## Hint for problem 6, set 6

One way to do this is to show that $f^{(n+1)}(z)=0$ at every point $z$. Do this by looking at $M(R) / R^{n}$ for $1 \leq R \leq 2$ (it is bounded there) then use the recursion to get to larger $R$. Now use the Cauchy integral formula for the $n+1$ st derivative at $z$. Your estimate of the integrand should involve $R-|z|$, where $R$ is chosen sufficiently large.

