



# Modeling of Cortical Network Dynamics

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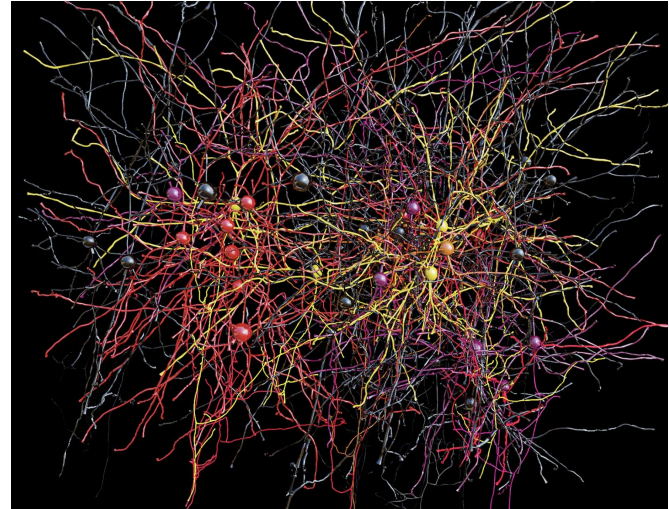
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# Biological Networks in the Brain

The human brain contains:

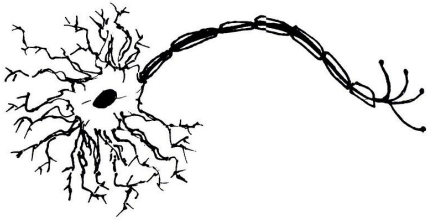
- $10^{10}$  neurons
- $10^{14}$  synapses/connections

A **neuron** is the most fundamental unit for neurocomputation in the brain.

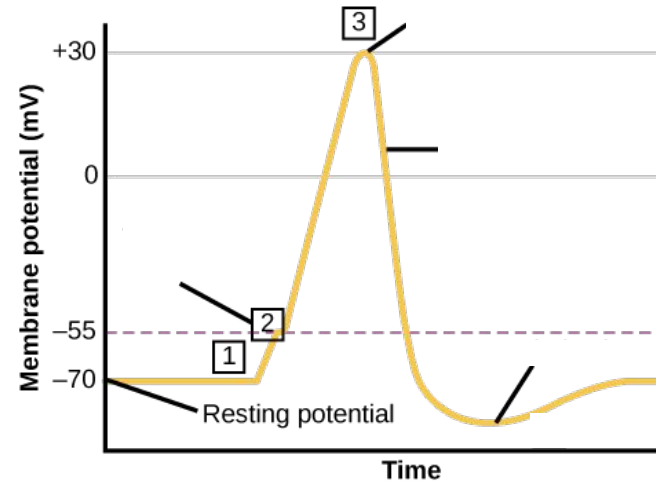


de Vries, S.E.J., Lecoq, J.A., Buice, M.A. et al.

# Neuronal Dynamics



Behaves similar to an electrical capacitor.

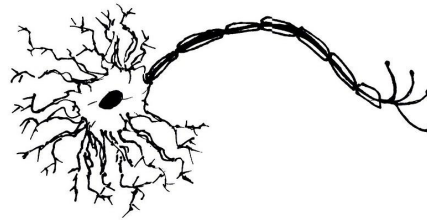


# How do neurons communicate?

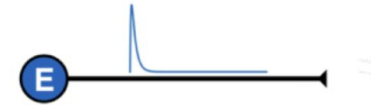
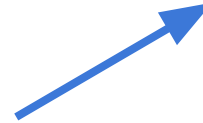
Excitatory  
Neuron



Inhibitory  
Neuron



Gerstner, Wulfram, et al.

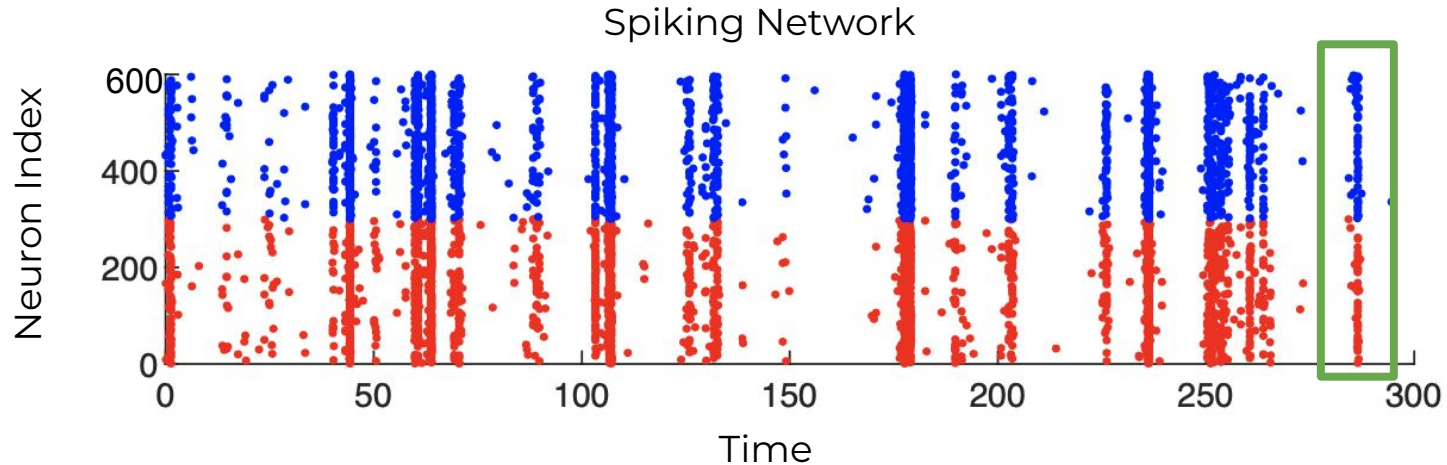


Depolarization



Hyperpolarization

# Multiple Firing Events (MFEs)



A class of significant firing patterns of neurons exhibiting transient synchrony produced by the recurrent interactions between neurons.

# Issues with Modeling Cortical Networks

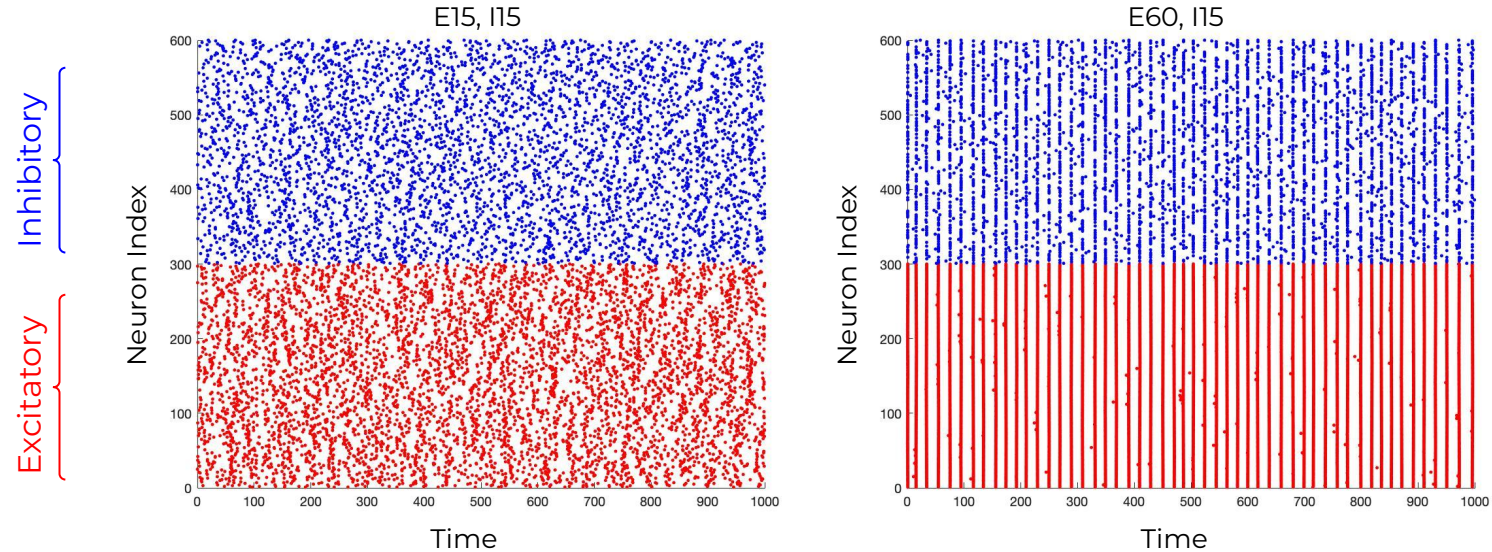
Coupled spiking networks have proven to be successful in modeling the brain and serve as a central aspect of computational neuroscience.

However, large spiking networks are hard to analyze and computationally expensive to simulate due to:

1. High-Dimensionality
2. Nonlinearity

**Research Question:** Can we successfully utilize machine learning to explore multiple firing events (MFEs)?

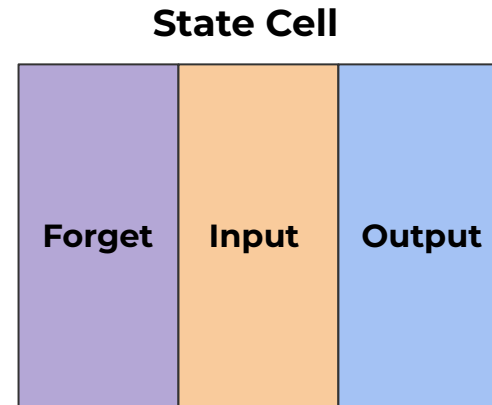
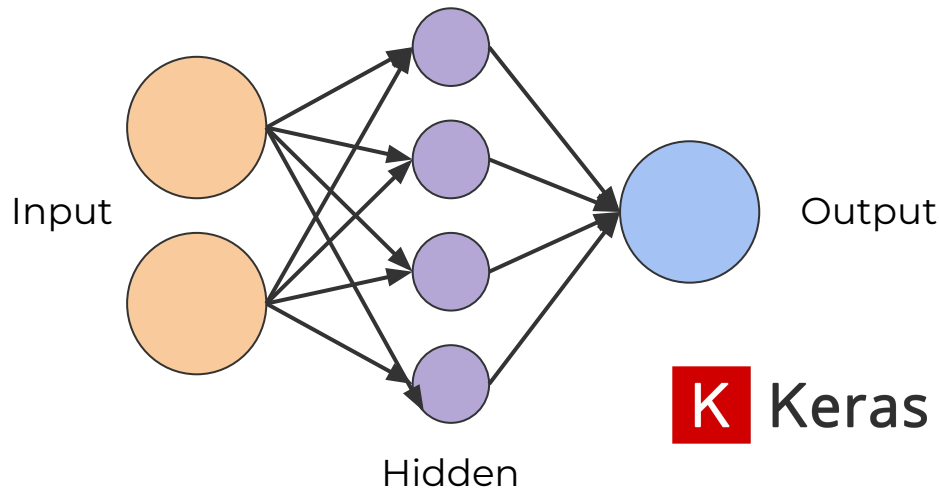
# Simulating Spiking Data



Through varying degrees of connections, we can notice synchronicity between spiking patterns.

# Modeling Spiking Networks with LSTMs

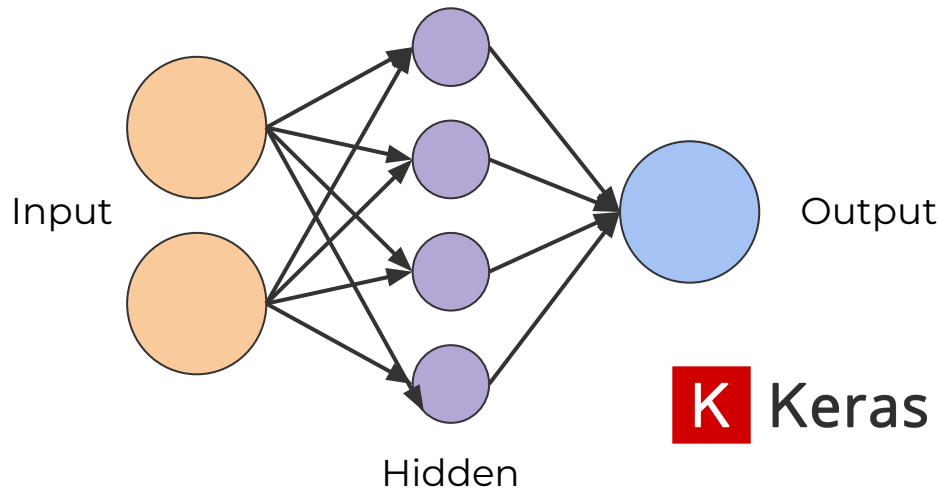
Multiple Firing Events (MFEs) are a temporal dynamic. Therefore, since we are dealing with time series data, we will utilize Long-Short Term Memory Networks (LSTMs), which are adept at extracting intrinsic dimensionality of the dynamics of the system.





# Modeling Spiking Networks with LSTMs

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**State Cell**

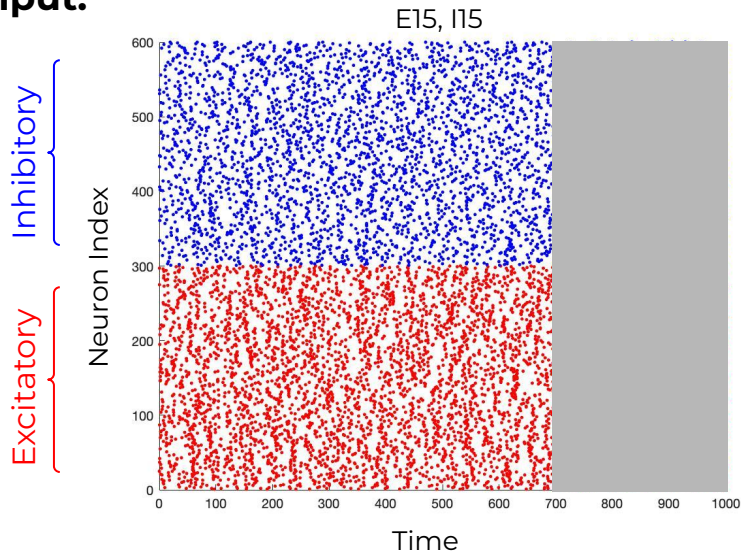
Our goal is to minimize the loss function

A diagram of an LSTM cell structure showing three gates: **Forget** (purple), **Input** (orange), and **Output** (blue). The text "Our goal is to minimize the loss function" is positioned above the diagram. To the right of the diagram, the text "cales," is partially visible.

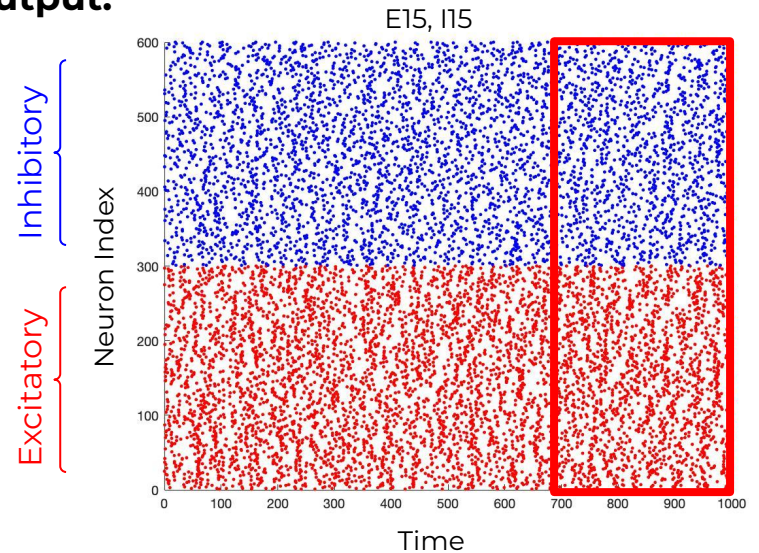
“vanishing gradient.”

# Model Parameters

**Input:**



**Output:**



# Predictions for Time-Series

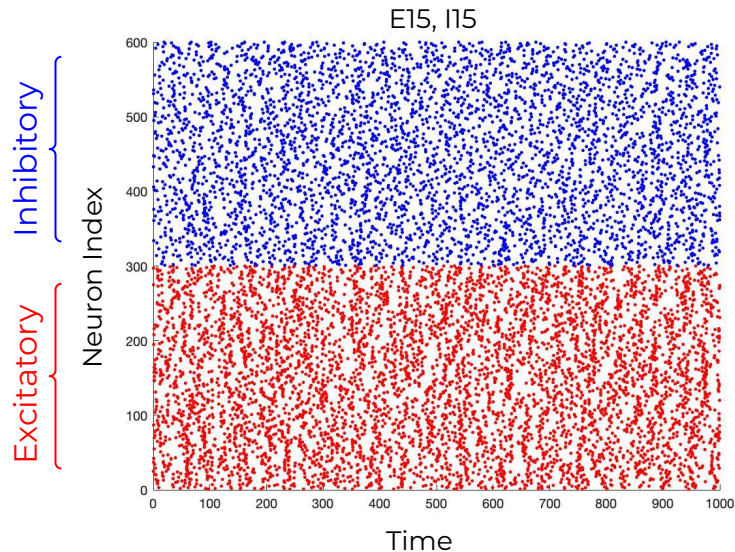
Accuracy over a hundred predictions: **54.7%**

Issues:

- Data is 600-dimensional over 1000 time steps
- Sample Data:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Revised Model Parameters



Sum of Excitatory Spikes  
over Time

Sum of Inhibitory Spikes  
over Time

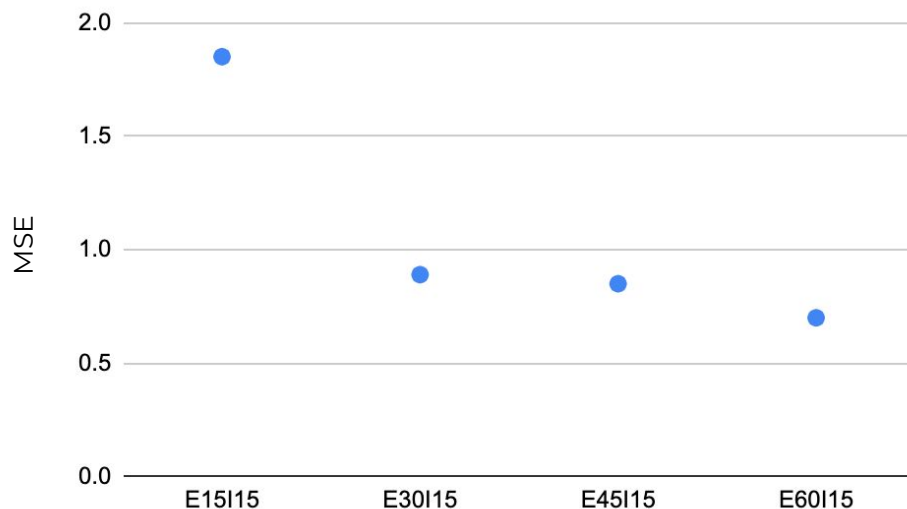
Since our objective is to study MFEs, we can reduce the dimensionality of the model while still being able to observe the synchronicity of the outputs.

# Predictions for Time-Series

Error Metric: MSE

$$J(\theta) = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Average MSE over a hundred predictions: **2.11**



# Conclusions

- Shows promise in determining the intrinsic dynamics of a neural system based off of its excitatory and inhibitory connections
- However, accuracy can be further improved

# Future Work

- Factor in external signals inputted into our simulation model
- Create classification machine learning models with input as time series and output as ratio of excitatory and inhibitory connections

# References

1. de Vries, S.E.J., Lecoq, J.A., Buice, M.A. et al. A large-scale standardized physiological survey reveals functional organization of the mouse visual cortex. *Nat Neurosci* 23, 138–151 (2020).  
<https://doi.org/10.1038/s41593-019-0550-9>
2. Gerstner, Wulfram, et al. “O Foundations of Neuronal Dynamics.” *Neuronal Dynamics from Single Neurons to Networks and Models of Cognition*, Cambridge University Press, Cambridge, 2016.
3. Xiao ZC, Lin KK. Multilevel monte carlo for cortical circuit models. *J Comput Neurosci*. 2022 Feb;50(1):9-15. doi: 10.1007/s10827-021-00807-3. Epub 2022 Jan 9. PMID: 35000059.