
538 the low-level background flow from easterlies to westerlies. This explains why the propagation  
539 direction of the MJO analog matches that of the change in background winds.

540 3. Background vertical shear with low-level westerlies favors the westward-moving reversed  
541 MJO analog. The underlying mechanism is related to eastward moisture advection, resulting in  
542 eastward-moving synoptic-scale disturbances and a westward-moving planetary-scale envelope.  
543 This explains why the background winds peaks slightly lead the direction switching of the MJO  
544 analog.

545 4. Mechanisms similar to 1-3 are repeated, but in opposite directions.

546 Fig.13c-d shows the log-scale wavenumber-frequency spectra of precipitation and zonal veloc-  
547 ity, which is akin to the realistic MJO analog in Fig.1. The spectra of both fields show a clear peak  
548 for eastward-moving planetary-scale envelope at wavenumber 2 and period of 50 days, with a  
549 band of extra spectra extending to higher wavenumber and frequency. For westward-moving com-  
550 ponents, the spectra of precipitation shows a peak at wavenumber 5-8 and period of 25-40 days.  
551 Extra bands of spectra occur at higher wavenumber and frequency, while that of zonal velocity has  
552 a more dominant peak at smaller wavenumber.

553 It is interesting to question why the scenario with dominant modulation effects by vertical shear  
554 does not exhibit such a QBO-like behavior, considering that the easterly vertical shear in the trail-  
555 ing edge is stronger than in the leading edge. Although the magnitude of westerly vertical shear  
556 in the leading edge is weaker, it covers a much broader area. After the eddy momentum transfer  
557 in both leading and trailing edges accumulate in space, the resulting background zonal winds are  
558 comparable with no persistent direction preference. Also, the mechanism that background verti-  
559 cal shear with low-level westerlies favoring westward-moving reversed MJO analog differs from  
560 the observation over Indian Ocean, presumably due to the idealized two-dimensional model setup  
561 without rotation. In the three-dimensional model setup, the presence of the Coriolis force would  
562 break the zonal symmetry and induce favorable propagation direction of the MJO analog.

563 *c. Improving other deficiencies by parameterizing the upscale impact of MCSs*

564 It would be interesting to consider other deficiencies in this idealized GCM due to different pa-  
565 rameter values and investigate how the upscale impact of MCSs would improve them. Here we  
566 specifically focus on two deficiencies. The first one has almost the same parameters as the realis-  
567 tic simulation in Fig.1, except for the coefficient of the second-baroclinic mode in linear moisture  
568 convergence  $\tilde{\lambda} = 0.3$  (optimal value is 0.6) and the background moisture stratification  $\tilde{Q} = 1.03$   
569 (optimal value is 1.0). This deficiency due to the reduced coupling of the second-baroclinic mode  
570 mimics the underestimated role of shallow convection in the cumulus parameterization in the  
571 GCMs (Zhang and Song 2009). The second deficiency differs from the realistic simulation in  
572 Fig.1 only by the inverse convective buoyancy time scale of deep clouds  $a_0 = 32$  (optimal value is  
573 12). These two deficiencies are modified by adding the parameterization under the same configu-  
574 ration as Fig.13.

575 Fig.14a shows the Hovmöller diagram for precipitation in the first deficiency during a 200-day  
576 period. The solution is characterized by eastward-moving precipitating events in wavenumber 5  
577 and period of 40 days. In contrast, the improved simulation by the parameterization in Fig.14b  
578 shows a clear two-scale structure with eastward-moving planetary-scale envelopes and embed-  
579 ded westward-moving synoptic-scale disturbances. The maximum precipitation is intensified to  
580  $30 \text{ Kday}^{-1}$ . Over a longer period, this improved simulation also shows a QBO-like behavior  
581 with direction switching in Fig.14c, similar to Fig.12a. Fig.14d shows the Hovmöller diagram  
582 for precipitation in the second deficiency. The solution is characterized by periodic eastward-  
583 moving events in wavenumber 5, which has much shorter length scale than the observed MJO in  
584 wavenumber 1-3 (Kiladis et al. 2009). After adding the parameterization, these eastward-moving  
585 events have larger spatial scales in wavenumber 3 with more intermittency in Fig.14e. Inter-

586 estingly, these planetary-scale envelopes exhibit persistent eastward propagation over the longer  
587 period in Fig.14f, presumably due to the stronger coupling with the second-baroclinic mode.

## 588 **5. Concluding Discussion**

589 A simple multicloud model for MJO analog and intraseasonal variability above the equator is  
590 studied. With reduced congestus and stratiform heating, the resulting solutions from this simple  
591 model are used as an idealized GCM having clear deficiencies. By adding eddy transfer of mo-  
592 mentum and temperature predicted by the MESD model, we assess the upscale impact of MCSs  
593 on three key features of the MJO analog: persistent propagation of a two-scale structure, real-  
594 istic planetary/intraseasonal variability in precipitation and winds, and a significant WWB. We  
595 then introduce a basic parameterization of upscale impact of upshear-moving MCSs modulated by  
596 the effects of deep heating excess and vertical shear strength and test its effects in the idealized  
597 deficient GCM.

598 Table 5 summarizes results reported in this paper regarding the above three key features of the  
599 MJO analog in the idealized deficient GCM. Compared to the realistic MJO analog, the idealized  
600 deficient GCM fails to reproduce these three features, thereby mimicking the significant bias of the  
601 simulated MJO in present-day GCMs. According to Khouider et al. (2012), MCSs and squall lines  
602 are prominent in the convectively active regions of the MJO envelope, indicating the modulation  
603 of the MCSs by the MJO convective center. The eddy transfer of momentum and temperature from  
604 westward-moving MCSs traveling at a slow speed ( $5 \text{ ms}^{-1}$ ) improves the two-scale structure of  
605 the eastward-moving MJO analog and space-time variability of precipitation and winds, but fails  
606 to strengthen WWB. This is consistent with the theoretical prediction by the MESD model (Yang  
607 and Majda 2018b); i.e., westward-moving MCSs embedded in the large-scale convective enve-  
608 lope provide favorable conditions for convection to the east, that promotes the eastward-moving

609 convective envelope. On the other hand, vertical shear plays a crucial role in organized tropical  
610 convection (Moncrieff 1992), including the influence on its front-to-rear tilt structure and propaga-  
611 tion directions (Moncrieff and Liu 1999; Stechmann and Majda 2009). In particular, eddy transfer  
612 of momentum and temperature from upshear-moving MCSs induces a significant WWB in the  
613 middle and west of the MJO analog. This is due to the two-way feedback between environmental  
614 easterly vertical shear and the embedded eddy momentum transfer with low-level eastward mo-  
615 mentum forcing. The eddy transfer of momentum and temperature modulated by the effects of  
616 vertical shear strength alone fails to reproduce the two-scale structure of the MJO analog and a  
617 realistic space-time variability of precipitation and winds.

618 In order to incorporate those improvements in global models, we provide a basic parameteriza-  
619 tion of the upscale impact of upshear-moving MCSs that linearly combines the modulation effects  
620 of deep heating excess and vertical shear strength. This basic parameterization shares goals similar  
621 to the MCSP introduced by Moncrieff et al. (2017); notably representing the upscale effects of or-  
622 ganized tropical convection that are missing from contemporary parameterizations in GCMs. The  
623 main purpose of the Moncrieff et al. (2017) prototype version of MCSP was to demonstrate the  
624 upscale effects of top-heavy convective heating and momentum transport in the simplest possible  
625 manner, in order to provide proof-of-concept. This was achieved by focusing on eastward propa-  
626 gation and a full GCM. The results of this present paper will be valuable for the future development  
627 of MCSP, because the heating and CMT (i.e., upscale impact of MCSs) have been quantified in  
628 simplest ways. However, this basic parameterization differs from the MCSP in several aspects  
629 that significantly improve the feasibility and reliability of the parameterization. First, it considers  
630 both deep heating excess (a similar concept as CAPE) and vertical shear strength in modulating  
631 the upscale impact of MCSs, while the parameterized CMT in MCSP has constant magnitude over  
632 convective regions. Secondly, it assumes eddy transfer of momentum and temperature from MCSs

633 that propagate upshear (opposite to vertical shear direction), allowing vertical shear to determine  
634 the propagation direction of MCSs and the sign of eddy momentum transfer. Thirdly, it highlights  
635 the crucial contribution of eddy transfer of temperature as predicted theoretically by the MESD  
636 model.

637 The implementation of this basic parameterization of upscale impact of MCSs in the idealized  
638 deficient GCM shows significant improvement in capturing key features of the MJO. A further ex-  
639 amination of a longer-period simulation reveals a three-way interaction between the MJO analog,  
640 the parameterization of upscale impact of MCSs, and the background mean flow. The westward-  
641 displaced deep heating excess in the eastward-moving MJO analog favors eddy momentum trans-  
642 fer with low-level eastward (upper-level westward) momentum forcing. The effects of the eddy  
643 momentum transfer accumulate in space and time and gradually switches the direction of back-  
644 ground mean flow which, in turn, alter the propagation directions of the MJO analog. Under this  
645 three-way interaction mechanism, the background mean flow exhibits a QBO-like behavior, re-  
646 sembling similar phenomenon in CRM simulations (Held et al. 1993). Although in reality the  
647 Coriolis force would break down the zonal symmetry, such a three-way interaction mechanism  
648 may shed light on the interactions between eastward-moving MJO, upscale impact of MCSs and  
649 climatological vertical shear.

650 The basic parameterization of upscale impact of MCSs can be elaborated in several ways and  
651 tested in a hierarchy of models. Besides the first-baroclinic mode, it is also interesting to investi-  
652 gate the effects of eddy transfer of momentum and temperature due to higher baroclinic modes, as  
653 shown by studies based on the MESD model (Yang and Majda 2018b) and reanalysis data (Oh et al.  
654 2015). A different scenario to assess the upscale impact of MCSs on the planetary/intraseasonal  
655 variability includes the Walker circulation over the warm pool. Furthermore, we would like to test  
656 effects of this basic parameterization of upscale impact of MCSs in more comprehensive GCMs.

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855 precipitation and winds with planetary/intraseasonal peaks, (3) westerly wind  
856 burst. . . . . 45

857 TABLE 1. Prognostic governing equations in the 2D multicloud model for the MJO analog and intraseasonal  
858 variability above the equator.

Name	Equation
Momentum, $j$ th-baroclinic mode, $j = 1, 2$	$\frac{\partial u_j}{\partial t} = \frac{\partial \theta_j}{\partial x} - \frac{C_d u_0}{h_b} u_j - \frac{1}{\tau_R} u_j + F_j^u$
Potential temperature, first-baroclinic mode	$\frac{\partial \theta_1}{\partial t} - \frac{\partial u_1}{\partial x} = P - Q_{R,1}^0 - \frac{1}{\tau_D} \theta_1 + F_1^\theta$
Potential temperature, second-baroclinic mode	$\frac{\partial \theta_2}{\partial t} - \frac{1}{4} \frac{\partial u_2}{\partial x} = -H_s + H_c - Q_{R,2}^0 - \frac{1}{\tau_D} \theta_2 + F_2^\theta$
Free tropospheric moisture	$\frac{\partial q}{\partial t} + \frac{\partial}{\partial x} \left[ (u_1 + \tilde{\alpha} u_2) q + \tilde{Q} (u_1 + \tilde{\lambda} u_2) \right] = -\frac{2\sqrt{2}}{\pi} P + \frac{D}{H_T}$
Boundary-layer equivalent potential temperature	$\frac{\partial \theta_{eb}}{\partial t} = \frac{1}{h_b} (E - D)$
Congestus heating	$\frac{\partial H_c}{\partial t} = \frac{1}{\tau_c} \left( \alpha_c \frac{\Lambda - \Lambda^*}{1 - \Lambda^*} \frac{D}{H_T} - H_c \right)$
Stratiform heating	$\frac{\partial H_s}{\partial t} = \frac{1}{\tau_s} (\alpha_s P - H_s)$

859 TABLE 2. Diagnostic equations in the 2D multcloud model for the MJO analog and intraseasonal variability  
860 above the equator. The notation bar indicates the value of variables at RCE state. The notation  $f^+$  represents  
861 positive value of  $f$  and vanishes when  $f < 0$ , that is,  $f^+ = \max\{f, 0\}$ .

Name	Equation
Mid-tropospheric equivalent potential temperature	$\theta_{em} = q + \frac{2\sqrt{2}}{\pi} (\theta_1 + \alpha_2 \theta_2)$
Switch function for mid-tropospheric dryness	$\Lambda = \begin{cases} 1 & \text{if } \bar{\theta}_{eb} - \bar{\theta}_{em} + \theta_{eb} - \theta_{em} \geq 20 \text{ K} \\ \text{linear} & \text{between} \\ \Lambda^* & \text{if } \bar{\theta}_{eb} - \bar{\theta}_{em} + \theta_{eb} - \theta_{em} \leq 10 \text{ K} \end{cases}$
Deep heating	$P = \frac{1-\Lambda}{1-\Lambda^*} P_0$ $= \frac{1-\Lambda}{1-\Lambda^*} \left[ \bar{Q} + \frac{1}{\tau_{conv}} (a_1 \theta_{eb} + a_2 q - a_0 (\theta_1 + \gamma_2 \theta_2)) \right]^+$
Downdrafts	$D = \Lambda D_0$ $= \Lambda m_0 \left[ 1 + \mu_2 \frac{H_s - H_c}{\bar{P}} \right]^+ (\bar{\theta}_{eb} - \bar{\theta}_{em} + \theta_{eb} - \theta_{em})$
Surface evaporation flux	$\frac{E}{h_b} = \frac{1}{\tau_e} (\theta_{eb}^* - \bar{\theta}_{eb} - \theta_{eb})$

862 TABLE 3. Parameters and constants in the idealized GCM with clear deficiencies. The different value of  
863 parameters and constants used for the realistic MJO analog above the equator is shown in the bracket. All the  
864 remaining ones are the same as Majda et al. (2007).

Name	Symbol	Value
First baroclinic radiative cooling rate	$Q_{R,1}^0$	1 K/day
Stratiform adjustment coefficient	$\alpha_s$	0.125 (0.25)
Congestus adjustment coefficient	$\alpha_c$	0.25 (0.5)
Height of troposphere	$H_T$	15.7 km
Height of the boundary layer	$h_b$	500 m
Relative contribution of stratiform and congestus to downdrafts	$\mu_2$	0.5
Convective time scale	$\tau_{comv}$	12 hrs
Momentum drag time scale due to turbulent fluctuations	$\tau_{tur}$	28.9 days
Rayleigh-wind relaxation time scale	$\tau_R$	150 days
Newtonian cooling time scale	$\tau_D$	100 days
Stratiform adjustment time scale	$\tau_s$	7 days
Congestus adjustment time scale	$\tau_c$	7 days
Inverse convective buoyancy time scale of deep clouds	$a_0$	12
Relative contribution fraction of $\theta_{eb}$ to deep convection	$a_1$	0.1
Relative contribution fraction of $q$ to deep convection	$a_2$	0.9
Relative contribution of $\theta_2$ to deep heating	$\gamma_2$	0.1
Relative contribution of $\theta_2$ to $\theta_{em}$	$\alpha_2$	0.1
Coefficient of $\mathbf{v}_2$ in nonlinear moisture convergence	$\tilde{\alpha}$	0.1
Coefficient of $\mathbf{v}_2$ in linear moisture convergence	$\tilde{\lambda}$	0.6
Background moisture stratification	$\tilde{Q}$	1.03 (1.0)
Lower threshold of the switch function $\Lambda$	$\Lambda^*$	0.2

865 TABLE 4. Value of thermodynamic variables at RCE state. The remaining variables not mentioned here are  
 866 all zero. The different values of parameters and constants used for the realistic MJO analog above the equator is  
 867 shown in the brackets.

Name	Symbol	Value
Discrepancy between boundary layer and middle troposphere $\theta_e$	$\bar{\theta}_{eb} - \bar{\theta}_{em}$	12 K
Discrepancy between boundary layer $\theta_e$ and its saturated value	$\theta_{eb}^* - \bar{\theta}_{eb}$	10 K
Moisture switch at RCE	$\bar{\Lambda}$	0.36
Bulk convective heating at RCE	$\bar{Q}$	$1.25 \text{ Kday}^{-1}$
Congestus heating at RCE	$\bar{H}_c$	$0.045 \text{ Kday}^{-1}$ (0.09 $\text{Kday}^{-1}$ )
Deep heating at RCE	$\bar{H}_d$	$1 \text{ Kday}^{-1}$
Stratiform heating at RCE	$\bar{H}_s$	$0.125 \text{ Kday}^{-1}$ (0.25 $\text{Kday}^{-1}$ )
Second baroclinic radiative cooling rate	$Q_{R,2}^0$	$-0.08 \text{ Kday}^{-1}$ (-0.16 $\text{Kday}^{-1}$ )
Downdraft mass flux reference scale	$m_0$	$0.0364 \text{ ms}^{-1}$ (0.035 $\text{ms}^{-1}$ )
Evaporation time scale	$\tau_e$	8.49 hrs

868 TABLE 5. Summary of all experiments under the different model setup and their results in capturing key fea-  
869 tures of the MJO. In the “upscale impact of MCSs” column, “no” means no eddy is added, “westward/eastward”  
870 means the propagation direction of MCSs, “slow/fast” corresponds to  $5/20 \text{ ms}^{-1}$ , “upshear/downshear” means  
871 the propagation direction of MCSs is opposite/along vertical shear direction. The “modulation” column shows  
872 the modulation effects of deep heating excess  $P_0$  and vertical shear strength. The “key feature” column includes  
873 (1) two-scale structure of the MJO analog, (2) wavenumber-frequency spectra of precipitation and winds with  
874 planetary/intraseasonal peaks, (3) westerly wind burst.

Experiments	Model Setup		Key Feature			Figure
	upscale impact of MCSs	modulation	two-scale	spectra	WWB	
Realistic MJO analog	no	N/A	<b>good</b>	<b>good</b>	<b>good</b>	Fig.1
Idealized GCM with clear deficiencies	no	N/A	bad	bad	bad	Fig.2
Improved simulations by the parameterization of upscale impact of MCSs	westward, slow	$P_0$	<b>good</b>	<b>good</b>	bad	Fig.4b,5c,5d,6a
	westward, fast	$P_0$	bad	<b>good</b>	bad	Fig.4c,5e,5f,6b
	westward, slow	shear	<b>good</b>	bad	bad	Fig.8b,9c,9d,10a
	upshear, slow	shear	bad	bad	<b>good</b>	Fig.8c,9e,9f,10b
	downshear, slow	shear	bad	not shown	not shown	Fig.8d
	upshear, slow	$P_0$ & shear	<b>good</b>	<b>good</b>	<b>good</b>	Fig.11,12,13

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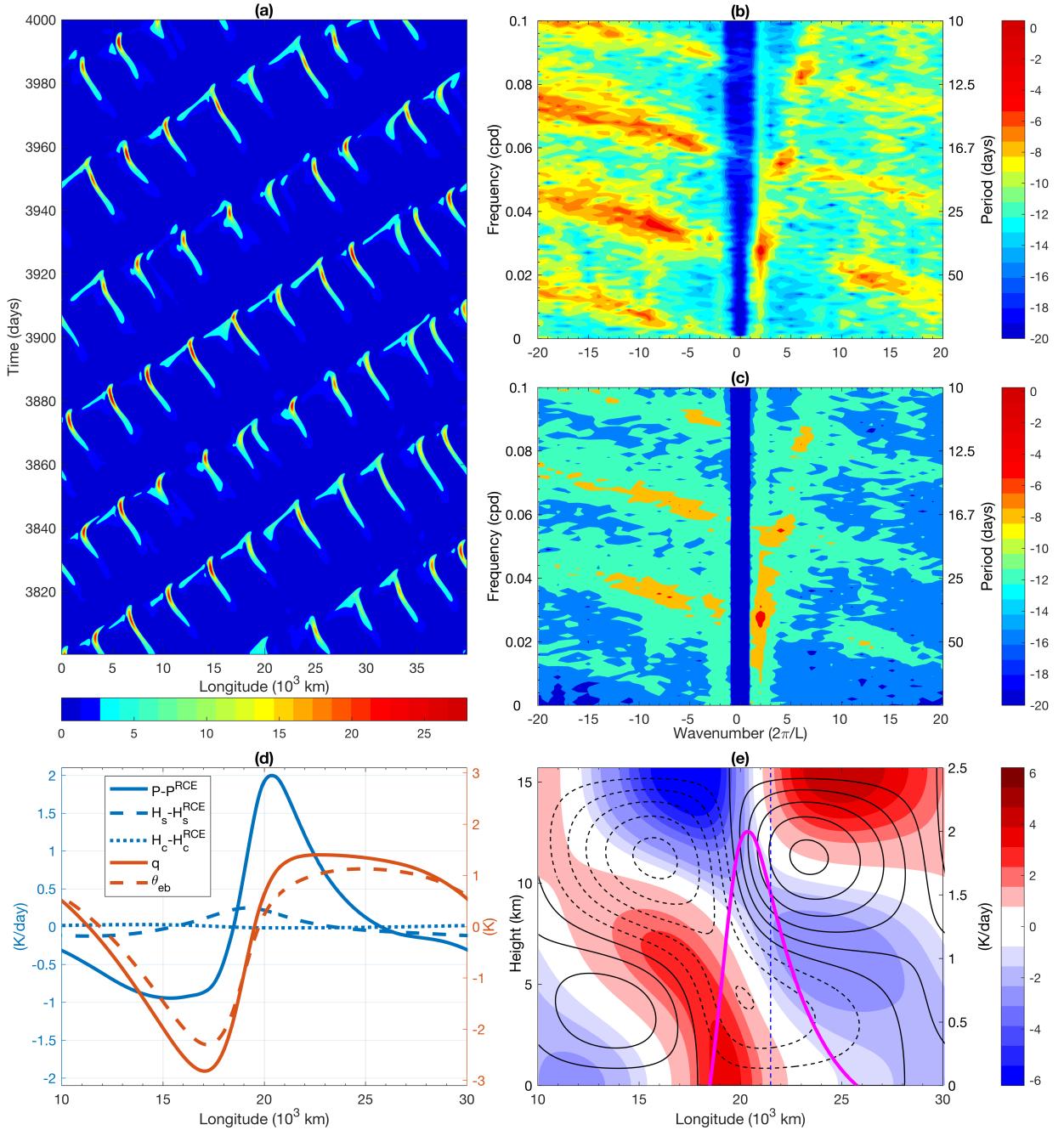
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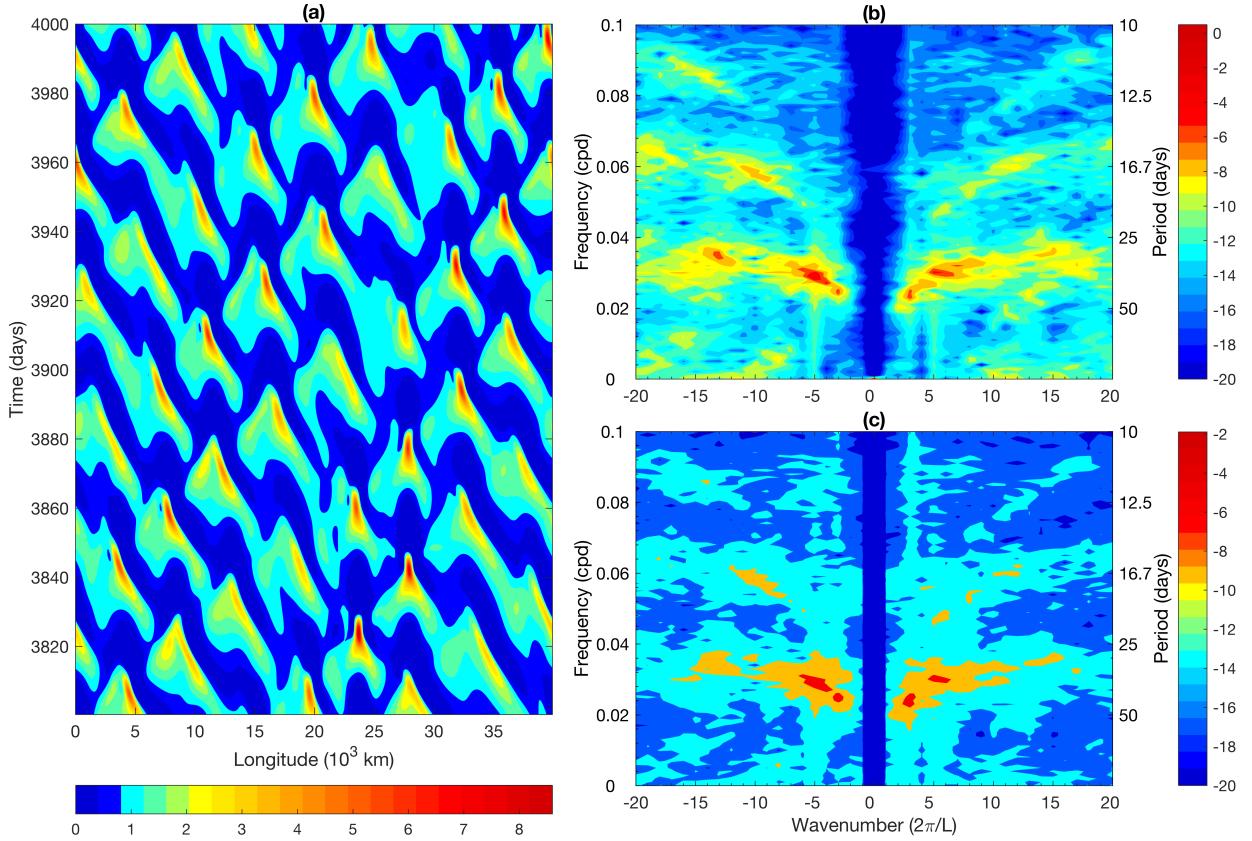
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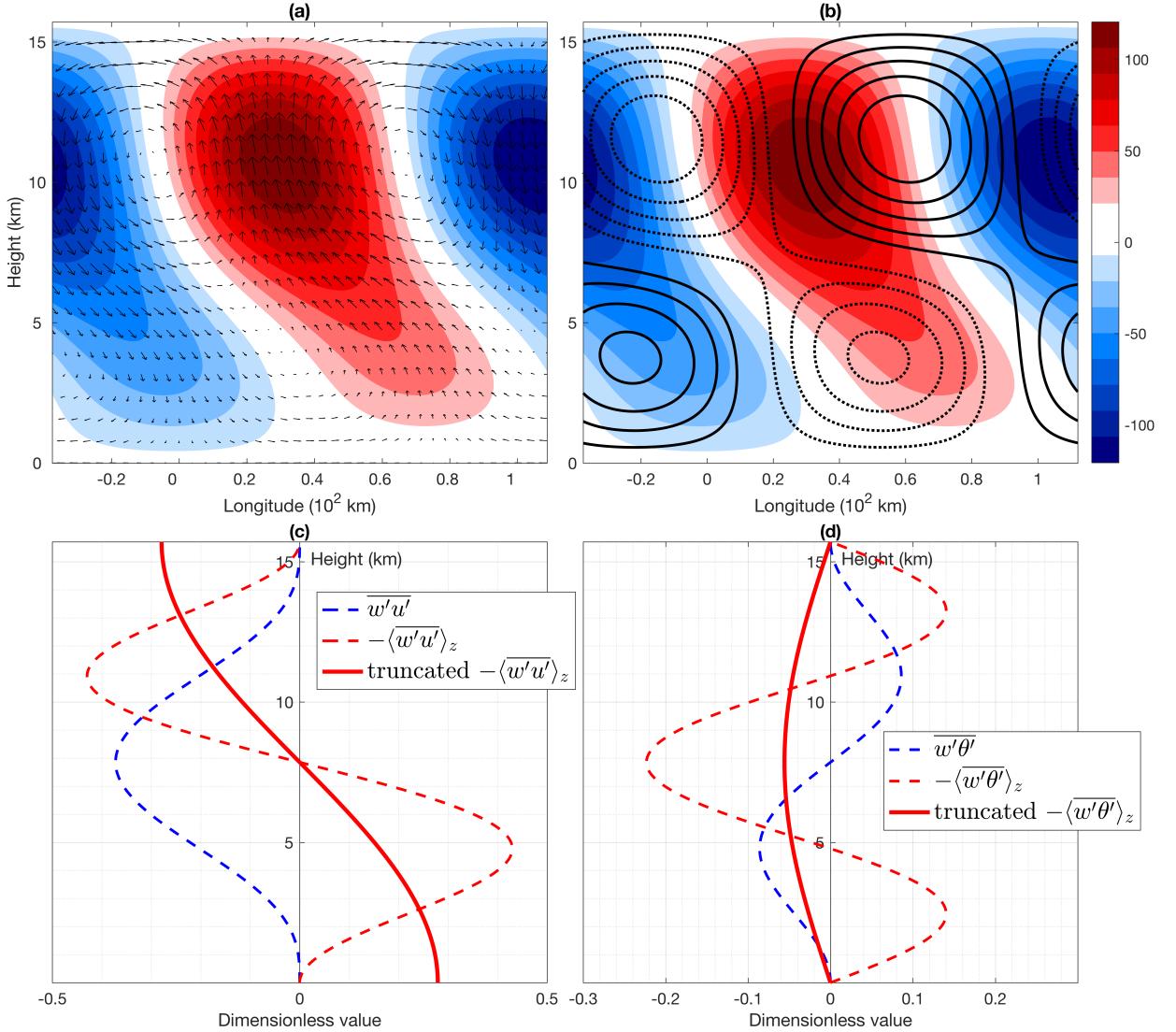
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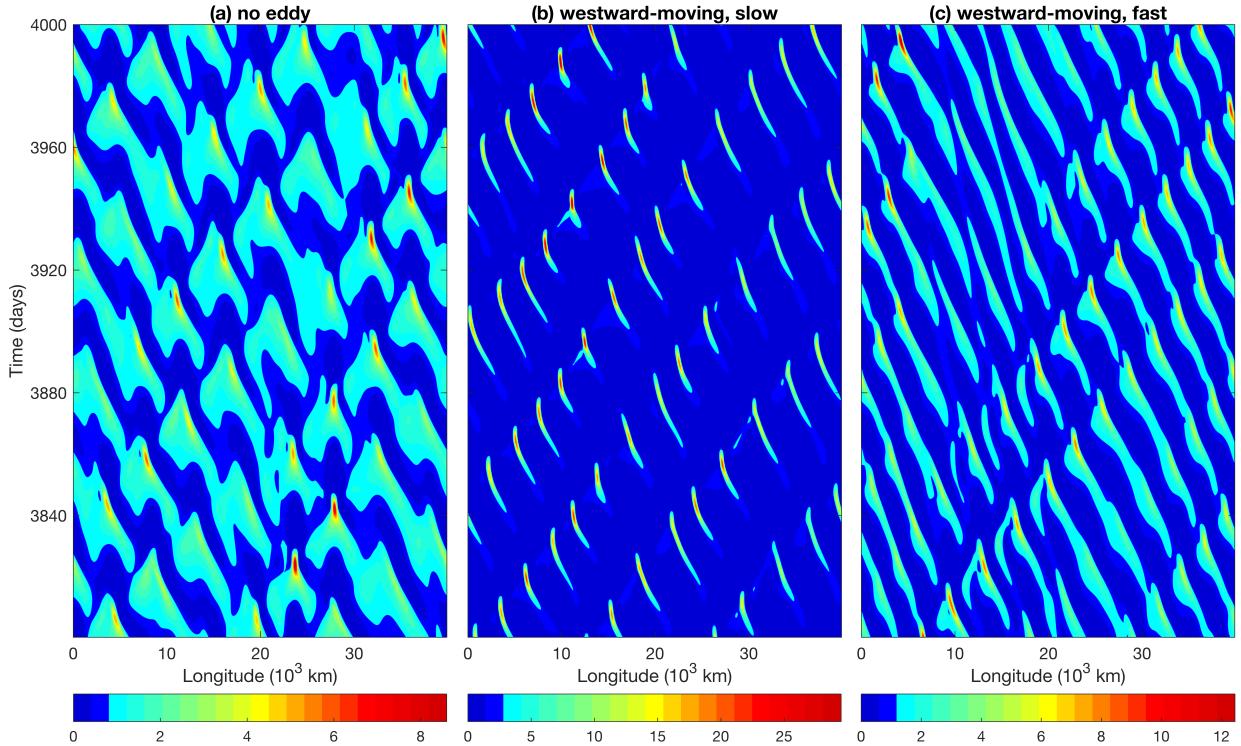
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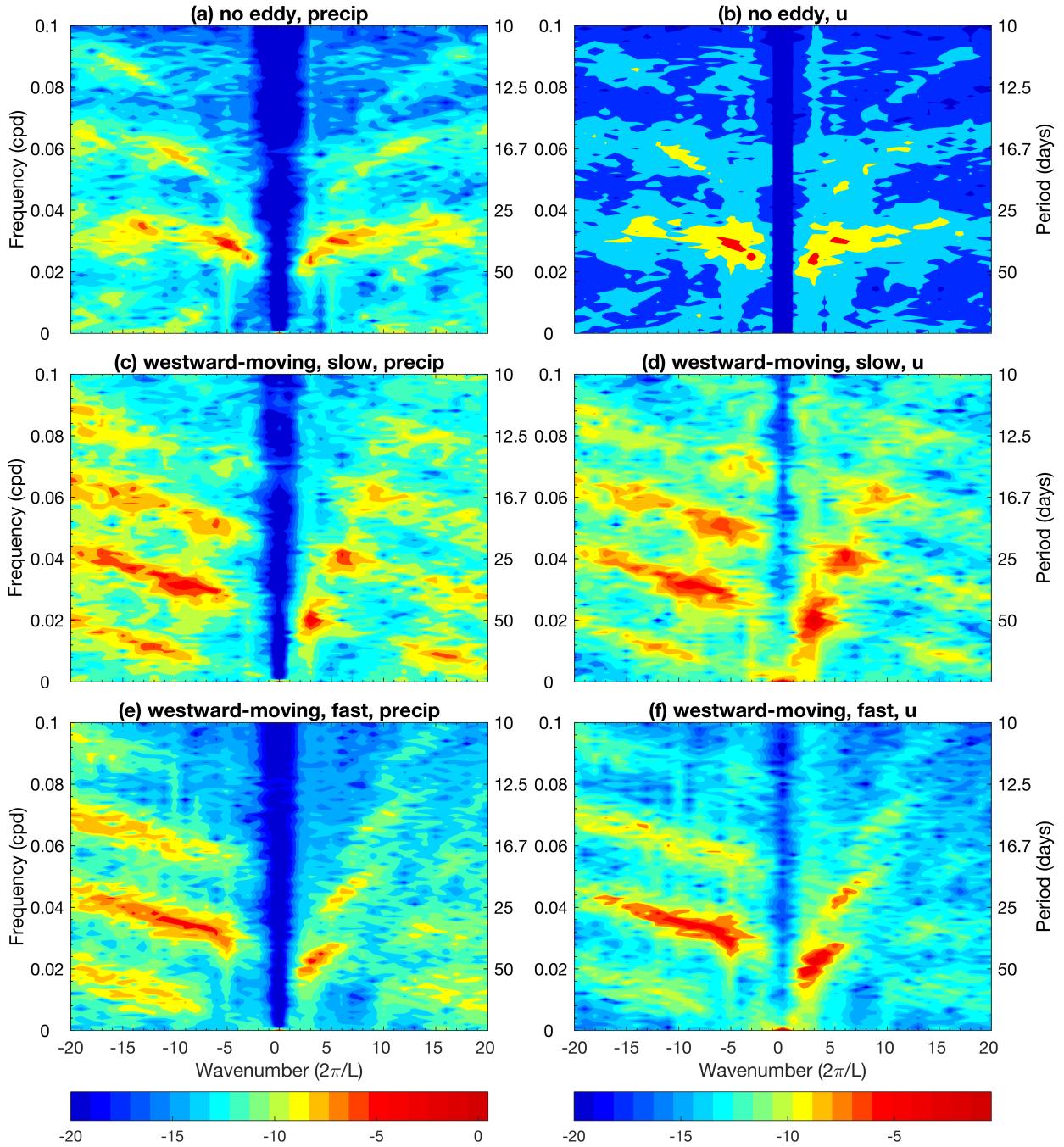
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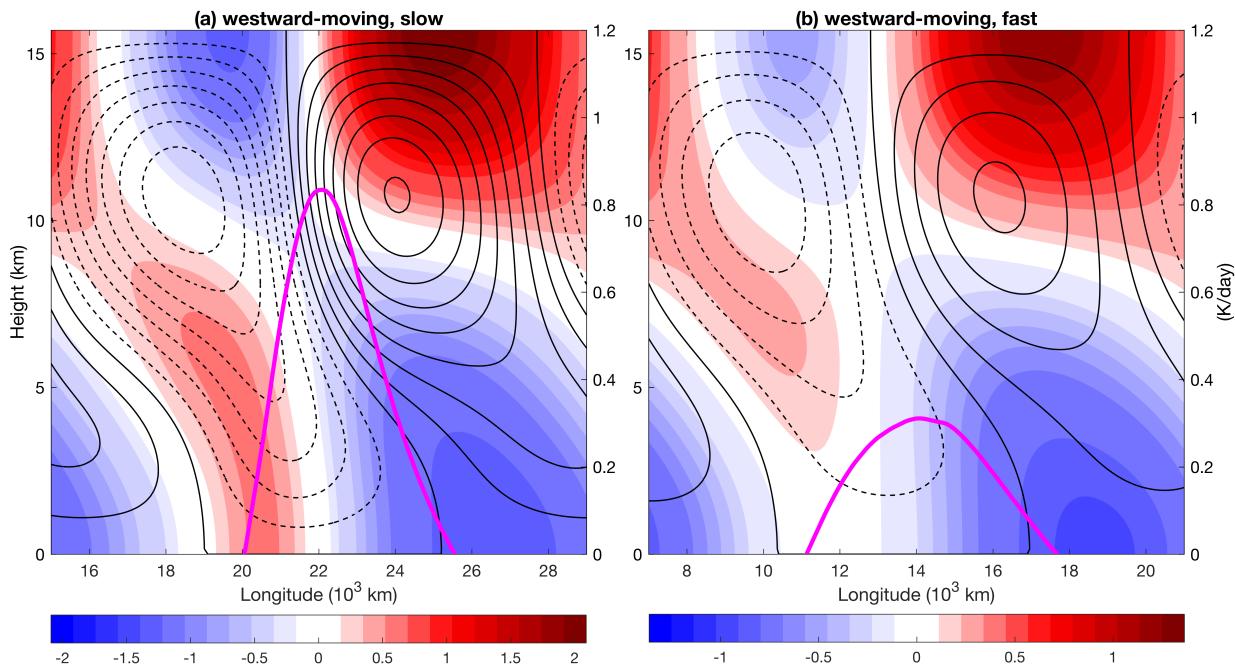
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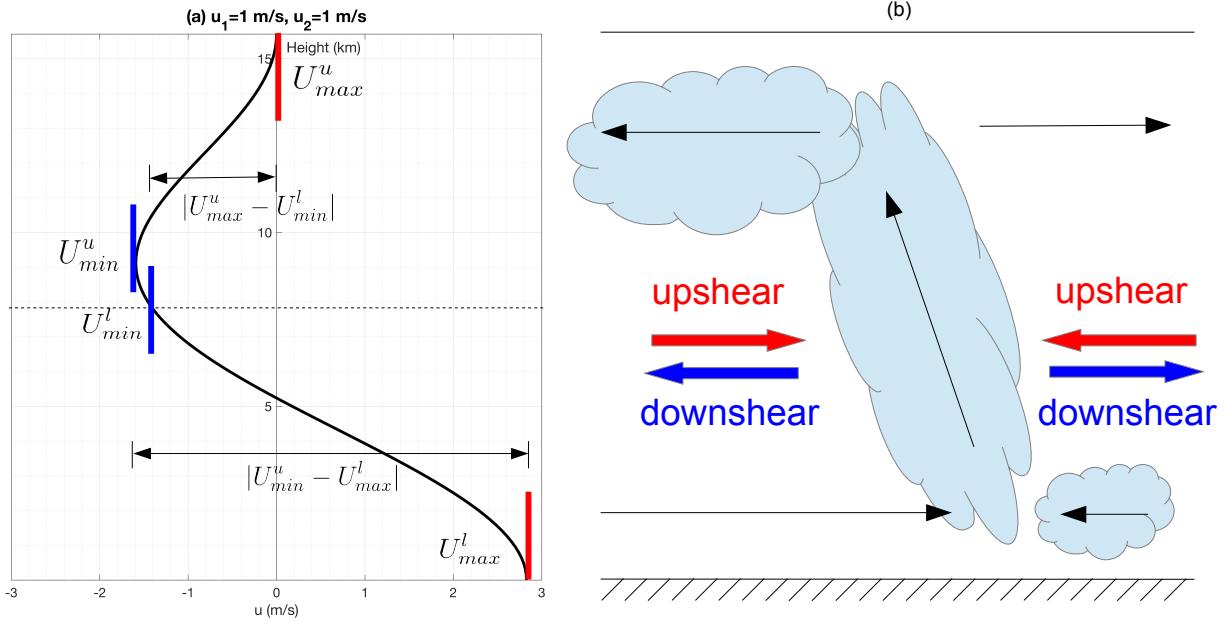
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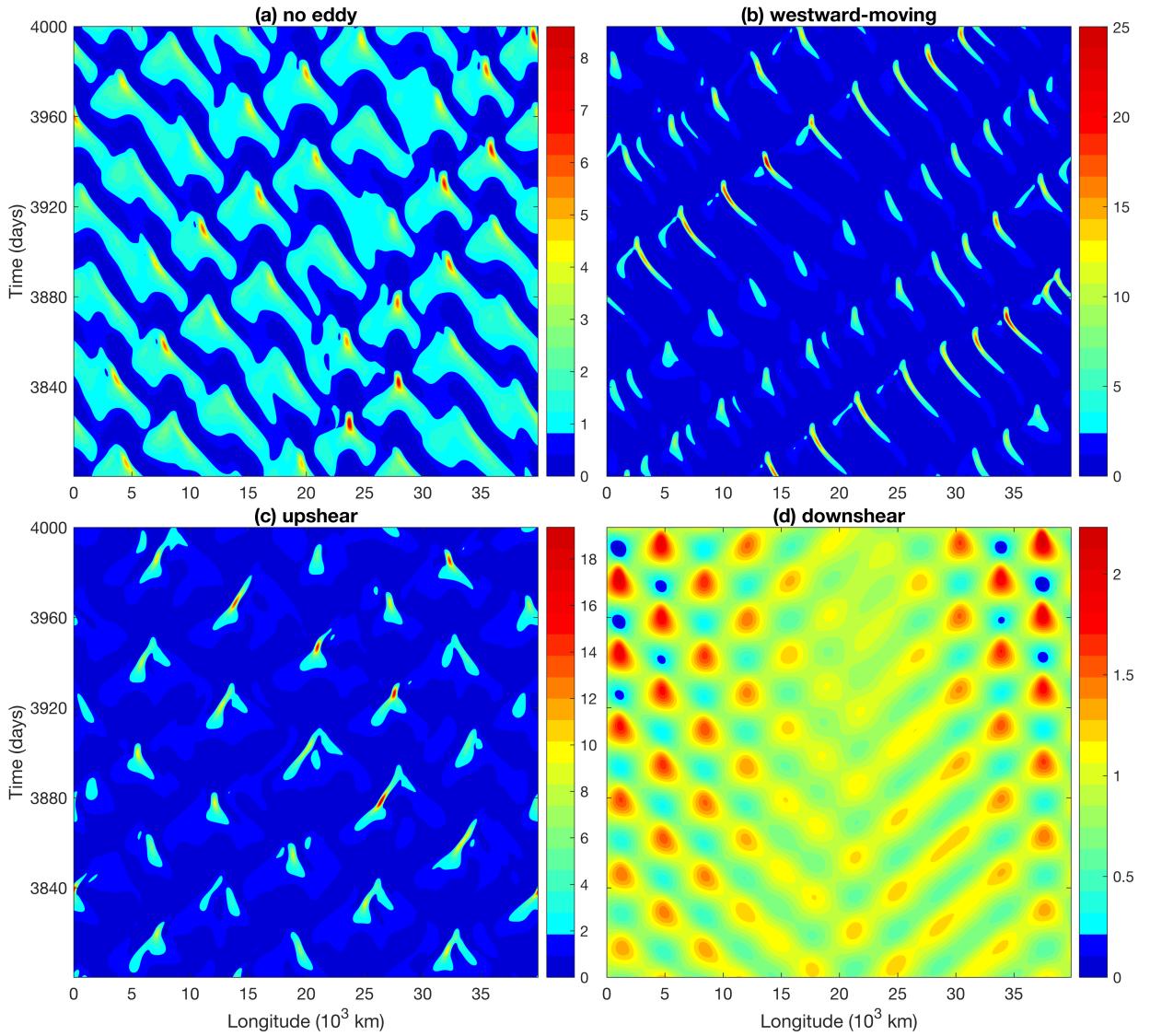
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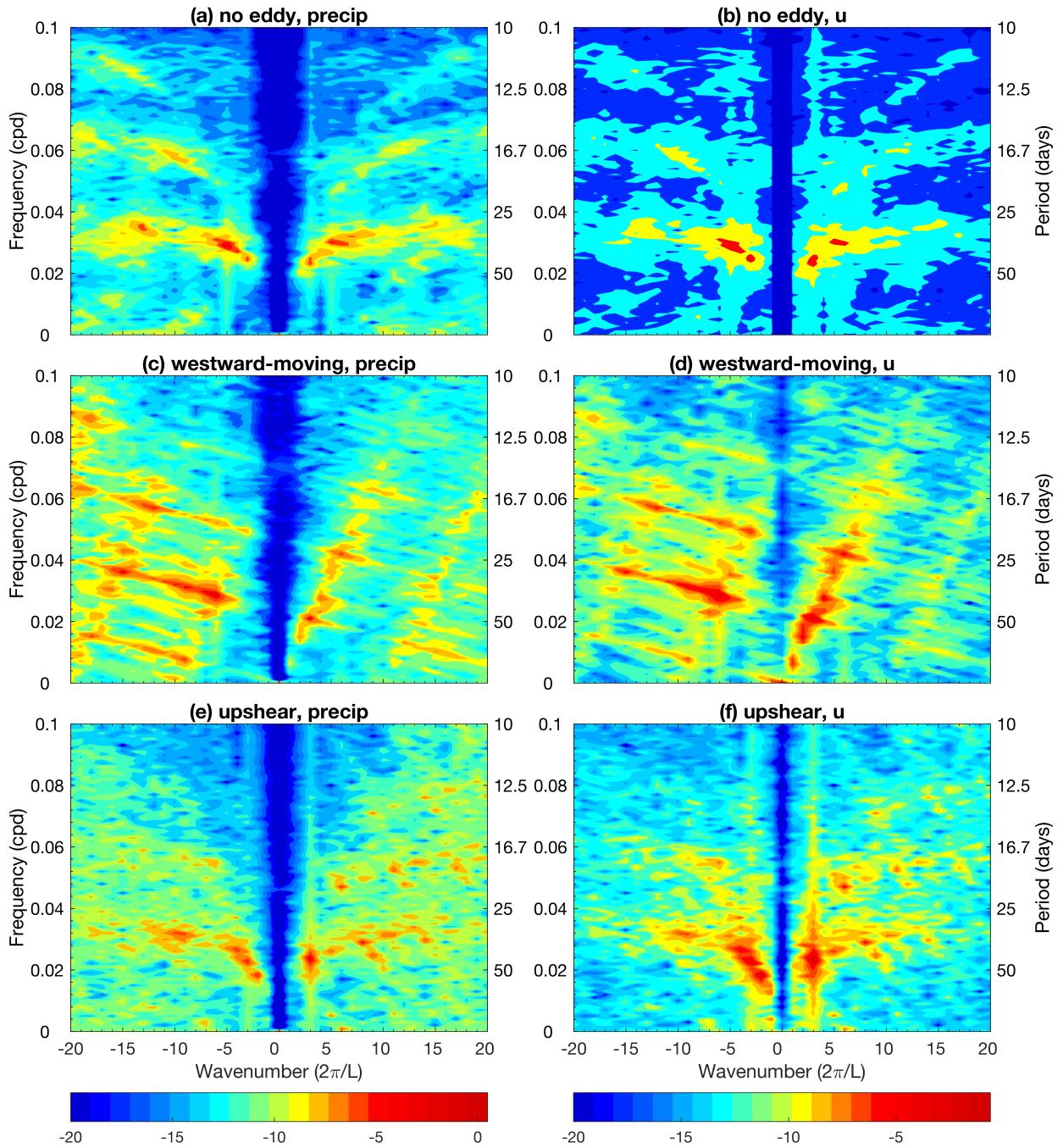
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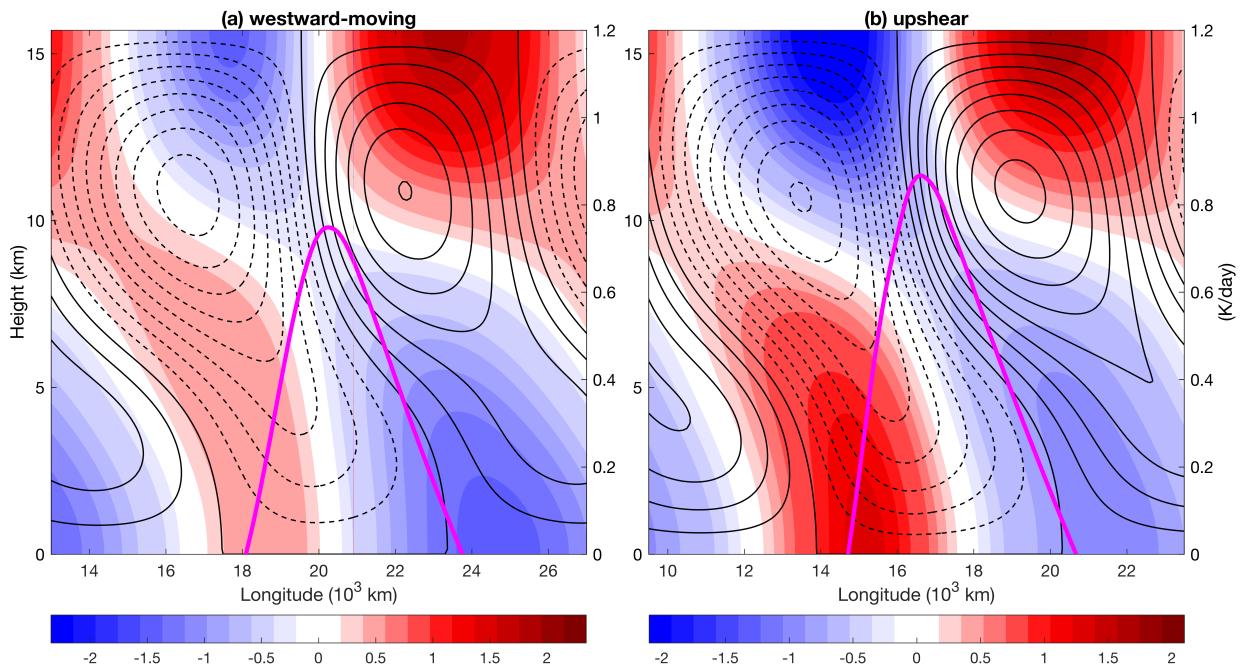
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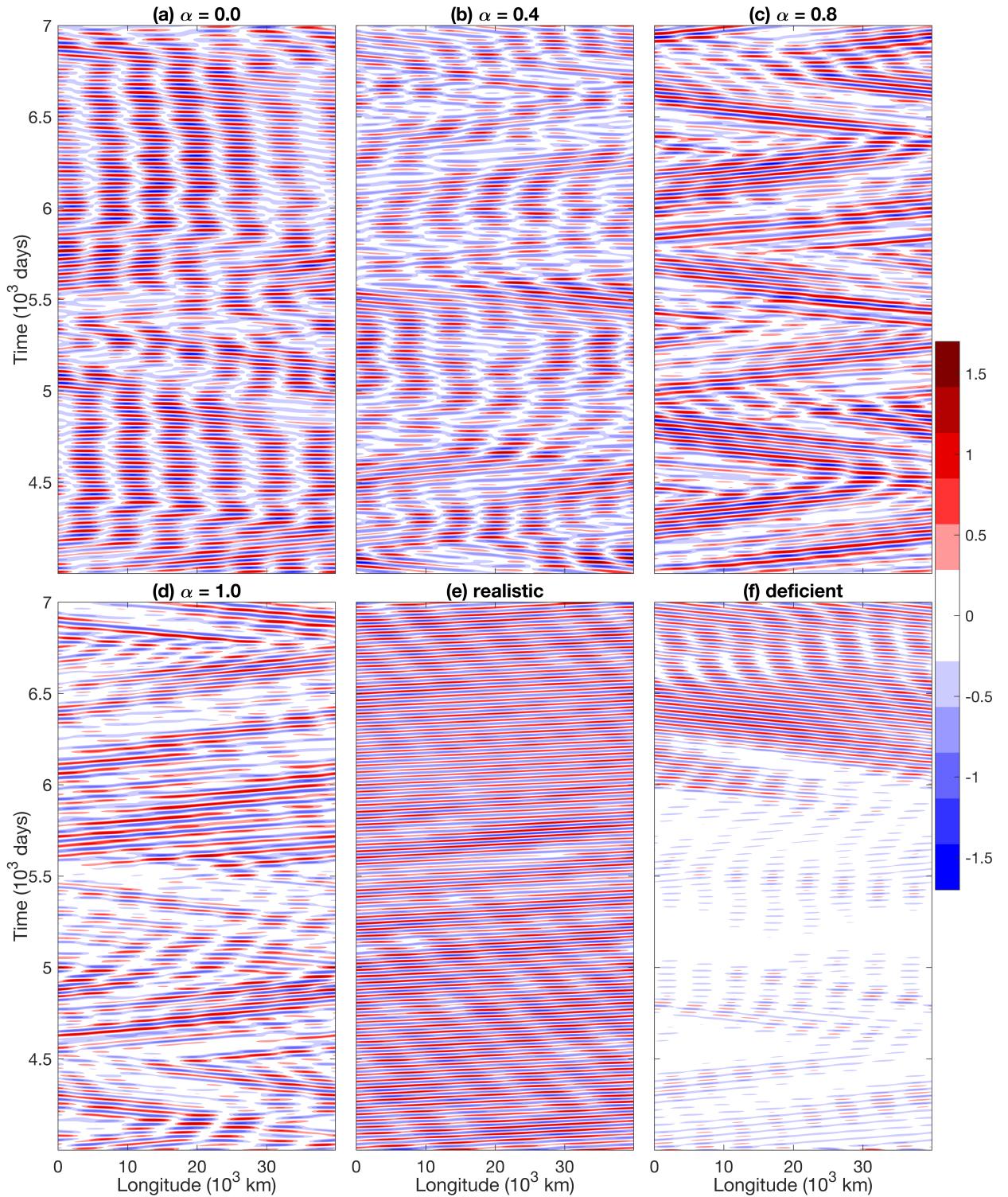
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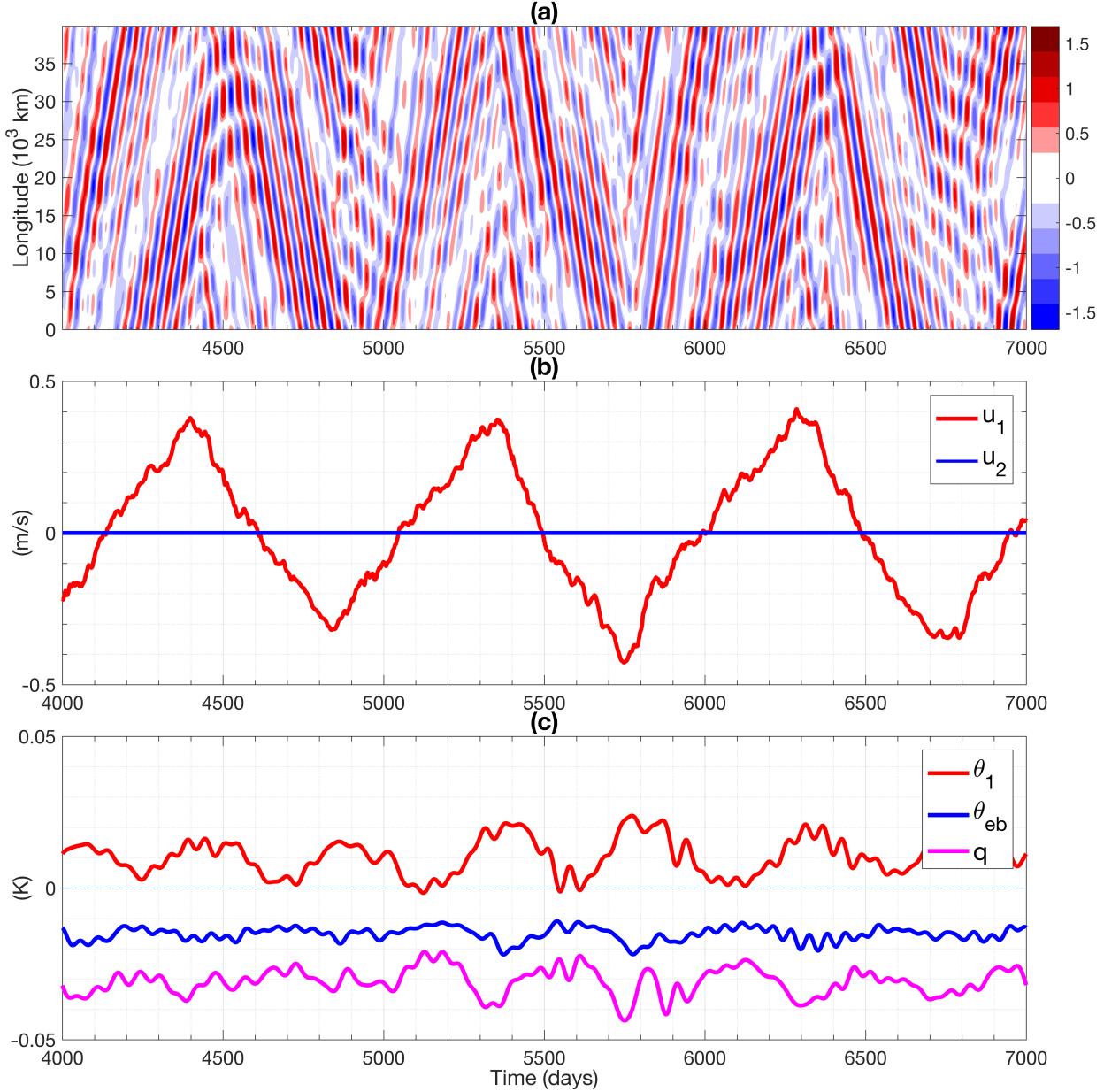
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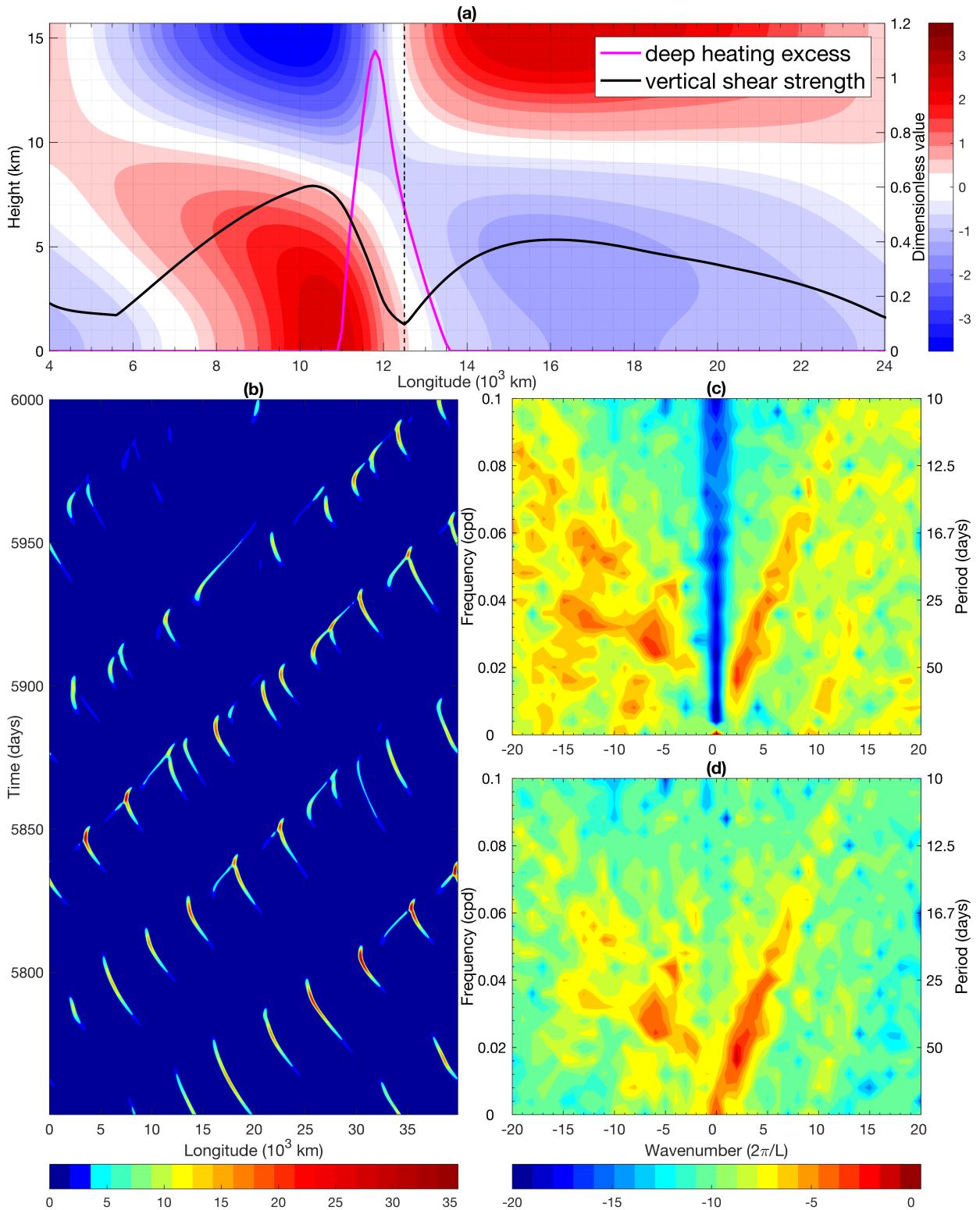
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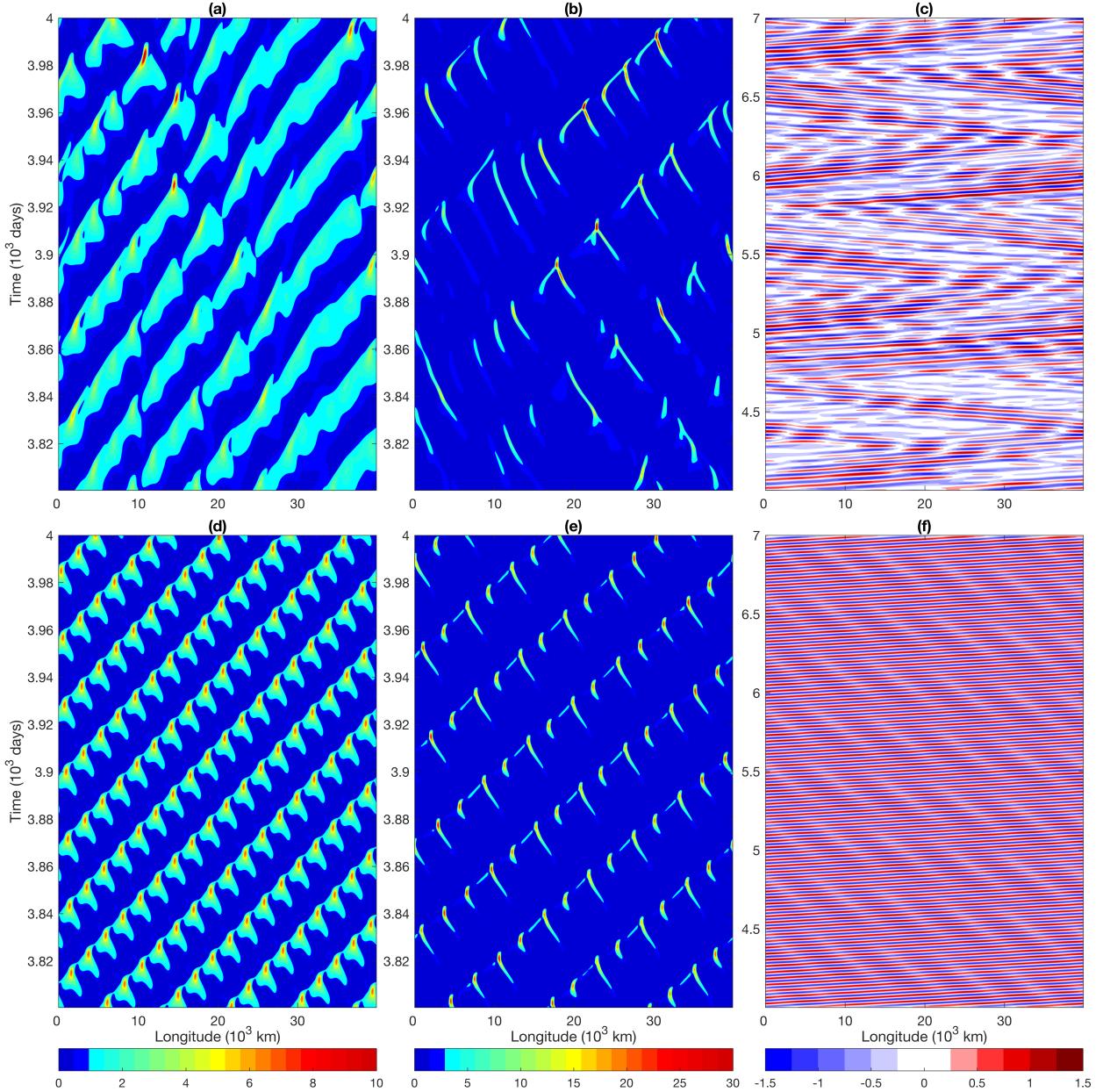
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1035 FIG. 12. Time series of precipitation, zonal velocity and thermodynamical fields between day 4000 and day  
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 1037 Fig.11c), while panel (b) and (c) show domain-mean zonal velocity ( $u_1$  and  $u_2$ ) and thermodynamic fields (first-  
 1038 baroclinic potential temperature  $\theta_1$ , boundary-layer equivalent potential temperature  $\theta_{eb}$ , moisture  $q$ ) during the  
 1039 same period, respectively. Only anomalies of these thermodynamic fields ( $\theta_1, \theta_{eb}, q$ ) on the time scale longer  
 1040 than 50 days are retained by using the low-pass filter. The units of precipitation and zonal velocity are  $K day^{-1}$ ,  
 1041  $ms^{-1}$ , respectively.



1042 FIG. 13. An idealized GCM with clear deficiencies and extra parameterization for upscale impact of MCSs  
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1051 FIG. 14. Hovmöller diagrams for precipitation from deficient GCMs and improved simulations by the param-  
 1052 eterization of upscale impact of MCSs. Panel (a) shows the solutions from the deficient GCM with  $\tilde{Q} = 1.03$  and  
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 1056 for the other deficient GCM with  $a_0 = 32$ . Panels in each column share the same colorbar in the bottom. The  
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