

17. $y = f(x) = x\sqrt{5-x}$ A. The domain is $\{x \mid 5-x \geq 0\} = (-\infty, 5]$ B. y -intercept: $f(0) = 0$;

x -intercepts: $f(x) = 0 \Leftrightarrow x = 0, 5$ C. No symmetry D. No asymptote

$$\text{E. } f'(x) = x \cdot \frac{1}{2}(5-x)^{-1/2}(-1) + (5-x)^{1/2} \cdot 1 = \frac{1}{2}(5-x)^{-1/2}[-x + 2(5-x)] = \frac{10-3x}{2\sqrt{5-x}} > 0 \Leftrightarrow x < \frac{10}{3},$$

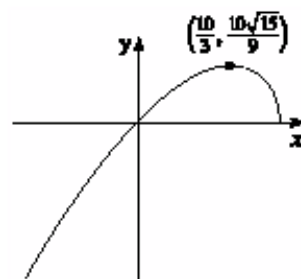
so f is increasing on $(-\infty, \frac{10}{3})$ and decreasing on $(\frac{10}{3}, 5)$.

F. Local maximum value $f(\frac{10}{3}) = \frac{10}{9}\sqrt{15} \approx 4.3$; no local minimum

$$\begin{aligned} \text{G. } f''(x) &= \frac{2(5-x)^{1/2}(-3) - (10-3x) \cdot 2(\frac{1}{2})(5-x)^{-1/2}(-1)}{(2\sqrt{5-x})^2} \\ &= \frac{(5-x)^{-1/2}[-6(5-x) + (10-3x)]}{4(5-x)} = \frac{3x-20}{4(5-x)^{3/2}} \end{aligned}$$

$f''(x) < 0$ for $x < 5$, so f is CD on $(-\infty, 5)$. No IP

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38. $y = f(x) = e^x/x$ A. $D = \{x \mid x \neq 0\}$ B. No intercept C. No symmetry D. $\lim_{x \rightarrow \infty} \frac{e^x}{x} \stackrel{H}{=} \lim_{x \rightarrow \infty} \frac{e^x}{1} = \infty$,

$$\lim_{x \rightarrow -\infty} \frac{e^x}{x} = 0, \text{ so } y = 0 \text{ is a HA. } \lim_{x \rightarrow 0^+} \frac{e^x}{x} = \infty, \lim_{x \rightarrow 0^-} \frac{e^x}{x} = -\infty, \text{ so } x = 0 \text{ is a VA. E. } f'(x) = \frac{xe^x - e^x}{x^2} > 0 \Leftrightarrow$$

$(x-1)e^x > 0 \Leftrightarrow x > 1$, so f is increasing on $(1, \infty)$, and decreasing on $(-\infty, 0)$ and $(0, 1)$.

F. $f(1) = e$ is a local minimum value.

$$\text{G. } f''(x) = \frac{x^2(xe^x) - 2x(xe^x - e^x)}{x^4} = \frac{e^x(x^2 - 2x + 2)}{x^3} > 0 \Leftrightarrow x > 0$$

since $x^2 - 2x + 2 > 0$ for all x . So f is CU on $(0, \infty)$ and CD on $(-\infty, 0)$.

No IP

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