

## Assignment 4.

**Due Oct 16.**

**1.** If  $\{X_i\}$  are independent observations from the uniform distribution on  $[-\theta, \theta]$ , i.e with density given by

$$f(\theta, x) = \frac{1}{2\theta}; \quad -\theta \leq x \leq \theta$$

Is there a sufficient statistic? What is it? Why is it sufficient?

**2.** For the uniform distribution on  $[0, \theta)$ , i.e

$$f(\theta, x) = \frac{1}{\theta}; \quad 0 \leq x \leq \theta$$

take  $t = \max\{x_1, \dots, x_n\}$ . What is  $E[t]$ . Find a constant  $c$  such that  $u = ct$  is unbiased. What is the variance of  $u$ ? Is it consistent with Cramér-Rao bound?