Partial Differential Equations for Finance MATH-GA 2706, Spring 2014 Mondays 5:10-7pm WWH 512

TA details added 2/4/2014

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Prerequisites: Working knowledge of stochastic calculus, and basic familiarity with the Black-Scholes approach to option pricing.

Content: An introduction to those aspects of partial differential equations and optimal control most relevant to finance. PDE's naturally associated to diffusion processes: the forward and backward Kolmogorov equations and their applications. Linear parabolic equations: fundamental solution, boundary value problems, maximum principle. Dynamic programming and optimal control: Hamilton-Jacobi-Bellman equation, verification arguments, optimal stopping. Applications to finance will be distributed throughout the course, including: barrier options; options on an underlying that can jump; portfolio optimization; American options; and other examples of optimal decision-making.

Special Dates: First lecture 1/27. No lecture 2/17 (Presidents' Day) and 3/17 (Spring Break). The final exam will be Mon 5/19, 5:10-7pm (our normal slot, during exam week).

Homeworks, exams, grades: There will be 6 or 7 homework sets, and a final exam. Grades will be based on the HW (1/2) and the final (1/2). Collaboration on HW is encouraged (homeworks are not exams), but students must write up and turn in their solutions individually. If you work closely with another student (or someone else, or you use other resources such as something on the web) please identify your collaborators and/or sources on your solution sheet. HW may be turned in late only by securing permission before it is due; no credit will be given for HW turned in after a solution sheet has been distributed. The HW is important not only because it counts as part of the grade, but also because it helps you master the material (and therefore helps you do well on the exam). The final will be closed-book, but you may bring two 8.5×11 sheets of notes (both sides, any font). Requests to take a makeup exam must be made in advance, and will not be granted for matters of personal convenience.

Resources: Lecture notes and homework sets will be posted on my website as they become available. An NYU-Classes site will be used for announcements, and for material I don't want to make public (such as HW solutions). Auditors can be added to the NYU-Classes site upon request. See a separate handout for a list of books that correlate with various parts of this class.

Semester plan: Lectures 1-2: the backward and forward Kolmogorov equations and their applications. Lectures 3-4: the linear heat equation – properties and solution formulas on the real line, a half-line, and an interval. Lectures 5-6: deterministic optimal control. Lectures 7-9: stochastic optimal control, including portfolio optimization, optimal stopping, and American options. Lectures 10-14: additional topics, including underlyings with jumps, the martingale approach to portfolio optimization, and asset price bubbles from heterogeneous expectations.