## Ordinary Differential Equations

## Table of Laplace Transforms

Please memorize the following table of Laplace transforms. When doing this, please remember that $a$ and $s$ can be complex numbers.

| $f(t)$ | $F(s)$ |  |
| :---: | :---: | :--- |
| 1 | $\frac{1}{s}$ | The Heaviside function gives the same $F$. |
| $e^{a t}$ | $\frac{1}{s-a}$ | This rule includes the sine and cosine rules. |
| $t e^{a t}$ | $\left(\frac{1}{s-a}\right)^{2}$ | For problems with resonance. |
| $b_{1} f_{1}(t)+b_{2} f_{2}(t)$ | $b_{1} F_{1}(t)+b_{2} F_{2}(t)$ | This rule allows partial fractions. |
| $\dot{f}(t)$ | $s F(s)-f(0)$ | This transforms differential equations into algebra. |
| $\ddot{f}(t)$ | $s^{2} F(s)-\dot{f}(0)-s f(0)$ | This transforms differential equations into algebra. |

